Package 'lrstat'

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Type Package

Title Power and Sample Size Calculation for Non-Proportional Hazards
and Beyond

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Description Performs power and sample size calculation for non-proportional hazards model using the Fleming-Harrington family of weighted log-rank tests. The sequentially calculated log-rank test score statistics are assumed to have independent increments as characterized in Anastasios A. Tsiatis (1982) <doi:10.1080/01621459.1982.10477898>. The mean and variance of log-rank test score statistics are calculated based on Kaifeng Lu (2021) <doi:10.1002/pst.2069>. The boundary crossing probabilities are calculated using the recursive integration algorithm described in Christopher Jennison and Bruce W. Turnbull (2000, ISBN:0849303168). The package can also be used for continuous, binary, and count data. For continuous data, it can handle missing data through mixed-model for repeated measures (MMRM). In crossover designs, it can estimate direct treatment effects while accounting for carryover effects. For binary data, it can design Simon's 2-stage, modified toxicity probability-2 (mTPI-2), and Bayesian optimal interval (BOIN) trials. For count data, it can design group sequential trials for negative binomial endpoints with censoring. Additionally, it facilitates group sequential equivalence trials for all supported data types. Moreover, it can design adaptive group sequential trials for changes in sample size, error spending function, number and spacing or future looks. Finally, it offers various options for adjusted p-values, including graphical and gatekeeping procedures.

License GPL (>= 2)

Imports Rcpp (>= 1.0.9), mvtnorm (>= 1.1-3), lpSolve (>= 5.6.1), shiny
(>= 1.7.1)

LinkingTo Rcpp

Suggests testthat (>= 3.0.0), dplyr (>= 1.1.4), tidyr (>= 1.3.0),
knitr (>= 1.45), rmarkdown (>= 2.25), survival (>= 3.5-7)

VignetteBuilder knitr

RoxygenNote 7.3.1

Encoding UTF-8

NeedsCompilation yes

Depends R (>= 2.10)

LazyData true

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Contents

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lrstat-package   *Power and Sample Size Calculation for Non-Proportional Hazards and Beyond*

Description

Performs power and sample size calculation for non-proportional hazards model using the Fleming-Harrington family of weighted log-rank tests.

Details

For proportional hazards, the power is determined by the total number of events and the constant hazard ratio along with information rates and spending functions. For non-proportional hazards, the hazard ratio varies over time and the calendar time plays a key role in determining the mean and variance of the log-rank test score statistic. It requires an iterative algorithm to find the calendar time at which the targeted number of events will be reached for each interim analysis. The lrstat package uses the analytic method in Lu (2021) to find the mean and variance of the weighted log-rank test score statistic at each interim analysis. In addition, the package approximates the variance and covariance matrix of the sequentially calculated log-rank test statistics under the alternative hypothesis with that under the null hypothesis to take advantage of the independent increments structure in Tsiatis (1982) applicable for the Fleming-Harrington family of weighted log-rank tests.

The most useful functions in the package are `lrstat`, `lrpower`, `lrsamplesize`, and `lrsim`, which calculate the mean and variance of log-rank test score statistic at a sequence of given calendar times, the power of the log-rank test, the sample size in terms of accrual duration and follow-up duration, and the log-rank test simulation, respectively. The `accrual` function calculates the number of patients accrued at given calendar times. The `caltime` function finds the calendar times to reach the targeted number of events. The `exitprob` function calculates the stagewise exit probabilities for specified boundaries with a varying mean parameter over time based on an adaptation of the recursive integration algorithm described in Chapter 19 of Jennison and Turnbull (2000).

The development of the lrstat package is heavily influenced by the rpact package. We find their function arguments to be self-explanatory. We have used the same names whenever appropriate so that users familiar with the rpact package can learn the lrstat package quickly. However, there are notable differences:

- lrstat uses direct approximation, while rpact uses the Schoenfeld method for log-rank test power and sample size calculation.
- lrstat uses `accrualDuration` to explicitly set the end of accrual period, while rpact incorporates the end of accrual period in `accrualTime`.
- lrstat considers the trial a failure at the last stage if the log-rank test cannot reject the null hypothesis up to this stage and cannot stop for futility at an earlier stage.
- the `lrsim` function uses the variance of the log-rank test score statistic as the information.

In addition to the log-rank test power and sample size calculations, the lrstat package can also be used for the following tasks:

- design generic group sequential trials.

- design generic group sequential equivalence trials.
- design adaptive group sequential trials for changes in sample size, error spending function, number and spacing or future looks.
- calculate the terminating and repeated confidence intervals for standard and adaptive group sequential trials.
- calculate the conditional power for non-proportional hazards with or without design changes.
- perform multiplicity adjustment based on graphical approaches using weighted Bonferroni tests, Bonferroni mixture of weighted Simes test, and Bonferroni mixture of Dunnett test as well as group sequential trials with multiple hypotheses.
- perform multiplicity adjustment using stepwise gatekeeping procedures for two sequences of hypotheses and the standard or modified mixture gatekeeping procedures in the general case.
- design parallel-group trials with the primary endpoint analyzed using mixed-model for repeated measures (MMRM).
- design crossover trials to estimate direct treatment effects while accounting for carryover effects.
- design one-way repeated measures ANOVA trials.
- design two-way ANOVA trials.
- design Simon's 2-stage trials.
- design modified toxicity probability-2 (mTPI-2) trials.
- design Bayesian optimal interval (BOIN) trials.
- design group sequential trials for negative binomial endpoints with censoring.
- design trials using Wilcoxon, Fisher's exact, and McNemar's test.
- calculate Clopper-Pearson confidence interval for single proportions.
- calculate Brookmeyer-Crowley confidence interval for quantiles of censored survival data.
- calculate Miettinen & Nurminen confidence interval for stratified risk difference, risk ratio, odds ratio, rate difference, and rate ratio.
- perform power and sample size calculation for logistic regression.
- perform power and sample size calculation for Cohen's kappa.
- calculate Hedges' g effect size.
- generate random numbers from truncated piecewise exponential distribution.
- perform power and sample size calculations for negative binomial data.

Author(s)

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References

Anastasios A. Tsiatis. Repeated significance testing for a general class of statistics used in censored survival analysis. J Am Stat Assoc. 1982;77:855-861.

Christopher Jennison, Bruce W. Turnbull. Group Sequential Methods with Applications to Clinical Trials. Chapman & Hall/CRC: Boca Raton, 2000, ISBN:0849303168

Kaifeng Lu. Sample size calculation for logrank test and prediction of number of events over time. Pharm Stat. 2021;20:229-244.

See Also

rpact, gsDesign

Examples

```
lrpower(kMax = 2, informationRates = c(0.8, 1),
        criticalValues = c(2.250, 2.025), accrualIntensity = 20,
        piecewiseSurvivalTime = c(0, 6),
        lambda1 = c(0.0533, 0.0309), lambda2 = c(0.0533, 0.0533),
        gamma1 = 0.00427, gamma2 = 0.00427,
        accrualDuration = 22, followupTime = 18)
```

---

accrual   *Number of Enrolled Subjects*

Description

Obtains the number of subjects enrolled by given calendar times.

Usage

```
accrual(
  time = NA_real_,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  accrualDuration = NA_real_
)
```

Arguments

time   A vector of calendar times at which to calculate the number of enrolled subjects.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity
                 A vector of accrual intensities. One for each accrual time interval.

accrualDuration
                 Duration of the enrollment period.

Value

A vector of total number of subjects enrolled by the specified calendar times.

Author(s)

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Examples

```
# Example 1: Uniform enrollment with 20 patients per month for 12 months.

accrual(time = 3, accrualTime = 0, accrualIntensity = 20,
        accrualDuration = 12)


# Example 2: Piecewise accrual, 10 patients per month for the first
# 3 months, and 20 patients per month thereafter. Patient recruitment
# ends at 12 months for the study.

accrual(time = c(2, 9), accrualTime = c(0, 3),
        accrualIntensity = c(10, 20), accrualDuration = 12)
```

---

adaptDesign   *Adaptive Design at an Interim Look*

Description

Obtains the conditional power for specified incremental information given the interim results, parameter value, and data-dependent changes in the error spending function, and the number and spacing of interim looks. Conversely, obtains the incremental information needed to attain a specified conditional power given the interim results, parameter value, and data-dependent changes in the error spending function, and the number and spacing of interim looks.

Usage

```
adaptDesign(
  betaNew = NA_real_,
  INew = NA_real_,
  L = NA_integer_,
  zL = NA_real_,
  theta = NA_real_,
  IMax = NA_real_,
  kMax = NA_integer_,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
```

```
    spendingTime = NA_real_,
    MullerSchafer = 0L,
    kNew = NA_integer_,
    informationRatesNew = NA_real_,
    efficacyStoppingNew = NA_integer_,
    futilityStoppingNew = NA_integer_,
    typeAlphaSpendingNew = "sfOF",
    parameterAlphaSpendingNew = NA_real_,
    typeBetaSpendingNew = "none",
    parameterBetaSpendingNew = NA_real_,
    userBetaSpendingNew = NA_real_,
    spendingTimeNew = NA_real_,
    varianceRatio = 1
)
```

Arguments

betaNew   The type II error for the secondary trial.

INew   The maximum information of the secondary trial. Either betaNew or INew
                 should be provided while the other one should be missing.

L   The interim adaptation look of the primary trial.

zL   The z-test statistic at the interim adaptation look of the primary trial.

theta   The parameter value.

IMax   The maximum information of the primary trial. Must be provided if futilityBounds
                 is missing and typeBetaSpending is not equal to "none", or if conditional
                 power calculation is desired.

kMax   The maximum number of stages of the primary trial.

informationRates
                 The information rates of the primary trial.

efficacyStopping
                 Indicators of whether efficacy stopping is allowed at each stage of the primary
                 trial. Defaults to true if left unspecified.

futilityStopping
                 Indicators of whether futility stopping is allowed at each stage of the primary
                 trial. Defaults to true if left unspecified.

criticalValues   The upper boundaries on the z-test statistic scale for efficacy stopping for the
                 primary trial.

alpha   The significance level of the primary trial. Defaults to 0.025.

typeAlphaSpending
                 The type of alpha spending for the primary trial. One of the following: "OF"
                 for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang &
                 Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP"
                 for Pocock type spending function, "sfKD" for Kim & DeMets spending func-
                 tion, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user
                 defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending
        The parameter value of alpha spending for the primary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending
        The user defined alpha spending for the primary trial. Cumulative alpha spent up to each stage.

futilityBounds   The lower boundaries on the z-test statistic scale for futility stopping for the primary trial. Defaults to rep(-6, kMax-1) if left unspecified.

typeBetaSpending
        The type of beta spending for the primary trial. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending
        The parameter value of beta spending for the primary trial. Corresponds to rho for "sfKD", and gamma for "sfHSD".

spendingTime   The error spending time of the primary trial. Defaults to missing, in which case, it is the same as informationRates.

MullerSchafer   Whether to use the Muller and Schafer (2001) method for trial adaptation.

kNew   The number of looks of the secondary trial.

informationRatesNew
        The spacing of looks of the secondary trial.

efficacyStoppingNew
        The indicators of whether efficacy stopping is allowed at each look of the secondary trial. Defaults to true if left unspecified.

futilityStoppingNew
        The indicators of whether futility stopping is allowed at each look of the secondary trial. Defaults to true if left unspecified.

typeAlphaSpendingNew
        The type of alpha spending for the secondary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpendingNew
        The parameter value of alpha spending for the secondary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

typeBetaSpendingNew
        The type of beta spending for the secondary trial. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpendingNew

    The parameter value of beta spending for the secondary trial. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpendingNew

    The user defined cumulative beta spending. Cumulative beta spent up to each stage of the secondary trial.

spendingTimeNew

    The error spending time of the secondary trial. Defaults to missing, in which case, it is the same as informationRatesNew.

varianceRatio   The ratio of the variance under H0 to the variance under H1.

Value

An adaptDesign object with two list components:

- primaryTrial: A list of selected information for the primary trial, including L, zL, theta, kMax, informationRates, efficacyBounds, futilityBounds, and MullerSchafer.
- secondaryTrial: A design object for the secondary trial.

Author(s)

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References

Lu Chi, H. M. James Hung, and Sue-Jane Wang. Modification of sample size in group sequential clinical trials. Biometrics 1999;55:853-857.

Hans-Helge Muller and Helmut Schafer. Adaptive group sequential designs for clinical trials: Combining the advantages of adaptive and of classical group sequential approaches. Biometrics 2001;57:886-891.

See Also

getDesign

Examples

```
# original group sequential design with 90% power to detect delta = 6
delta = 6
sigma = 17
n = 282
(des1 = getDesign(IMax = n/(4*sigma^2), theta = delta, kMax = 3,
                  alpha = 0.05, typeAlphaSpending = "sfHSD",
                  parameterAlphaSpending = -4))

# interim look results
L = 1
n1 = n/3
delta1 = 4.5
sigma1 = 20
```

```
zL = delta1/sqrt(4/n1*sigma1^2)

t = des1$byStageResults$informationRates

# conditional power with sample size increase
(des2 = adaptDesign(
  betaNew = NA, INew = 420/(4*sigma1^2),
  L, zL, theta = delta1,
  IMax = n/(4*sigma1^2), kMax = 3, informationRates = t,
  alpha = 0.05, typeAlphaSpending = "sfHSD",
  parameterAlphaSpending = -4))

# Muller & Schafer (2001) method to design the secondary trial:
# 3-look gamma(-2) spending with 84% power at delta = 4.5 and sigma = 20
(des2 = adaptDesign(
  betaNew = 0.16, INew = NA,
  L, zL, theta = delta1,
  IMax = n/(4*sigma1^2), kMax = 3, informationRates = t,
  alpha = 0.05, typeAlphaSpending = "sfHSD",
  parameterAlphaSpending = -4,
  MullerSchafer = TRUE,
  kNew = 3, typeAlphaSpendingNew = "sfHSD",
  parameterAlphaSpendingNew = -2))

# incremental sample size for sigma = 20
(nNew = 4*sigma1^2*des2$secondaryTrial$overallResults$information)
```

---

aml   *Acute myelogenous leukemia survival data from the survival package*

Description

Survival in patients with acute myelogenous leukemia.

time Survival or censoring time

status censoring status

x maintenance chemotherapy given or not

Usage

```
aml
```

Format

An object of class data.frame with 23 rows and 3 columns.

binary_tte_sim   *Simulation for a Binary Endpoint and a Time-to-Event Endpoint*

Description

Performs simulation for two-endpoint two-arm group sequential trials. The first endpoint is a binary endpoint and the Mantel-Haenszel test is used to test risk difference. The second endpoint is a time-to-event endpoint and the log-rank test is used to test the treatment difference. The analysis times of the first endpoint are determined by the specified calendar times, while the analysis times for the second endpoint is based on the planned number of events at each look. The binary endpoint is assessed at the first post-treatment follow-up visit.

Usage

```
binary_tte_sim(
  kMax1 = 1L,
  kMax2 = 1L,
  riskDiffH0 = 0,
  hazardRatioH0 = 1,
  allocation1 = 1L,
  allocation2 = 1L,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  globalOddsRatio = 1,
  pi1 = NA_real_,
  pi2 = NA_real_,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  delta1 = 0L,
  delta2 = 0L,
  upper1 = NA_real_,
  upper2 = NA_real_,
  accrualDuration = NA_real_,
  plannedTime = NA_real_,
  plannedEvents = NA_integer_,
  maxNumberOfIterations = 1000L,
  maxNumberOfRawDatasetsPerStage = 0L,
  seed = NA_integer_
)
```

Arguments

kMax1   Number of stages for the binary endpoint.

kMax2	Number of stages for the time-to-event endpoint.
riskDiffH0	Risk difference under the null hypothesis for the binary endpoint.
hazardRatioH0	Hazard ratio under the null hypothesis for the time-to-event endpoint.
allocation1	Number of subjects in the treatment group in a randomization block. Defaults to 1 for equal randomization.
allocation2	Number of subjects in the control group in a randomization block. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

        A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

        A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

        A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

globalOddsRatio

        The global odds ratio of the Plackett copula.

pi1	Response probabilities by stratum for the treatment group for the binary endpoint.
pi2	Response probabilities by stratum for the control group for the binary endpoint.
lambda1	A vector of hazard rates for the event in each analysis time interval by stratum for the treatment group for the time-to-event endpoint.
lambda2	A vector of hazard rates for the event in each analysis time interval by stratum for the control group for the time-to-event endpoint.
gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the treatment group.
gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.
delta1	The hazard rate for exponential treatment discontinuation, a vector of hazard rates for piecewise exponential treatment discontinuation applicable for all strata, or a vector of hazard rates for treatment discontinuation in each analysis time interval by stratum for the treatment group for the binary endpoint.
delta2	The hazard rate for exponential treatment discontinuation, a vector of hazard rates for piecewise exponential treatment discontinuation applicable for all strata, or a vector of hazard rates for treatment discontinuation in each analysis time interval by stratum for the control group for the binary endpoint.
upper1	The protocol-specified treatment duration for the treatment group.
upper2	The protocol-specified treatment duration for the control group.

accrualDuration
              Duration of the enrollment period.

plannedTime   The calendar times for the analyses of the binary endpoint.

plannedEvents The planned cumulative total number of events for the time-to-event endpoint.

maxNumberOfIterations
              The number of simulation iterations.

maxNumberOfRawDatasetsPerStage
              The number of raw datasets per stage to extract.

seed   The seed to reproduce the simulation results. The seed from the environment
              will be used if left unspecified.

Details

We consider dual primary endpoints with endpoint 1 being a binary endpoint and endpoint 2 being a time-to-event endpoint. The analyses of endpoint 1 will be based on calendar times, while the analyses of endpoint 2 will be based on the number of events. Therefore, the analyses of the two endpoints are not at the same time points. The correlation between the two endpoints is characterized by the global odds ratio of the Plackett copula. In addition, the time-to-event endpoint will render the binary endpoint as a non-responder, and so does the dropout. In addition, the treatment discontinuation will impact the number of available subjects for analysis. The administrative censoring will exclude subjects from the analysis of the binary endpoint.

Value

A list with 4 components:

- sumdataBIN: A data frame of summary data by iteration and stage for the binary endpoint:
    - iterationNumber: The iteration number.
    - stageNumber: The stage number, covering all stages even if the trial stops at an interim look.
    - analysisTime: The time for the stage since trial start.
    - accruals1: The number of subjects enrolled at the stage for the treatment group.
    - accruals2: The number of subjects enrolled at the stage for the control group.
    - totalAccruals: The total number of subjects enrolled at the stage.
    - source1: The total number of subjects with response status determined by the underlying latent response variable.
    - source2: The total number of subjects with response status (non-responder) determined by experiencing the event for the time-to-event endpoint.
    - source3: The total number of subjects with response status (non-responder) determined by dropping out prior to the PTFU1 visit.
    - n1: The number of subjects included in the analysis of the binary endpoint for the treatment group.
    - n2: The number of subjects included in the analysis of the binary endpoint for the control group.
    - n: The total number of subjects included in the analysis of the binary endpoint at the stage.

- y1: The number of responders for the binary endpoint in the treatment group.
- y2: The number of responders for the binary endpoint in the control group.
- y: The total number of responders for the binary endpoint at the stage.
- riskDiff: The estimated risk difference for the binary endpoint.
- seRiskDiff: The standard error for risk difference based on the Sato approximation.
- mnStatistic: The Mantel-Haenszel test Z-statistic for the binary endpoint.

- sumdataTTE: A data frame of summary data by iteration and stage for the time-to-event endpoint:

  - iterationNumber: The iteration number.
  - eventsNotAchieved: Whether the target number of events is not achieved for the iteration.
  - stageNumber: The stage number, covering all stages even if the trial stops at an interim look.
  - analysisTime: The time for the stage since trial start.
  - accruals1: The number of subjects enrolled at the stage for the treatment group.
  - accruals2: The number of subjects enrolled at the stage for the control group.
  - totalAccruals: The total number of subjects enrolled at the stage.
  - events1: The number of events at the stage for the treatment group.
  - events2: The number of events at the stage for the control group.
  - totalEvents: The total number of events at the stage.
  - dropouts1: The number of dropouts at the stage for the treatment group.
  - dropouts2: The number of dropouts at the stage for the control group.
  - totalDropouts: The total number of dropouts at the stage.
  - logRankStatistic: The log-rank test Z-statistic for the time-to-event endpoint.

- rawdataBIN (exists if maxNumberOfRawDatasetsPerStage is a positive integer): A data frame for subject-level data for the binary endpoint for selected replications, containing the following variables:

  - iterationNumber: The iteration number.
  - stageNumber: The stage under consideration.
  - analysisTime: The time for the stage since trial start.
  - subjectId: The subject ID.
  - arrivalTime: The enrollment time for the subject.
  - stratum: The stratum for the subject.
  - treatmentGroup: The treatment group (1 or 2) for the subject.
  - survivalTime: The underlying survival time for the time-to-event endpoint for the subject.
  - dropoutTime: The underlying dropout time for the time-to-event endpoint for the subject.
  - ptfu1Time: The underlying assessment time for the binary endpoint for the subject.
  - timeUnderObservation: The time under observation since randomization for the binary endpoint for the subject.
  - responder: Whether the subject is a responder for the binary endpoint.

      – source: The source of the determination of responder status for the binary endpoint:
= 1 based on the underlying latent response variable, = 2 based on the occurrence of
the time-to-event endpoint before the assessment time of the binary endpoint (imputed
as a non-responder), = 3 based on the dropout before the assessment time of the binary
endpoint (imputed as a non-responder), = 4 excluded from analysis due to administrative
censoring.

- rawdataTTE (exists if maxNumberOfRawDatasetsPerStage is a positive integer): A data
frame for subject-level data for the time-to-event endpoint for selected replications, containing
the following variables:

      – iterationNumber: The iteration number.

      – stageNumber: The stage under consideration.

      – analysisTime: The time for the stage since trial start.

      – subjectId: The subject ID.

      – arrivalTime: The enrollment time for the subject.

      – stratum: The stratum for the subject.

      – treatmentGroup: The treatment group (1 or 2) for the subject.

      – survivalTime: The underlying survival time for the time-to-event endpoint for the sub-
ject.

      – dropoutTime: The underlying dropout time for the time-to-event endpoint for the subject.

      – timeUnderObservation: The time under observation since randomization for the time-
to-event endpoint for the subject.

      – event: Whether the subject experienced the event for the time-to-event endpoint.

      – dropoutEvent: Whether the subject dropped out for the time-to-event endpoint.

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Examples

```
tcut = c(0, 12, 36, 48)
surv = c(1, 0.95, 0.82, 0.74)
lambda2 = (log(surv[1:3]) - log(surv[2:4]))/(tcut[2:4] - tcut[1:3])

sim1 = binary_tte_sim(
  kMax1 = 1,
  kMax2 = 2,
  accrualTime = 0:8,
  accrualIntensity = c(((1:8) - 0.5)/8, 1)*40,
  piecewiseSurvivalTime = c(0,12,36),
  globalOddsRatio = 1,
  pi1 = 0.80,
  pi2 = 0.65,
  lambda1 = 0.65*lambda2,
  lambda2 = lambda2,
  gamma1 = -log(1-0.04)/12,
  gamma2 = -log(1-0.04)/12,
  delta1 = -log(1-0.02)/12,
```

```
delta2 = -log(1-0.02)/12,
upper1 = 15*28/30.4,
upper2 = 12*28/30.4,
accrualDuration = 20,
plannedTime = 20 + 15*28/30.4,
plannedEvents = c(130, 173),
maxNumberOfIterations = 1000,
maxNumberOfRawDatasetsPerStage = 1,
seed = 314159)
```

BOINTable   *BOIN Decision Table*

Description

Obtains the decision table for the Bayesian optimal interval (BOIN) design.

Usage

```
BOINTable(
  nMax = NA_integer_,
  pT = 0.3,
  phi1 = 0.6 * pT,
  phi2 = 1.4 * pT,
  a = 1,
  b = 1,
  pExcessTox = 0.95
)
```

Arguments

nMax	The maximum number of subjects in a dose cohort.
pT	The target toxicity probability. Defaults to 0.3.
phi1	The lower equivalence limit for target toxicity probability.
phi2	The upper equivalence limit for target toxicity probability.
a	The prior toxicity parameter for the beta prior.
b	The prior non-toxicity parameter for the beta prior.
pExcessTox	The threshold for excessive toxicity, i.e., if $\text{Prob}(p > pT \mid \text{Data}) > pExcessTox$, then the current and all higher doses will be excluded and never be used again in the remainder of the trial to avoid any other subjects receiving treatment at those doses. Defaults to 0.95.

Value

An S3 class `BOINTable` object with the following components:

- `settings`: The input settings data frame with the following variables:
    - `nMax`: The maximum number of subjects in a dose cohort.
    - `pT`: The target toxicity probability.
    - `phi1`: The lower equivalence limit for target toxicity probability.
    - `phi2`: The upper equivalence limit for target toxicity probability.
    - `lambda1`: The lower decision boundary for observed toxicity probability.
    - `lambda2`: The upper decision boundary for observed toxicity probability.
    - `a`: The prior toxicity parameter for the beta prior.
    - `b`: The prior non-toxicity parameter for the beta prior.
    - `pExcessTox`: The threshold for excessive toxicity.
- `decisionDataFrame`: The decision data frame for the BOIN design. It includes the following variables:
    - `n`: The sample size.
    - `y`: The number of toxicities.
    - `decision`: The dosing decision.
- `decisionMatrix`: The decision matrix corresponding to the decision data frame.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
BOINTable(nMax = 18, pT = 0.3, phi = 0.6*0.3, phi2 = 1.4*0.3)
```

---

caltime   *Calendar Times for Target Number of Events*

Description

Obtains the calendar times needed to reach the target number of subjects experiencing an event.

Usage

```
caltime(
  nevents = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
```

```
    lambda1 = NA_real_,
    lambda2 = NA_real_,
    gamma1 = 0L,
    gamma2 = 0L,
    accrualDuration = NA_real_,
    followupTime = NA_real_,
    fixedFollowup = 0L
)
```

Arguments

nevents   A vector of target number of events.

allocationRatioPlanned

        Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

        A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

        A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

        A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1   A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.

lambda2   A vector of hazard rates for the event in each analysis time interval by stratum for the control group.

gamma1   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.

gamma2   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration

        Duration of the enrollment period.

followupTime   Follow-up time for the last enrolled subject.

fixedFollowup   Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

Value

A vector of calendar times expected to yield the target number of events.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Piecewise accrual, piecewise exponential survivals, and 5% dropout by
# the end of 1 year.

caltime(nevents = c(24, 80), allocationRatioPlanned = 1,
        accrualTime = seq(0, 8),
        accrualIntensity = 26/9*seq(1, 9),
        piecewiseSurvivalTime = c(0, 6),
        lambda1 = c(0.0533, 0.0309),
        lambda2 = c(0.0533, 0.0533),
        gamma1 = -log(1-0.05)/12,
        gamma2 = -log(1-0.05)/12,
        accrualDuration = 22,
        followupTime = 18, fixedFollowup = FALSE)
```

ClopperPearsonCI   *Clopper-Pearson Confidence Interval for One-Sample Proportion*

Description

Obtains the Clopper-Pearson exact confidence interval for a one-sample proportion.

Usage

```
ClopperPearsonCI(n, y, cilevel = 0.95)
```

Arguments

n	The sample size.
y	The number of responses.
cilevel	The confidence interval level.

Value

A data frame with the following variables:

- n: The sample size.
- y: The number of responses.
- phat: The observed proportion of responses.
- lower: The lower limit of the confidence interval.
- upper: The upper limit of the confidence interval.
- cilevel: The confidence interval level.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
ClopperPearsonCI(20, 3)
```

---

covrmst   *Covariance Between Restricted Mean Survival Times*

Description

Obtains the covariance between restricted mean survival times at two different time points.

Usage

```
covrmst(
  t2 = NA_real_,
  tau1 = NA_real_,
  tau2 = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  maxFollowupTime = NA_real_
)
```

Arguments

t2	The calendar time for analysis 2.
tau1	The milestone time for analysis 1.
tau2	The milestone time for analysis 2.
allocationRatioPlanned	
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).
accrualIntensity	
	A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

lambda1   A vector of hazard rates for the event for the active treatment group. One for each analysis time interval.

lambda2   A vector of hazard rates for the event for the control group. One for each analysis time interval.

gamma1   The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the active treatment group.

gamma2   The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the control group.

accrualDuration

Duration of the enrollment period.

maxFollowupTime

Follow-up time for the first enrolled subject. For fixed follow-up, `maxFollowupTime = minFollowupTime`. For variable follow-up, `maxFollowupTime = accrualDuration + minFollowupTime`.

Value

The covariance between the restricted mean survival times for each treatment group.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
covrmst(t2 = 25, tau1 = 16, tau2 = 18, allocationRatioPlanned = 1,
        accrualTime = c(0, 3), accrualIntensity = c(10, 20),
        piecewiseSurvivalTime = c(0, 6),
        lambda1 = c(0.0533, 0.0309), lambda2 = c(0.0533, 0.0533),
        gamma1 = -log(1-0.05)/12, gamma2 = -log(1-0.05)/12,
        accrualDuration = 12, maxFollowupTime = 30)
```

---

errorSpent   *Error Spending*

Description

Obtains the error spent at given spending times for the specified error spending function.

Usage

```
errorSpent(t, error, sf = "sfOF", sfpar = NA)
```

Arguments

t	A vector of spending times, typically equal to information fractions.
error	The total error to spend.
sf	The spending function. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, and "sfHSD" for Hwang, Shi & DeCani spending function. Defaults to "sfOF".
sfpar	The parameter for the spending function. Corresponds to rho for "sfKD" and gamma for "sfHSD".

Value

A vector of errors spent up to the interim look.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
errorSpent(t = 0.5, error = 0.025, sf = "sfOF")

errorSpent(t = c(0.5, 0.75, 1), error = 0.025, sf = "sfHSD", sfpar = -4)
```

---

exitprob	*Stagewise Exit Probabilities*

Description

Obtains the stagewise exit probabilities for both efficacy and futility stopping.

Usage

```
exitprob(b, a = NA, theta = 0, I = NA)
```

Arguments

b	Upper boundaries on the z-test statistic scale.
a	Lower boundaries on the z-test statistic scale. Defaults to c(rep(-6.0, kMax-1), b[kMax]) if left unspecified, where kMax = length(b).
theta	Stagewise parameter of interest, e.g., -U/V for weighted log-rank test, where U is the mean and V is the variance of the weighted log-rank test score statistic at each stage. For proportional hazards and conventional log-rank test, use the scalar input, theta = -log(HR). Defaults to 0 corresponding to the null hypothesis.

| I | Stagewise cumulative information, e.g., `V`, the variance of the weighted log-rank test score statistic at each stage. For conventional log-rank test, information can be approximated by `phi*(1-phi)*D`, where `phi` is the probability of being allocated to the active arm, and `D` is the total number of events at each stage. Defaults to `seq(1, kMax)` if left unspecified. |

Value

A list of stagewise exit probabilities:

- `exitProbUpper`: The vector of efficacy stopping probabilities
- `exitProbLower`: The vector of futility stopping probabilities.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
exitprob(b = c(3.471, 2.454, 2.004), theta = -log(0.6),
         I = c(50, 100, 150)/4)

exitprob(b = c(2.963, 2.359, 2.014),
         a = c(-0.264, 0.599, 2.014),
         theta = c(0.141, 0.204, 0.289),
         I = c(81, 121, 160))
```

| fadjpbon | *Adjusted p-Values for Bonferroni-Based Graphical Approaches* |

Description

Obtains the adjusted p-values for graphical approaches using weighted Bonferroni tests.

Usage

```
fadjpbon(w, G, p)
```

Arguments

w	The vector of initial weights for elementary hypotheses.
G	The initial transition matrix.
p	The raw p-values for elementary hypotheses.

Value

A matrix of adjusted p-values.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Frank Bretz, Willi Maurer, Werner Brannath and Martin Posch. A graphical approach to sequentially rejective multiple test procedures. Statistics in Medicine. 2009; 28:586-604.

Examples

```
pvalues <- matrix(c(0.01,0.005,0.015,0.022, 0.02,0.015,0.010,0.023),
                  nrow=2, ncol=4, byrow=TRUE)
w <- c(0.5,0.5,0,0)
g <- matrix(c(0,0,1,0,0,0,0,1,0,1,0,0,1,0,0,0),
            nrow=4, ncol=4, byrow=TRUE)
fadjpbon(w, g, pvalues)
```

---

fadjpdun	*Adjusted p-Values for Dunnett-Based Graphical Approaches*

Description

Obtains the adjusted p-values for graphical approaches using weighted Dunnett tests.

Usage

```
fadjpdun(wgtmat, p, family = NULL, corr = NULL)
```

Arguments

wgtmat	The weight matrix for intersection hypotheses.
p	The raw p-values for elementary hypotheses.
family	The matrix of family indicators for elementary hypotheses.
corr	The correlation matrix that should be used for the parametric test. Can contain NAs for unknown correlations between families.

Value

A matrix of adjusted p-values.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Frank Bretz, Martin Posch, Ekkehard Glimm, Florian Klinglmueller, Willi Maurer, and Kornelius Rohmeyer. Graphical approach for multiple comparison procedures using weighted Bonferroni, Simes, or parameter tests. Biometrical Journal. 2011; 53:894-913.

Examples

```
pvalues <- matrix(c(0.01,0.005,0.015,0.022, 0.02,0.015,0.010,0.023),
                  nrow=2, ncol=4, byrow=TRUE)
w <- c(0.5,0.5,0,0)
g <- matrix(c(0,0,1,0,0,0,0,1,0,1,0,0,1,0,0,0),
            nrow=4, ncol=4, byrow=TRUE)
wgtmat = fwgtmat(w,g)

family = matrix(c(1,1,0,0,0,0,1,1), nrow=2, ncol=4, byrow=TRUE)
corr = matrix(c(1,0.5,NA,NA, 0.5,1,NA,NA,
                NA,NA,1,0.5, NA,NA,0.5,1),
              nrow = 4, byrow = TRUE)
fadjpdun(wgtmat, pvalues, family, corr)
```

---

fadjpsim   *Adjusted p-Values for Simes-Based Graphical Approaches*

Description

Obtains the adjusted p-values for graphical approaches using weighted Simes tests.

Usage

```
fadjpsim(wgtmat, p, family = NULL)
```

Arguments

wgtmat	The weight matrix for intersection hypotheses.
p	The raw p-values for elementary hypotheses.
family	The matrix of family indicators for elementary hypotheses.

Value

A matrix of adjusted p-values.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Frank Bretz, Martin Posch, Ekkehard Glimm, Florian Klinglmueller, Willi Maurer, and Kornelius Rohmeyer. Graphical approach for multiple comparison procedures using weighted Bonferroni, Simes, or parameter tests. Biometrical Journal. 2011; 53:894-913.

Kaifeng Lu. Graphical approaches using a Bonferroni mixture of weighted Simes tests. Statistics in Medicine. 2016; 35:4041-4055.

Examples

```
pvalues <- matrix(c(0.01,0.005,0.015,0.022, 0.02,0.015,0.010,0.023),
                  nrow=2, ncol=4, byrow=TRUE)
w <- c(0.5,0.5,0,0)
g <- matrix(c(0,0,1,0,0,0,0,1,0,1,0,0,1,0,0,0),
            nrow=4, ncol=4, byrow=TRUE)
wgtmat = fwgtmat(w,g)

family = matrix(c(1,1,0,0,0,0,1,1), nrow=2, ncol=4, byrow=TRUE)
fadjpsim(wgtmat, pvalues, family)
```

---

float_to_fraction	*Converting a decimal to a fraction*

Description

Converts a decimal to a fraction based on the algorithm from http://stackoverflow.com/a/5128558/221955.

Usage

```
float_to_fraction(x, tol = 1e-06)
```

Arguments

x	The fraction in decimal form.
tol	The tolerance level for the conversion error.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
float_to_fraction(5/3)
```

---

fmodmix   *Adjusted p-Values for Modified Mixture Gatekeeping Procedures*

Description

Obtains the adjusted p-values for the modified gatekeeping procedures for multiplicity problems involving serial and parallel logical restrictions.

Usage

```
fmodmix(
  p,
  family = NULL,
  serial,
  parallel,
  gamma,
  test = "hommel",
  exhaust = TRUE
)
```

Arguments

p	The raw p-values for elementary hypotheses.
family	The matrix of family indicators for the hypotheses.
serial	The matrix of serial rejection set for the hypotheses.
parallel	The matrix of parallel rejection set for the hypotheses.
gamma	The truncation parameters for each family. The truncation parameter for the last family is automatically set to 1.
test	The component multiple testing procedure. Options include "holm", "hochberg", or "hommel". Defaults to "hommel".
exhaust	Whether to use alpha-exhausting component testing procedure for the last family with active hypotheses. It defaults to TRUE.

Value

A matrix of adjusted p-values.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Alex Dmitrienko, George Kordzakhia, and Thomas Brechenmacher. Mixture-based gatekeeping procedures for multiplicity problems with multiple sequences of hypotheses. Journal of Biopharmaceutical Statistics. 2016; 26(4):758–780.

George Kordzakhia, Thomas Brechenmacher, Eiji Ishida, Alex Dmitrienko, Winston Wenxiang Zheng, and David Fuyuan Li. An enhanced mixture method for constructing gatekeeping procedures in clinical trials. Journal of Biopharmaceutical Statistics. 2018; 28(1):113–128.

Examples

```
p = c(0.0194, 0.0068, 0.0271, 0.0088, 0.0370, 0.0018, 0.0814, 0.0066)
family = matrix(c(1, 1, 0, 0, 0, 0, 0, 0,
                  0, 0, 1, 1, 0, 0, 0, 0,
                  0, 0, 0, 0, 1, 1, 0, 0,
                  0, 0, 0, 0, 0, 0, 1, 1),
                nrow=4, byrow=TRUE)

serial = matrix(c(0, 0, 0, 0, 0, 0, 0, 0,
                  0, 0, 0, 0, 0, 0, 0, 0,
                  1, 0, 0, 0, 0, 0, 0, 0,
                  0, 1, 0, 0, 0, 0, 0, 0,
                  0, 0, 1, 0, 0, 0, 0, 0,
                  0, 0, 0, 1, 0, 0, 0, 0,
                  0, 0, 0, 0, 1, 0, 0, 0,
                  0, 0, 0, 0, 0, 1, 0, 0),
                nrow=8, byrow=TRUE)

parallel = matrix(0, 8, 8)
gamma = c(0.6, 0.6, 0.6, 1)
fmodmix(p, family, serial, parallel, gamma, test = "hommel", exhaust = TRUE)
```

---

fquantile	*The Quantiles of a Survival Distribution*

Description

Obtains the quantiles of a survival distribution.

Usage

```
fquantile(S, probs, ...)
```

Arguments

S	The survival function of a univariate survival time.
probs	The numeric vector of probabilities.
...	Additional arguments to be passed to S.

Value

A vector of length(probs) for the quantiles.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
fquantile(pweibull, probs = c(0.25, 0.5, 0.75),
          shape = 1.37, scale = 1/0.818, lower.tail = FALSE)
```

---

fseqbon   *Group Sequential Trials Using Bonferroni-Based Graphical Ap-*
                           proaches

Description

Obtains the test results for group sequential trials using graphical approaches based on weighted
Bonferroni tests.

Usage

```
fseqbon(
  w,
  G,
  alpha = 0.025,
  kMax,
  typeAlphaSpending = NULL,
  parameterAlphaSpending = NULL,
  incidenceMatrix = NULL,
  maxInformation = NULL,
  p,
  information,
  spendingTime = NULL
)
```

Arguments

w	The vector of initial weights for elementary hypotheses.
G	The initial transition matrix.
alpha	The significance level. Defaults to 0.025.
kMax	The maximum number of stages.

typeAlphaSpending

> The vector of alpha spending functions. Each element is one of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF" if not provided.

parameterAlphaSpending

> The vector of parameter values for the alpha spending functions. Each element corresponds to the value of Delta for "WT", rho for "sfKD", or gamma for "sfHSD". Defaults to missing if not provided.

incidenceMatrix

> The incidence matrix indicating whether the specific hypothesis will be tested at the given look. The number of columns of incidenceMatrix must be equal to the maximum number of study looks (kMax). If not provided, defaults to testing each hypothesis at all study looks.

maxInformation The vector of target maximum information for each hypothesis. Defaults to a vector of 1s if not provided.

p   The matrix of raw p-values for each hypothesis by study look.

information   The matrix of observed information for each hypothesis by study look.

spendingTime   The spending time for alpha spending by study look. If not provided, it is the same as informationRates calculated from information and maxInformation.

Value

A vector to indicate the first look the specific hypothesis is rejected (0 if the hypothesis is not rejected).

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Willi Maurer and Frank Bretz. Multiple testing in group sequential trials using graphical approaches. Statistics in Biopharmaceutical Research. 2013; 5:311-320.

Examples

```
# Case study from Maurer & Bretz (2013)

fseqbon(
  w = c(0.5, 0.5, 0, 0),
  G = matrix(c(0, 0.5, 0.5, 0,  0.5, 0, 0, 0.5,
               0, 1, 0, 0,  1, 0, 0, 0),
             nrow=4, ncol=4, byrow=TRUE),
  alpha = 0.025,
  kMax = 3,
  typeAlphaSpending = rep("sfOF", 4),
```

```
    maxInformation = rep(1, 4),
    p = matrix(c(0.0062, 0.017, 0.009, 0.13,
                 0.0002, 0.0035, 0.002, 0.06),
               nrow=4, ncol=2),
    information = matrix(c(rep(1/3, 4), rep(2/3, 4)),
                         nrow=4, ncol=2))
```

---

fstdmix   *Adjusted p-Values for Standard Mixture Gatekeeping Procedures*

Description

Obtains the adjusted p-values for the standard gatekeeping procedures for multiplicity problems involving serial and parallel logical restrictions.

Usage

```
fstdmix(
  p,
  family = NULL,
  serial,
  parallel,
  gamma,
  test = "hommel",
  exhaust = TRUE
)
```

Arguments

p	The raw p-values for elementary hypotheses.
family	The matrix of family indicators for the hypotheses.
serial	The matrix of serial rejection set for the hypotheses.
parallel	The matrix of parallel rejection set for the hypotheses.
gamma	The truncation parameters for each family. The truncation parameter for the last family is automatically set to 1.
test	The component multiple testing procedure. Options include "holm", "hochberg", or "hommel". Defaults to "hommel".
exhaust	Whether to use alpha-exhausting component testing procedure for the last family with active hypotheses. It defaults to TRUE.

Value

A matrix of adjusted p-values.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Alex Dmitrienko and Ajit C Tamhane. Mixtures of multiple testing procedures for gatekeeping applications in clinical trials. Statistics in Medicine. 2011; 30(13):1473–1488.

Examples

```
p = c(0.0194, 0.0068, 0.0271, 0.0088, 0.0370, 0.0018, 0.0814, 0.0066)
family = matrix(c(1, 1, 0, 0, 0, 0, 0, 0,
                  0, 0, 1, 1, 0, 0, 0, 0,
                  0, 0, 0, 0, 1, 1, 0, 0,
                  0, 0, 0, 0, 0, 0, 1, 1),
                nrow=4, byrow=TRUE)

serial = matrix(c(0, 0, 0, 0, 0, 0, 0, 0,
                  0, 0, 0, 0, 0, 0, 0, 0,
                  1, 0, 0, 0, 0, 0, 0, 0,
                  0, 1, 0, 0, 0, 0, 0, 0,
                  0, 0, 1, 0, 0, 0, 0, 0,
                  0, 0, 0, 1, 0, 0, 0, 0,
                  0, 0, 0, 0, 1, 0, 0, 0,
                  0, 0, 0, 0, 0, 1, 0, 0),
                nrow=8, byrow=TRUE)

parallel = matrix(0, 8, 8)
gamma = c(0.6, 0.6, 0.6, 1)
fstdmix(p, family, serial, parallel, gamma, test = "hommel",
        exhaust = FALSE)
```

---

fstp2seq   *Adjusted p-Values for Stepwise Testing Procedures for Two Sequences*

Description

Obtains the adjusted p-values for the stepwise gatekeeping procedures for multiplicity problems involving two sequences of hypotheses.

Usage

```
fstp2seq(p, gamma, test = "hochberg", retest = TRUE)
```

Arguments

p	The raw p-values for elementary hypotheses.
gamma	The truncation parameters for each family. The truncation parameter for the last family is automatically set to 1.
test	The component multiple testing procedure. It is either "Holm" or "Hochberg", and it defaults to "Hochberg".
retest	Whether to allow retesting. It defaults to TRUE.

Value

A matrix of adjusted p-values.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
p = c(0.0194, 0.0068, 0.0271, 0.0088, 0.0370, 0.0018, 0.0814, 0.0066)
gamma = c(0.6, 0.6, 0.6, 1)
fstp2seq(p, gamma, test="hochberg", retest=1)
```

---

ftrunc	*Adjusted p-Values for Holm, Hochberg, and Hommel Procedures*

Description

Obtains the adjusted p-values for possibly truncated Holm, Hochberg, and Hommel procedures.

Usage

```
ftrunc(p, test = "hommel", gamma = 1)
```

Arguments

p	The raw p-values for elementary hypotheses.
test	The test to use, e.g., "holm", "hochberg", or "hommel" (default).
gamma	The value of the truncation parameter. Defaults to 1 for the regular Holm, Hochberg, or Hommel procedure.

Value

A matrix of adjusted p-values.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Alex Dmitrienko, Ajit C. Tamhane, and Brian L. Wiens. General multistage gatekeeping procedures. Biometrical Journal. 2008; 5:667-677.

Examples

```
pvalues <- matrix(c(0.01,0.005,0.015,0.022, 0.02,0.015,0.010,0.023),
                  nrow=2, ncol=4, byrow=TRUE)
ftrunc(pvalues, "hochberg")
```

---

fwgtmat	*Weight Matrix for All Intersection Hypotheses*

Description

Obtains the weight matrix for all intersection hypotheses.

Usage

```
fwgtmat(w, G)
```

Arguments

w	The vector of weights for elementary hypotheses.
G	The transition matrix.

Value

The weight matrix starting with the global null hypothesis.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
w = c(0.5,0.5,0,0)
g = matrix(c(0,0,1,0, 0,0,0,1, 0,1,0,0, 1,0,0,0),
           nrow=4, ncol=4, byrow=TRUE)
(wgtmat = fwgtmat(w,g))
```

---

getAccrualDurationFromN

Accrual Duration to Enroll Target Number of Subjects

Description

Obtains the accrual duration to enroll the target number of subjects.

Usage

```
getAccrualDurationFromN(
  nsubjects = NA_real_,
  accrualTime = 0L,
  accrualIntensity = NA_real_
)
```

Arguments

nsubjects   The vector of target number of subjects.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time
                 intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual
                 intervals: [0, 3) and [3, Inf).

accrualIntensity
                 A vector of accrual intensities. One for each accrual time interval.

Value

A vector of accrual durations.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
getAccrualDurationFromN(nsubjects = c(20, 150), accrualTime = c(0, 3),
                        accrualIntensity = c(10, 20))
```

---

getADCI   *Confidence Interval After Adaptation*

Description

Obtains the p-value, median unbiased point estimate, and confidence interval after the end of an adaptive trial.

Usage

```
getADCI(
  L = NA_integer_,
  zL = NA_real_,
  IMax = NA_real_,
  kMax = NA_integer_,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.25,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  spendingTime = NA_real_,
  L2 = NA_integer_,
  zL2 = NA_real_,
  INew = NA_real_,
  MullerSchafer = 0L,
  informationRatesNew = NA_real_,
  efficacyStoppingNew = NA_integer_,
  typeAlphaSpendingNew = "sfOF",
  parameterAlphaSpendingNew = NA_real_,
  spendingTimeNew = NA_real_
)
```

Arguments

L	The interim adaptation look of the primary trial.
zL	The z-test statistic at the interim adaptation look of the primary trial.
IMax	The maximum information of the primary trial.
kMax	The maximum number of stages of the primary trial.
informationRates	
	The information rates of the primary trial.
efficacyStopping	
	Indicators of whether efficacy stopping is allowed at each stage of the primary trial. Defaults to true if left unspecified.
criticalValues	The upper boundaries on the z-test statistic scale for efficacy stopping for the primary trial.

alpha   The significance level of the primary trial. Defaults to 0.025.

typeAlphaSpending
                         The type of alpha spending for the primary trial. One of the following: "OF"
                         for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang &
                         Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP"
                         for Pocock type spending function, "sfKD" for Kim & DeMets spending func-
                         tion, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no
                         early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending
                         The parameter value of alpha spending for the primary trial. Corresponds to
                         Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

spendingTime   The error spending time of the primary trial. Defaults to missing, in which case,
                         it is the same as informationRates.

L2   The termination look of the secondary trial.

zL2   The z-test statistic at the termination look of the secondary trial.

INew   The maximum information of the secondary trial.

MullerSchafer   Whether to use the Muller and Schafer (2001) method for trial adaptation.

informationRatesNew
                         The spacing of looks of the secondary trial up to look L2.

efficacyStoppingNew
                         The indicators of whether efficacy stopping is allowed at each look of the sec-
                         ondary trial up to look L2. Defaults to true if left unspecified.

typeAlphaSpendingNew
                         The type of alpha spending for the secondary trial. One of the following: "OF"
                         for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang &
                         Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP"
                         for Pocock type spending function, "sfKD" for Kim & DeMets spending func-
                         tion, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no
                         early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpendingNew
                         The parameter value of alpha spending for the secondary trial. Corresponds to
                         Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

spendingTimeNew
                         The error spending time of the secondary trial up to look L2. Defaults to missing,
                         in which case, it is the same as informationRatesNew.

Value

A data frame with the following variables:

- pvalue: p-value for rejecting the null hypothesis.

- thetahat: Median unbiased point estimate of the parameter.

- cilevel: Confidence interval level.

- lower: Lower bound of confidence interval.

- upper: Upper bound of confidence interval.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Ping Gao, Lingyun Liu and Cyrus Mehta. Exact inference for adaptive group sequential designs. Stat Med. 2013;32(23):3991-4005.

See Also

adaptDesign

Examples

```
# original group sequential design with 90% power to detect delta = 6
delta = 6
sigma = 17
n = 282
(des1 = getDesign(IMax = n/(4*sigma^2), theta = delta, kMax = 3,
                  alpha = 0.05, typeAlphaSpending = "sfHSD",
                  parameterAlphaSpending = -4))

# interim look results
L = 1
n1 = n/3
delta1 = 4.5
sigma1 = 20
zL = delta1/sqrt(4/n1*sigma1^2)

t = des1$byStageResults$informationRates

# Muller & Schafer (2001) method to design the secondary trial:
des2 = adaptDesign(
  betaNew = 0.2, L = L, zL = zL, theta = 5,
  kMax = 3, informationRates = t,
  alpha = 0.05, typeAlphaSpending = "sfHSD",
  parameterAlphaSpending = -4,
  MullerSchafer = TRUE,
  kNew = 3, typeAlphaSpendingNew = "sfHSD",
  parameterAlphaSpendingNew = -2)

n2 = ceiling(des2$secondaryTrial$overallResults$information*4*20^2)
ns = round(n2*(1:3)/3)
 (des2 = adaptDesign(
   INew = n2/(4*20^2), L = L, zL = zL, theta = 5,
   kMax = 3, informationRates = t,
   alpha = 0.05, typeAlphaSpending = "sfHSD",
   parameterAlphaSpending = -4,
   MullerSchafer = TRUE,
   kNew = 3, informationRatesNew = ns/n2,
   typeAlphaSpendingNew = "sfHSD",
   parameterAlphaSpendingNew = -2))
```

```
# termination at the second look of the secondary trial
L2 = 2
delta2 = 6.86
sigma2 = 21.77
zL2 = delta2/sqrt(4/197*sigma2^2)

t2 = des2$secondaryTrial$byStageResults$informationRates[1:L2]

# confidence interval
getADCI(L = L, zL = zL,
        IMax = n/(4*sigma1^2), kMax = 3,
        informationRates = t,
        alpha = 0.05, typeAlphaSpending = "sfHSD",
        parameterAlphaSpending = -4,
        L2 = L2, zL2 = zL2,
        INew = n2/(4*sigma2^2),
        MullerSchafer = TRUE,
        informationRatesNew = t2,
        typeAlphaSpendingNew = "sfHSD",
        parameterAlphaSpendingNew = -2)
```

---

getADRCI   *Repeated Confidence Interval After Adaptation*

Description

Obtains the repeated p-value, conservative point estimate, and repeated confidence interval for an adaptive group sequential trial.

Usage

```
getADRCI(
  L = NA_integer_,
  zL = NA_real_,
  IMax = NA_real_,
  kMax = NA_integer_,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  spendingTime = NA_real_,
  L2 = NA_integer_,
  zL2 = NA_real_,
  INew = NA_real_,
  MullerSchafer = 0L,
```

```
    informationRatesNew = NA_real_,
    efficacyStoppingNew = NA_integer_,
    typeAlphaSpendingNew = "sfOF",
    parameterAlphaSpendingNew = NA_real_,
    spendingTimeNew = NA_real_
)
```

Arguments

L	The interim adaptation look of the primary trial.
zL	The z-test statistic at the interim adaptation look of the primary trial.
IMax	The maximum information of the primary trial.
kMax	The maximum number of stages of the primary trial.
informationRates	
	The information rates of the primary trial.
efficacyStopping	
	Indicators of whether efficacy stopping is allowed at each stage of the primary trial. Defaults to true if left unspecified.
criticalValues	The upper boundaries on the z-test statistic scale for efficacy stopping for the primary trial.
alpha	The significance level of the primary trial. Defaults to 0.025.
typeAlphaSpending	
	The type of alpha spending for the primary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	
	The parameter value of alpha spending for the primary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
spendingTime	The error spending time of the primary trial. Defaults to missing, in which case, it is the same as informationRates.
L2	The look of interest in the secondary trial.
zL2	The z-test statistic at the look of the secondary trial.
INew	The maximum information of the secondary trial.
MullerSchafer	Whether to use the Muller and Schafer (2001) method for trial adaptation.
informationRatesNew	
	The spacing of looks of the secondary trial.
efficacyStoppingNew	
	The indicators of whether efficacy stopping is allowed at each look of the secondary trial up to look L2. Defaults to true if left unspecified.

typeAlphaSpendingNew

> The type of alpha spending for the secondary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpendingNew

> The parameter value of alpha spending for the secondary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

spendingTimeNew

> The error spending time of the secondary trial. up to look L2. Defaults to missing, in which case, it is the same as informationRatesNew.

Value

A data frame with the following variables:

- pvalue: Repeated p-value for rejecting the null hypothesis.
- thetahat: Point estimate of the parameter.
- cilevel: Confidence interval level.
- lower: Lower bound of repeated confidence interval.
- upper: Upper bound of repeated confidence interval.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Cyrus R. Mehta, Peter Bauer, Martin Posch and Werner Brannath. Repeated confidence intervals for adaptive group sequential trials. Stat Med. 2007;26:5422–5433.

See Also

[adaptDesign](#)

Examples

```
# original group sequential design with 90% power to detect delta = 6
delta = 6
sigma = 17
n = 282
(des1 = getDesign(IMax = n/(4*sigma^2), theta = delta, kMax = 3,
                  alpha = 0.05, typeAlphaSpending = "sfHSD",
                  parameterAlphaSpending = -4))

# interim look results
L = 1
```

```
n1 = n/3
delta1 = 4.5
sigma1 = 20
zL = delta1/sqrt(4/n1*sigma1^2)

t = des1$byStageResults$informationRates

# Muller & Schafer (2001) method to design the secondary trial:
des2 = adaptDesign(
  betaNew = 0.2, L = L, zL = zL, theta = 5,
  kMax = 3, informationRates = t,
  alpha = 0.05, typeAlphaSpending = "sfHSD",
  parameterAlphaSpending = -4,
  MullerSchafer = TRUE,
  kNew = 3, typeAlphaSpendingNew = "sfHSD",
  parameterAlphaSpendingNew = -2)

n2 = ceiling(des2$secondaryTrial$overallResults$information*4*20^2)
ns = round(n2*(1:3)/3)
(des2 = adaptDesign(
  INew = n2/(4*20^2), L = L, zL = zL, theta = 5,
  kMax = 3, informationRates = t,
  alpha = 0.05, typeAlphaSpending = "sfHSD",
  parameterAlphaSpending = -4,
  MullerSchafer = TRUE,
  kNew = 3, informationRatesNew = ns/n2,
  typeAlphaSpendingNew = "sfHSD",
  parameterAlphaSpendingNew = -2))

# termination at the second look of the secondary trial
L2 = 2
delta2 = 6.86
sigma2 = 21.77
zL2 = delta2/sqrt(4/197*sigma2^2)

t2 = des2$secondaryTrial$byStageResults$informationRates[1:L2]

# repeated confidence interval
getADRCI(L = L, zL = zL,
         IMax = n/(4*sigma1^2), kMax = 3,
         informationRates = t,
         alpha = 0.05, typeAlphaSpending = "sfHSD",
         parameterAlphaSpending = -4,
         L2 = L2, zL2 = zL2,
         INew = n2/(4*sigma2^2),
         MullerSchafer = TRUE,
         informationRatesNew = t2,
         typeAlphaSpendingNew = "sfHSD",
         parameterAlphaSpendingNew = -2)
```

---

getBound | *Efficacy Boundaries for Group Sequential Design*

Description

Obtains the efficacy stopping boundaries for a group sequential design.

Usage

```
getBound(
  k = NA,
  informationRates = NA,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA,
  userAlphaSpending = NA,
  spendingTime = NA,
  efficacyStopping = NA
)
```

Arguments

k   Look number for the current analysis.

informationRates

                  Information rates up to the current look. Must be increasing and less than or equal to 1.

alpha   The significance level. Defaults to 0.025.

typeAlphaSpending

                  The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

                  The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

                  The user defined alpha spending. Cumulative alpha spent up to each stage.

spendingTime   A vector of length k for the error spending time at each analysis. Must be increasing and less than or equal to 1. Defaults to missing, in which case, it is the same as informationRates.

efficacyStopping

                  Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

Details

If `typeAlphaSpending` is "OF", "P", or "WT", then the boundaries will be based on equally spaced looks.

Value

A numeric vector of critical values up to the current look.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
getBound(k = 2, informationRates = c(0.5,1),
          alpha = 0.025, typeAlphaSpending = "sfOF")
```

---

getCI   *Confidence Interval After Trial Termination*

Description

Obtains the p-value, median unbiased point estimate, and confidence interval after the end of a group sequential trial.

Usage

```
getCI(
  L = NA_integer_,
  zL = NA_real_,
  IMax = NA_real_,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

L	The termination look.
zL	The z-test statistic at the termination look.
IMax	The maximum information of the trial.

informationRates

         The information rates up to look L.

efficacyStopping

         Indicators of whether efficacy stopping is allowed at each stage up to look L. Defaults to true if left unspecified.

criticalValues   The upper boundaries on the z-test statistic scale for efficacy stopping up to look L.

alpha   The significance level. Defaults to 0.025.

typeAlphaSpending

         The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

         The parameter value of alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

spendingTime   The error spending time up to look L. Defaults to missing, in which case, it is the same as informationRates.

Value

A data frame with the following components:

- pvalue: p-value for rejecting the null hypothesis.
- thetahat: Median unbiased point estimate of the parameter.
- cilevel: Confidence interval level.
- lower: Lower bound of confidence interval.
- upper: Upper bound of confidence interval.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Anastasios A. Tsiatis, Gary L. Rosner and Cyrus R. Mehta. Exact confidence intervals following a group sequential test. Biometrics 1984;40:797-803.

Examples

```
# group sequential design with 90% power to detect delta = 6
delta = 6
sigma = 17
n = 282
(des1 = getDesign(IMax = n/(4*sigma^2), theta = delta, kMax = 3,
                  alpha = 0.05, typeAlphaSpending = "sfHSD",
```

```
                parameterAlphaSpending = -4))

# crossed the boundary at the second look
L = 2
n1 = n*2/3
delta1 = 7
sigma1 = 20
zL = delta1/sqrt(4/n1*sigma1^2)

# confidence interval
getCI(L = L, zL = zL, IMax = n/(4*sigma1^2),
      informationRates = c(1/3, 2/3), alpha = 0.05,
      typeAlphaSpending = "sfHSD", parameterAlphaSpending = -4)
```

---

getCP   *Conditional Power Allowing for Varying Parameter Values*

Description

Obtains the conditional power for specified incremental information given the interim results, parameter values, and data-dependent changes in the error spending function, as well as the number and spacing of interim looks.

Usage

```
getCP(
  INew = NA_real_,
  L = NA_integer_,
  zL = NA_real_,
  theta = NA_real_,
  IMax = NA_real_,
  kMax = NA_integer_,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  spendingTime = NA_real_,
  MullerSchafer = 0L,
  kNew = NA_integer_,
  informationRatesNew = NA_real_,
```

```
  efficacyStoppingNew = NA_integer_,
  futilityStoppingNew = NA_integer_,
  typeAlphaSpendingNew = "sfOF",
  parameterAlphaSpendingNew = NA_real_,
  typeBetaSpendingNew = "none",
  parameterBetaSpendingNew = NA_real_,
  spendingTimeNew = NA_real_,
  varianceRatio = 1
)
```

Arguments

INew	The maximum information of the secondary trial.
L	The interim adaptation look of the primary trial.
zL	The z-test statistic at the interim adaptation look of the primary trial.
theta	A scalar or a vector of parameter values of length kMax + kMax - L if MullerSchafer = FALSE or length kMax + kNew if MullerSchafer = TRUE.
IMax	The maximum information of the primary trial.
kMax	The maximum number of stages of the primary trial.
informationRates	
	The information rates of the primary trial.
efficacyStopping	
	Indicators of whether efficacy stopping is allowed at each stage of the primary trial. Defaults to true if left unspecified.
futilityStopping	
	Indicators of whether futility stopping is allowed at each stage of the primary trial. Defaults to true if left unspecified.
criticalValues	The upper boundaries on the z-test statistic scale for efficacy stopping for the primary trial.
alpha	The significance level of the primary trial. Defaults to 0.025.
typeAlphaSpending	
	The type of alpha spending for the primary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	
	The parameter value of alpha spending for the primary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	
	The user defined alpha spending for the primary trial. Cumulative alpha spent up to each stage.
futilityBounds	The lower boundaries on the z-test statistic scale for futility stopping for the primary trial. Defaults to rep(-6, kMax-1) if left unspecified.

typeBetaSpending
:   The type of beta spending for the primary trial. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending
:   The parameter value of beta spending for the primary trial. Corresponds to rho for "sfKD", and gamma for "sfHSD".

spendingTime
:   The error spending time of the primary trial. Defaults to missing, in which case, it is the same as informationRates.

MullerSchafer
:   Whether to use the Muller and Schafer (2001) method for trial adaptation.

kNew
:   The number of looks of the secondary trial.

informationRatesNew
:   The spacing of looks of the secondary trial.

efficacyStoppingNew
:   The indicators of whether efficacy stopping is allowed at each look of the secondary trial. Defaults to true if left unspecified.

futilityStoppingNew
:   The indicators of whether futility stopping is allowed at each look of the secondary trial. Defaults to true if left unspecified.

typeAlphaSpendingNew
:   The type of alpha spending for the secondary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpendingNew
:   The parameter value of alpha spending for the secondary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

typeBetaSpendingNew
:   The type of beta spending for the secondary trial. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpendingNew
:   The parameter value of beta spending for the secondary trial. Corresponds to rho for "sfKD", and gamma for "sfHSD".

spendingTimeNew
:   The error spending time of the secondary trial. Defaults to missing, in which case, it is the same as informationRatesNew.

varianceRatio
:   The ratio of the variance under H0 to the variance under H1.

Value

The conditional power given the interim results, parameter values, and data-dependent design changes.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Cyrus R. Mehta and Stuart J. Pocock. Adaptive increase in sample size when interim results are promising: A practical guide with examples. Stat Med. 2011;30:3267–3284.

See Also

[getDesign](#)

Examples

```
# Conditional power calculation with delayed treatment effect

# Two interim analyses have occurred with 179 and 266 events,
# respectively. The observed hazard ratio at the second interim
# look is 0.81.

trialsdt = as.Date("2020-03-04")                        # trial start date
iadt = c(as.Date("2022-02-01"), as.Date("2022-11-01")) # interim dates
mo1 = as.numeric(iadt - trialsdt + 1)/30.4375          # interim months

# Assume a piecewise Poisson enrollment process with a 8-month ramp-up
# and 521 patients were enrolled after 17.94 months
N = 521                 # total number of patients
Ta = 17.94              # enrollment duration
Ta1 = 8                 # assumed end of enrollment ramp-up
enrate = N / (Ta - Ta1/2) # enrollment rate after ramp-up

# Assume a median survival of 16.7 months for the control group, a
# 5-month delay in treatment effect, and a hazard ratio of 0.7 after
# the delay
lam1 = log(2)/16.7  # control group hazard of exponential distribution
t1 = 5              # months of delay in treatment effect
hr = 0.7            # hazard ratio after delay
lam2 = hr*lam1      # treatment group hazard after delay

# Assume an annual dropout rate of 5%
gam = -log(1-0.05)/12  # hazard for dropout

# The original target number of events was 298 and the new target is 335
mo2 <- caltime(
  nevents = c(298, 335),
  allocationRatioPlanned = 1,
  accrualTime = seq(0, Ta1),
```

```
    accrualIntensity = enrate*seq(1, Ta1+1)/(Ta1+1),
    piecewiseSurvivalTime = c(0, t1),
    lambda1 = c(lam1, lam2),
    lambda2 = c(lam1, lam1),
    gamma1 = gam,
    gamma2 = gam,
    accrualDuration = Ta,
    followupTime = 1000)

# expected number of events and average hazard ratios
(lr1 <- lrstat(
  time = c(mo1, mo2),
  accrualTime = seq(0, Ta1),
  accrualIntensity = enrate*seq(1, Ta1+1)/(Ta1+1),
  piecewiseSurvivalTime = c(0, t1),
  lambda1 = c(lam1, lam2),
  lambda2 = c(lam1, lam1),
  gamma1 = gam,
  gamma2 = gam,
  accrualDuration = Ta,
  followupTime = 1000,
  predictTarget = 3))


hr2 = 0.81                    # observed hazard ratio at interim 2
z2 = (-log(hr2))*sqrt(266/4)  # corresponding z-test statistic value

# expected mean of -log(HR) at the original looks and the new final look
theta = -log(lr1$HR[c(1,2,3,4)])

# conditional power with sample size increase
getCP(INew = (335 - 266)/4,
      L = 2, zL = z2, theta = theta,
      IMax = 298/4, kMax = 3,
      informationRates = c(179, 266, 298)/298,
      alpha = 0.025, typeAlphaSpending = "sfOF")
```

---

getDesign	*Power and Sample Size for a Generic Group Sequential Design*

Description

Obtains the maximum information and stopping boundaries for a generic group sequential design assuming a constant treatment effect, or obtains the power given the maximum information and stopping boundaries.

Usage

```
getDesign(
```

```
    beta = NA_real_,
    IMax = NA_real_,
    theta = NA_real_,
    kMax = 1L,
    informationRates = NA_real_,
    efficacyStopping = NA_integer_,
    futilityStopping = NA_integer_,
    criticalValues = NA_real_,
    alpha = 0.025,
    typeAlphaSpending = "sfOF",
    parameterAlphaSpending = NA_real_,
    userAlphaSpending = NA_real_,
    futilityBounds = NA_real_,
    typeBetaSpending = "none",
    parameterBetaSpending = NA_real_,
    userBetaSpending = NA_real_,
    spendingTime = NA_real_,
    varianceRatio = 1
)
```

Arguments

beta	The type II error.
IMax	The maximum information. Either `beta` or `IMax` should be provided while the other one should be missing.
theta	The parameter value.
kMax	The maximum number of stages.
informationRates	
	The information rates. Fixed prior to the trial. Defaults to `(1:kMax) / kMax` if left unspecified.
efficacyStopping	
	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	
	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	
	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

> The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

> The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

> The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

> The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

> The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

varianceRatio The ratio of the variance under H0 to the variance under H1.

Value

An S3 class design object with three components:

- overallResults: A data frame containing the following variables:
    - overallReject: The overall rejection probability.
    - alpha: The overall significance level.
    - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
    - kMax: The number of stages.
    - theta: The parameter value.
    - information: The maximum information.
    - expectedInformationH1: The expected information under H1.
    - expectedInformationH0: The expected information under H0.
    - drift: The drift parameter, equal to theta*sqrt(information).
    - inflationFactor: The inflation factor (relative to the fixed design).
- byStageResults: A data frame containing the following variables:
    - informationRates: The information rates.
    - efficacyBounds: The efficacy boundaries on the Z-scale.
    - futilityBounds: The futility boundaries on the Z-scale.
    - rejectPerStage: The probability for efficacy stopping.
    - futilityPerStage: The probability for futility stopping.

- cumulativeRejection: The cumulative probability for efficacy stopping.
- cumulativeFutility: The cumulative probability for futility stopping.
- cumulativeAlphaSpent: The cumulative alpha spent.
- efficacyTheta: The efficacy boundaries on the parameter scale.
- futilityTheta: The futility boundaries on the parameter scale.
- efficacyP: The efficacy boundaries on the p-value scale.
- futilityP: The futility boundaries on the p-value scale.
- information: The cumulative information.
- efficacyStopping: Whether to allow efficacy stopping.
- futilityStopping: Whether to allow futility stopping.
- rejectPerStageH0: The probability for efficacy stopping under H0.
- futilityPerStageH0: The probability for futility stopping under H0.
- cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
- cumulativeFutilityH0: The cumulative probability for futility stopping under H0.

- settings: A list containing the following input parameters:
    - typeAlphaSpending: The type of alpha spending.
    - parameterAlphaSpending: The parameter value for alpha spending.
    - userAlphaSpending: The user defined alpha spending.
    - typeBetaSpending: The type of beta spending.
    - parameterBetaSpending: The parameter value for beta spending.
    - userBetaSpending: The user defined beta spending.
    - spendingTime: The error spending time at each analysis.
    - varianceRatio: The ratio of the variance under H0 to the variance under H1.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Christopher Jennison, Bruce W. Turnbull. Group Sequential Methods with Applications to Clinical Trials. Chapman & Hall/CRC: Boca Raton, 2000, ISBN:0849303168

Examples

```
# Example 1: obtain the maximum information given power
(design1 <- getDesign(
  beta = 0.2, theta = -log(0.7),
  kMax = 2, informationRates = c(0.5,1),
  alpha = 0.025, typeAlphaSpending = "sfOF",
  typeBetaSpending = "sfP"))

# Example 2: obtain power given the maximum information
(design2 <- getDesign(
  IMax = 72.5, theta = -log(0.7),
  kMax = 3, informationRates = c(0.5, 0.75, 1),
```

```
    alpha = 0.025, typeAlphaSpending = "sfOF",
    typeBetaSpending = "sfP"))
```

---

getDesignAgreement   *Power and Sample Size for Cohen's kappa*

Description

Obtains the power given sample size or obtains the sample size given power for Cohen's kappa.

Usage

```
getDesignAgreement(
  beta = NA_real_,
  n = NA_real_,
  ncats = NA_integer_,
  kappaH0 = NA_real_,
  kappa = NA_real_,
  p1 = NA_real_,
  p2 = NA_real_,
  rounding = TRUE,
  alpha = 0.025
)
```

Arguments

beta	The type II error.
n	The total sample size.
ncats	The number of categories.
kappaH0	The kappa coefficient under the null hypothesis.
kappa	The kappa coefficient under the alternative hypothesis.
p1	The marginal probabilities for the first rater.
p2	The marginal probabilities for the second rater. Defaults to be equal to the marginal probabilities for the first rater if not provided.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The one-sided significance level. Defaults to 0.025.

Details

The kappa coefficient is defined as

$$\kappa = \frac{\pi_o - \pi_e}{1 - \pi_e},$$

where $\pi_o = \sum_i \pi_{ii}$ is the observed agreement, and $\pi_e = \sum_i \pi_{i.}\pi_{.i}$ is the expected agreement by chance.

By Fleiss et al. (1969), the variance of $\hat{\kappa}$ is given by

$$Var(\hat{\kappa}) = \frac{v_1}{n},$$

where

$$v_1 = \frac{Q_1 + Q_2 - Q3 - Q4}{(1 - \pi_e)^4},$$

$$Q_1 = \pi_o(1 - \pi_e)^2,$$

$$Q_2 = (1 - \pi_o)^2 \sum_i \sum_j \pi_{ij}(\pi_{i.} + \pi_{.j})^2,$$

$$Q_3 = 2(1 - \pi_o)(1 - \pi_e) \sum_i \pi_{ii}(\pi_{i.} + \pi_{.i}),$$

$$Q_4 = (\pi_o\pi_e - 2\pi_e + \pi_o)^2.$$

Given κ and marginals $\{(\pi_{i.}, \pi_{.i}) : i = 1, \ldots, k\}$, we obtain π_o. The only unknowns are the double summation in Q_2 and the single summation in Q_3.

We find the optimal configuration of cell probabilities that yield the maximum variance of $\hat{\kappa}$ by treating the problem as a linear programming problem with constraints to match the given marginal probabilities and the observed agreement and ensure that the cell probabilities are nonnegative. This is an extension of Flack et al. (1988) by allowing unequal marginal probabilities of the two raters.

We perform the optimization under both the null and alternative hypotheses to obtain $\max Var(\hat{\kappa}|\kappa = \kappa_0)$ and $\max Var(\hat{\kappa}|\kappa = \kappa_1)$ for a single subject, and then calculate the sample size or power according to the following equation:

$$\sqrt{n}|\kappa - \kappa_0| = z_{1-\alpha}\sqrt{\max Var(\hat{\kappa}|\kappa = \kappa_0)} + z_{1-\beta}\sqrt{\max Var(\hat{\kappa}|\kappa = \kappa_1)}.$$

Value

An S3 class `designAgreement` object with the following components:

- power: The power to reject the null hypothesis.
- alpha: The one-sided significance level.
- n: The total sample size.
- ncats: The number of categories.
- kappaH0: The kappa coefficient under the null hypothesis.
- kappa: The kappa coefficient under the alternative hypothesis.
- p1: The marginal probabilities for the first rater.
- p2: The marginal probabilities for the second rater.
- piH0: The cell probabilities that maximize the variance of estimated kappa under H0.
- pi: The cell probabilities that maximize the variance of estimated kappa under H1.
- rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

V. F. Flack, A. A. Afifi, and P. A. Lachenbruch. Sample size determinations for the two rater kappa statistic. Psychometrika 1988; 53:321-325.

Examples

```
(design1 <- getDesignAgreement(
  beta = 0.2, n = NA, ncats = 4, kappaH0 = 0.4, kappa = 0.6,
  p1 = c(0.1, 0.2, 0.3, 0.4), p2 = c(0.15, 0.2, 0.24, 0.41),
  rounding = TRUE, alpha = 0.05))
```

---

getDesignANOVA   *Power and Sample Size for One-Way ANOVA*

Description

Obtains the power and sample size for one-way analysis of variance.

Usage

```
getDesignANOVA(
  beta = NA_real_,
  n = NA_real_,
  ngroups = 2,
  means = NA_real_,
  stDev = 1,
  allocationRatioPlanned = NA_real_,
  rounding = TRUE,
  alpha = 0.05
)
```

Arguments

beta	The type II error.
n	The total sample size.
ngroups	The number of treatment groups.
means	The treatment group means.
stDev	The common standard deviation.
allocationRatioPlanned	
	Allocation ratio for the treatment groups. It has length ngroups - 1 or ngroups. If it is of length ngroups - 1, then the last treatment group will assume value 1 for allocation ratio.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.

Details

Let $\{\mu_i : i = 1, \ldots, k\}$ denote the group means, and $\{r_i : i = 1, \ldots, k\}$ denote the randomization probabilities to the k treatment groups. Let σ denote the common standard deviation, and n denote the total sample size. Then the F-statistic

$$F = \frac{SSR/(k-1)}{SSE/(n-k)} \sim F_{k-1,n-k,\lambda},$$

where

$$\lambda = n \sum_{i=1}^{k} r_i (\mu_i - \bar{\mu})^2 / \sigma^2$$

is the noncentrality parameter, and $\bar{\mu} = \sum_{i=1}^{k} r_i \mu_i$.

Value

An S3 class designANOVA object with the following components:

- power: The power to reject the null hypothesis that there is no difference among the treatment groups.

- alpha: The two-sided significance level.

- n: The number of subjects.

- ngroups: The number of treatment groups.

- means: The treatment group means.

- stDev: The common standard deviation.

- effectsize: The effect size.

- allocationRatioPlanned: Allocation ratio for the treatment groups.

- rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignANOVA(
  beta = 0.1, ngroups = 4, means = c(1.5, 2.5, 2, 0),
  stDev = 3.5, allocationRatioPlanned = c(2, 2, 2, 1),
  alpha = 0.05))
```

getDesignANOVAContrast

Power and Sample Size for One-Way ANOVA Contrast

Description

Obtains the power and sample size for a single contrast in one-way analysis of variance.

Usage

```
getDesignANOVAContrast(
  beta = NA_real_,
  n = NA_real_,
  ngroups = 2,
  means = NA_real_,
  stDev = 1,
  contrast = NA_real_,
  meanContrastH0 = 0,
  allocationRatioPlanned = NA_real_,
  rounding = TRUE,
  alpha = 0.025
)
```

Arguments

beta	The type II error.
n	The total sample size.
ngroups	The number of treatment groups.
means	The treatment group means.
stDev	The common standard deviation.
contrast	The coefficients for the single contrast.
meanContrastH0	The mean of the contrast under the null hypothesis.
allocationRatioPlanned	
	Allocation ratio for the treatment groups. It has length ngroups - 1 or ngroups. If it is of length ngroups - 1, then the last treatment group will assume value 1 for allocation ratio.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The one-sided significance level. Defaults to 0.025.

Value

An S3 class designANOVAContrast object with the following components:

- power: The power to reject the null hypothesis for the treatment contrast.

- alpha: The one-sided significance level.
- n: The number of subjects.
- ngroups: The number of treatment groups.
- means: The treatment group means.
- stDev: The common standard deviation.
- contrast: The coefficients for the single contrast.
- meanContrastH0: The mean of the contrast under the null hypothesis.
- meanContrast: The mean of the contrast under the alternative hypothesis.
- effectsize: The effect size.
- allocationRatioPlanned: Allocation ratio for the treatment groups.
- rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignANOVAContrast(
  beta = 0.1, ngroups = 4, means = c(1.5, 2.5, 2, 0),
  stDev = 3.5, contrast = c(1, 1, 1, -3)/3,
  allocationRatioPlanned = c(2, 2, 2, 1),
  alpha = 0.025))
```

---

getDesignEquiv   *Power and Sample Size for a Generic Group Sequential Equivalence Design*

Description

Obtains the maximum information and stopping boundaries for a generic group sequential equivalence design assuming a constant treatment effect, or obtains the power given the maximum information and stopping boundaries.

Usage

```
getDesignEquiv(
  beta = NA_real_,
  IMax = NA_real_,
  thetaLower = NA_real_,
  thetaUpper = NA_real_,
  theta = 0,
  kMax = 1L,
  informationRates = NA_real_,
```

```
    criticalValues = NA_real_,
    alpha = 0.05,
    typeAlphaSpending = "sfOF",
    parameterAlphaSpending = NA_real_,
    userAlphaSpending = NA_real_,
    spendingTime = NA_real_
)
```

Arguments

`beta`	The type II error.
`IMax`	The maximum information. Either `beta` or `IMax` should be provided while the other one should be missing.
`thetaLower`	The parameter value at the lower equivalence limit.
`thetaUpper`	The parameter value at the upper equivalence limit.
`theta`	The parameter value under the alternative hypothesis.
`kMax`	The maximum number of stages.
`informationRates`	
	The information rates. Fixed prior to the trial. Defaults to `(1:kMax) / kMax` if left unspecified.
`criticalValues`	Upper boundaries on the z-test statistic scale for stopping for efficacy.
`alpha`	The significance level for each of the two one-sided tests, e.g., 0.05.
`typeAlphaSpending`	
	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
`parameterAlphaSpending`	
	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
`userAlphaSpending`	
	The user defined alpha spending. Cumulative alpha spent up to each stage.
`spendingTime`	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as `informationRates`.

Details

Consider the equivalence design with two one-sided hypotheses:

$$H_{10} : \theta \leq \theta_{10},$$

$$H_{20} : \theta \geq \theta_{20}.$$

We reject H_{10} at or before look k if

$$Z_{1j} = (\hat{\theta}_j - \theta_{10})\sqrt{I_j} \geq b_j$$

for some $j = 1, \ldots, k$, where $\{b_j : j = 1, \ldots, K\}$ are the critical values associated with the specified alpha-spending function, and I_j is the information for θ (inverse variance of $\hat{\theta}$ under the alternative hypothesis) at the jth look. For example, for estimating the risk difference $\theta = \pi_1 - \pi_2$,

$$I_j = \left\{ \frac{\pi_1(1 - \pi_1)}{n_{1j}} + \frac{\pi_2(1 - \pi_2)}{n_{2j}} \right\}^{-1}.$$

It follows that

$$(Z_{1j} \geq b_j) = (Z_j \geq b_j + (\theta_{10} - \theta)\sqrt{I_j}),$$

where $Z_j = (\hat{\theta}_j - \theta)\sqrt{I_j}$.

Similarly, we reject H_{20} at or before look k if

$$Z_{2j} = (\hat{\theta}_j - \theta_{20})\sqrt{I_j} \leq -b_j$$

for some $j = 1, \ldots, k$. We have

$$(Z_{2j} \leq -b_j) = (Z_j \leq -b_j + (\theta_{20} - \theta)\sqrt{I_j}).$$

Let $l_j = b_j + (\theta_{10} - \theta)\sqrt{I_j}$, and $u_j = -b_j + (\theta_{20} - \theta)\sqrt{I_j}$. The cumulative probability to reject $H_0 = H_{10} \cup H_{20}$ at or before look k under the alternative hypothesis H_1 is given by

$$P_\theta \left(\cup_{j=1}^k (Z_{1j} \geq b_j) \cap \cup_{j=1}^k (Z_{2j} \leq -b_j) \right) = p_1 + p_2 + p_{12},$$

where

$$p_1 = P_\theta \left(\cup_{j=1}^k (Z_{1j} \geq b_j) \right) = P_\theta \left(\cup_{j=1}^k (Z_j \geq l_j) \right),$$

$$p_2 = P_\theta \left(\cup_{j=1}^k (Z_{2j} \leq -b_j) \right) = P_\theta \left(\cup_{j=1}^k (Z_j \leq u_j) \right),$$

and

$$p_{12} = P_\theta \left(\cup_{j=1}^k (Z_j \geq l_j) \cup (Z_j \leq u_j) \right).$$

Of note, both p_1 and p_2 can be evaluated using one-sided exit probabilities for group sequential designs. If there exists $j \leq k$ such that $l_j \leq u_j$, then $p_{12} = 1$. Otherwise, p_{12} can be evaluated using two-sided exit probabilities for group sequential designs.

Since the equivalent hypothesis is tested using two one-sided tests, the type I error is controlled. To evaluate the attained type I error of the equivalence trial under H_{10} (or H_{20}), we simply fix the control group parameters, update the active treatment group parameters according to the null hypothesis, and use the parameters in the power calculation outlined above.

Value

An S3 class designEquiv object with three components:

- overallResults: A data frame containing the following variables:
    - overallReject: The overall rejection probability.
    - alpha: The overall significance level.
    - attainedAlphaH10: The attained significance level under H10.
    - attainedAlphaH20: The attained significance level under H20.
    - kMax: The number of stages.

- – thetaLower: The parameter value at the lower equivalence limit.
- – thetaUpper: The parameter value at the upper equivalence limit.
- – theta: The parameter value under the alternative hypothesis.
- – information: The maximum information.
- – expectedInformationH1: The expected information under H1.
- – expectedInformationH10: The expected information under H10.
- – expectedInformationH20: The expected information under H20.
- byStageResults: A data frame containing the following variables:
  - – informationRates: The information rates.
  - – efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - – rejectPerStage: The probability for efficacy stopping.
  - – cumulativeRejection: The cumulative probability for efficacy stopping.
  - – cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - – cumulativeAttainedAlphaH10: The cumulative probability for efficacy stopping under H10.
  - – cumulativeAttainedAlphaH20: The cumulative probability for efficacy stopping under H20.
  - – efficacyThetaLower: The efficacy boundaries on the parameter scale for the one-sided null hypothesis at the lower equivalence limit.
  - – efficacyThetaUpper: The efficacy boundaries on the parameter scale for the one-sided null hypothesis at the upper equivalence limit.
  - – efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - – information: The cumulative information.
- settings: A list containing the following components:
  - – typeAlphaSpending: The type of alpha spending.
  - – parameterAlphaSpending: The parameter value for alpha spending.
  - – userAlphaSpending: The user defined alpha spending.
  - – spendingTime: The error spending time at each analysis.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: obtain the maximum information given power
(design1 <- getDesignEquiv(
  beta = 0.2, thetaLower = log(0.8), thetaUpper = log(1.25),
  kMax = 2, informationRates = c(0.5, 1),
  alpha = 0.05, typeAlphaSpending = "sfOF"))


# Example 2: obtain power given the maximum information
(design2 <- getDesignEquiv(
  IMax = 72.5, thetaLower = log(0.7), thetaUpper = -log(0.7),
```

```
kMax = 3, informationRates = c(0.5, 0.75, 1),
alpha = 0.05, typeAlphaSpending = "sfOF"))
```

getDesignFisherExact   *Power and Sample Size for Fisher's Exact Test for Two Proportions*

Description

Obtains the power given sample size or obtains the sample size given power for Fisher's exact test
for two proportions.

Usage

```
getDesignFisherExact(
  beta = NA_real_,
  n = NA_real_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  alpha = 0.05
)
```

Arguments

beta	The type II error.
n	The total sample size.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
allocationRatioPlanned	
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
alpha	The two-sided significance level. Defaults to 0.05.

Value

A data frame with the following variables:

- alpha: The two-sided significance level.
- power: The power.
- n: The sample size.
- pi1: The assumed probability for the active treatment group.
- pi2: The assumed probability for the control group.
- allocationRatioPlanned: Allocation ratio for the active treatment versus control.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignFisherExact(
  beta = 0.2, pi1 = 0.5, pi2 = 0.2, alpha = 0.05))
```

---

getDesignLogistic *Power and Sample Size for Logistic Regression*

Description

Obtains the power given sample size or obtains the sample size given power for logistic regression of a binary response given the covariate of interest and other covariates.

Usage

```
getDesignLogistic(
  beta = NA_real_,
  n = NA_real_,
  ncovariates = NA_integer_,
  nconfigs = NA_integer_,
  x = NA_real_,
  pconfigs = NA_real_,
  corr = 0,
  oddsratios = NA_real_,
  responseprob = NA_real_,
  rounding = TRUE,
  alpha = 0.05
)
```

Arguments

beta	The type II error.
n	The total sample size.
ncovariates	The number of covariates.
nconfigs	The number of configurations of discretized covariate values.
x	The matrix of covariate values.
pconfigs	The vector of probabilities for the configurations.
corr	The multiple correlation between the predictor and other covariates. Defaults to 0.
oddsratios	The odds ratios for one unit increase in the covariates.

responseprob	The response probability in the full model when all predictor variables are equal to their means.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.

Details

We consider the logistic regression of a binary response variable Y on a set of predictor variables $x = (x_1, \ldots, x_K)^T$ with x_1 being the covariate of interest: $\log \frac{P(Y_i=1)}{1-P(Y_i=1)} = \psi_0 + x_i^T \psi$, where $\psi = (\psi_1, \ldots, \psi_K)^T$. Similar to Self et al (1992), we assume that all covariates are either inherently discrete or discretized from continuous distributions (e.g. using the quantiles). Let m denote the total number of configurations of the covariate values. Let

$$\pi_i = P(x = x_i), i = 1, \ldots, m$$

denote the probabilities for the configurations of the covariates under independence. The likelihood ratio test statistic for testing $H_0 : \psi_1 = 0$ can be approximated by a noncentral chi-square distribution with one degree of freedom and noncentrality parameter

$$\Delta = 2 \sum_{i=1}^m \pi_i [b'(\theta_i)(\theta_i - \theta_i^*) - \{b(\theta_i) - b(\theta_i^*)\}],$$

where

$$\theta_i = \psi_0 + \sum_{j=1}^k \psi_j x_{ij},$$

$$\theta_i^* = \psi_0^* + \sum_{j=2}^k \psi_j^* x_{ij},$$

for $\psi_0^* = \psi_0 + \psi_1 \mu_1$, and $\psi_j^* = \psi_j$ for $j = 2, \ldots, K$. Here μ_1 is the mean of x_1, e.g., $\mu_1 = \sum_i \pi_i x_{i1}$. In addition, by formulating the logistic regression in the framework of generalized linear models,

$$b(\theta) = \log(1 + \exp(\theta)),$$

and

$$b'(\theta) = \frac{\exp(\theta)}{1 + \exp(\theta)}.$$

The regression coefficients ψ can be obtained by taking the log of the odds ratios for the covariates. The intercept ψ_0 can be derived as

$$\psi_0 = \log(\bar{\mu}/(1 - \bar{\mu})) - \sum_{j=1}^K \psi_j \mu_j,$$

where $\bar{\mu}$ denotes the response probability when all predictor variables are equal to their means.

Finally, let ρ denote the multiple correlation between the predictor and other covariates. The noncentrality parameter of the chi-square test is adjusted downward by multiplying by $1 - \rho^2$.

Value

An S3 class `designLogistic` object with the following components:

- power: The power to reject the null hypothesis.
- alpha: The two-sided significance level.
- n: The total sample size.
- ncovariates: The number of covariates.
- nconfigs: The number of configurations of discretized covariate values.
- x: The matrix of covariate values.
- pconfigs: The vector of probabilities for the configurations.
- corr: The multiple correlation between the predictor and other covariates.
- oddsratios: The odds ratios for one unit increase in the covariates.
- responseprob: The response probability in the full model when all predictor variables are equal to their means.
- effectsize: The effect size for the chi-square test.
- rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Steven G. Self, Robert H. Mauritsen and Jill Ohara. Power calculations for likelihood ratio tests in generalized linear models. Biometrics 1992; 48:31-39.

Examples

```
# two ordinal covariates
x1 = c(5, 10, 15, 20)
px1 = c(0.2, 0.3, 0.3, 0.2)

x2 = c(2, 4, 6)
px2 = c(0.4, 0.4, 0.2)

# discretizing a normal distribution with mean 4 and standard deviation 2
nbins = 10
x3 = qnorm(((1:nbins) - 0.5)/nbins)*2 + 4
px3 = rep(1/nbins, nbins)

# combination of covariate values
nconfigs = length(x1)*length(x2)*length(x3)
x = expand.grid(x3 = x3, x2 = x2, x1 = x1)
x = as.matrix(x[, ncol(x):1])

# probabilities for the covariate configurations under independence
pconfigs = as.numeric(px1 %x% px2 %x% px3)
```

```
# convert the odds ratio for the predictor variable in 5-unit change
# to the odds ratio in 1-unit change
(design1 <- getDesignLogistic(
  beta = 0.1, ncovariates = 3,
  nconfigs = nconfigs,
  x = x,
  pconfigs = pconfigs,
  oddsratios = c(1.2^(1/5), 1.4, 1.3),
  responseprob = 0.25,
  alpha = 0.1))
```

---

getDesignMeanDiff   *Group Sequential Design for Two-Sample Mean Difference*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample mean difference.

Usage

```
getDesignMeanDiff(
  beta = NA_real_,
  n = NA_real_,
  meanDiffH0 = 0,
  meanDiff = 0.5,
  stDev = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
meanDiffH0	The mean difference under the null hypothesis. Defaults to 0.
meanDiff	The mean difference under the alternative hypothesis.
stDev	The standard deviation.
allocationRatioPlanned	
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
normalApproximation	
	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	
	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
efficacyStopping	
	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	
	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	
	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	
	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	
	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.
typeBetaSpending	
	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for

Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designMeanDiff object with three components:

- overallResults: A data frame containing the following variables:
    - overallReject: The overall rejection probability.
    - alpha: The overall significance level.
    - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
    - kMax: The number of stages.
    - theta: The parameter value.
    - information: The maximum information.
    - expectedInformationH1: The expected information under H1.
    - expectedInformationH0: The expected information under H0.
    - drift: The drift parameter, equal to theta*sqrt(information).
    - inflationFactor: The inflation factor (relative to the fixed design).
    - numberOfSubjects: The maximum number of subjects.
    - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
    - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
    - meanDiffH0: The mean difference under the null hypothesis.
    - meanDiff: The mean difference under the alternative hypothesis.
    - stDev: The standard deviation.
- byStageResults: A data frame containing the following variables:
    - informationRates: The information rates.
    - efficacyBounds: The efficacy boundaries on the Z-scale.
    - futilityBounds: The futility boundaries on the Z-scale.
    - rejectPerStage: The probability for efficacy stopping.
    - futilityPerStage: The probability for futility stopping.
    - cumulativeRejection: The cumulative probability for efficacy stopping.
    - cumulativeFutility: The cumulative probability for futility stopping.
    - cumulativeAlphaSpent: The cumulative alpha spent.
    - efficacyP: The efficacy boundaries on the p-value scale.
    - futilityP: The futility boundaries on the p-value scale.

– `information`: The cumulative information.

– `efficacyStopping`: Whether to allow efficacy stopping.

– `futilityStopping`: Whether to allow futility stopping.

– `rejectPerStageH0`: The probability for efficacy stopping under H0.

– `futilityPerStageH0`: The probability for futility stopping under H0.

– `cumulativeRejectionH0`: The cumulative probability for efficacy stopping under H0.

– `cumulativeFutilityH0`: The cumulative probability for futility stopping under H0.

– `efficacyMeanDiff`: The efficacy boundaries on the mean difference scale.

– `futilityMeanDiff`: The futility boundaries on the mean difference scale.

– `numberOfSubjects`: The number of subjects.

- `settings`: A list containing the following input parameters:

    – `typeAlphaSpending`: The type of alpha spending.

    – `parameterAlphaSpending`: The parameter value for alpha spending.

    – `userAlphaSpending`: The user defined alpha spending.

    – `typeBetaSpending`: The type of beta spending.

    – `parameterBetaSpending`: The parameter value for beta spending.

    – `userBetaSpending`: The user defined beta spending.

    – `spendingTime`: The error spending time at each analysis.

    – `allocationRatioPlanned`: Allocation ratio for the active treatment versus control.

    – `normalApproximation`: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.

    – `rounding`: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignMeanDiff(
  beta = NA, n = 456, meanDiff = 9, stDev = 32,
  kMax = 5, alpha = 0.025, typeAlphaSpending = "sfOF",
  typeBetaSpending = "sfP"))

# Example 2: sample size calculation for two-sample t-test
(design2 <- getDesignMeanDiff(
  beta = 0.1, n = NA, meanDiff = 0.3, stDev = 1,
  normalApproximation = FALSE, alpha = 0.025))
```

getDesignMeanDiffCarryover
                                    Power and Sample Size for Direct Treatment Effects in Crossover Tri-
                                    als

Description

Obtains the power and sample size for direct treatment effects in crossover trials accounting or
without accounting for carryover effects.

Usage

```
getDesignMeanDiffCarryover(
  beta = NA_real_,
  n = NA_real_,
  trtpair = NA_real_,
  carryover = TRUE,
  meanDiffH0 = 0,
  meanDiff = 0.5,
  stDev = 1,
  corr = 0.5,
  design = NA_real_,
  cumdrop = NA_real_,
  allocationRatioPlanned = NA_real_,
  normalApproximation = FALSE,
  rounding = TRUE,
  alpha = 0.025
)
```

Arguments

beta	The type II error.
n	The total sample size.
trtpair	The treatment pair of interest to power the study. If not given, it defaults to comparing the first treatment to the last treatment.
carryover	Whether to account for carryover effects in the power calculation. Defaults to TRUE.
meanDiffH0	The mean difference for the treatment pair of interest under the null hypothesis. Defaults to 0.
meanDiff	The mean difference for the treatment pair of interest under the alternative hypothesis.
stDev	The standard deviation for within-subject random error.
corr	The intra-subject correlation due to subject random effect.
design	The crossover design represented by a matrix with rows indexing the sequences, columns indexing the periods, and matrix entries indicating the treatments.

cumdrop	The cumulative dropout rate over periods.
allocationRatioPlanned	
	Allocation ratio for the sequences. Defaults to equal randomization if not provided.
normalApproximation	
	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
rounding	Whether to round up the sample size. Defaults to TRUE for sample size rounding.
alpha	The one-sided significance level. Defaults to 0.025.

Details

The linear mixed-effects model to assess the direct treatment effects in the presence of carryover treatment effects is given by

$$y_{ijk} = \mu + \alpha_i + b_{ij} + \gamma_k + \tau_{d(i,k)} + \lambda_{c(i,k-1)} + e_{ijk},$$

$$i = 1, \ldots, n; j = 1, \ldots, r_i; k = 1, \ldots, p; d, c = 1, \ldots, t,$$

where μ is the general mean, α_i is the effect of the ith treatment sequence, b_{ij} is the random effect with variance σ_b^2 for the jth subject of the ith treatment sequence, γ_k is the period effect, and e_{ijk} is the random error with variance σ^2 for the subject in period k. The direct effect of the treatment administered in period k of sequence i is $\tau_{d(i,k)}$, and $\lambda_{c(i,k-1)}$ is the carryover effect of the treatment administered in period $k-1$ of sequence i. The value of the carryover effect for the observed response in the first period is $\lambda_{c(i,0)} = 0$ since there is no carryover effect in the first period. The intra-subject correlation due to the subject random effect is

$$\rho = \frac{\sigma_b^2}{\sigma_b^2 + \sigma^2}.$$

Therefore, stDev $= \sigma^2$ and corr $= \rho$. By constructing the design matrix X for the linear model with a compound symmetry covariance matrix for the response vector of a subject, we can obtain

$$Var(\hat{\beta}) = (X'V^{-1}X)^{-1}.$$

The covariance matrix for the direct treatment effects and carryover treatment effects can be extracted from the appropriate sub-matrices. The covariance matrix for the direct treatment effects without accounting for the carryover treatment effects can be obtained by omitting the carryover effect terms from the model.

The power is for the direct treatment effect for the treatment pair of interest with or without accounting for carryover effects as determined by the input parameter carryover. The relative efficiency is for the direct treatment effect for the treatment pair of interest accounting for carryover effects relative to that without accounting for carryover effects.

The degrees of freedom for the t-test accounting for carryover effects can be calculated as the total number of observations minus the number of subjects minus $p-1$ minus $2(t-1)$ to account for the subject effect, period effect, and direct and carryover treatment effects. The degrees of freedom for the t-test without accounting for carryover effects is equal to the total number of observations minus the number of subjects minus $p-1$ minus $t-1$ to account for the subject effect, period effect, and direct treatment effects.

Value

An S3 class `designMeanDiffCarryover` object with the following components:

- `power`: The power to reject the null hypothesis.
- `alpha`: The one-sided significance level.
- `numberOfSubjects`: The maximum number of subjects.
- `trtpair`: The treatment pair of interest to power the study.
- `carryover`: Whether to account for carryover effects in the power calculation.
- `meanDiffH0`: The mean difference for the treatment pair of interest under the null hypothesis.
- `meanDiff`: The mean difference for the treatment pair of interest under the alternative hypothesis.
- `stDev`: The standard deviation for within-subject random error.
- `corr`: The intra-subject correlation due to subject random effect.
- `design`: The crossover design represented by a matrix with rows indexing the sequences, columns indexing the periods, and matrix entries indicating the treatments.
- `designMatrix`: The design matrix accounting for intercept, sequence, period, direct treatment effects and carryover treatment effects when `carryover = TRUE`, or the design matrix accounting for intercept, sequence, period, and direct treatment effects when `carryover = FALSE`.
- `nseq`: The number of sequences.
- `nprd`: The number of periods.
- `ntrt`: The number of treatments.
- `cumdrop`: The cumulative dropout rate over periods.
- `V_direct_only`: The covariance matrix for direct treatment effects without accounting for carryover effects. The treatment comparisons for the covariance matrix are for the first $t-1$ treatments relative to the last treatment.
- `V_direct_carry`: The covariance matrix for direct and carryover treatment effects.
- `v_direct_only`: The variance of the direct treatment effect for the treatment pair of interest without accounting for carryover effects.
- `v_direct`: The variance of the direct treatment effect for the treatment pair of interest accounting for carryover effects.
- `v_carry`: The variance of the carryover treatment effect for the treatment pair of interest.
- `releff_direct`: The relative efficiency of the design for estimating the direct treatment effect for the treatment pair of interest after accounting for carryover effects with respect to that without accounting for carryover effects. This is equal to `v_direct_only/v_direct`.
- `releff_carry`: The relative efficiency of the design for estimating the carryover effect for the treatment pair of interest. This is equal to `v_direct_only/v_carry`.
- `allocationRatioPlanned`: Allocation ratio for the sequences.
- `normalApproximation`: The type of computation of the p-values. If `TRUE`, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
- `rounding`: Whether to round up the sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Robert O. Kuehl. Design of Experiments: Statistical Principles of Research Design and Analysis. Brooks/Cole: Pacific Grove, CA. 2000.

Examples

```
# Williams design for 4 treatments

(design1 = getDesignMeanDiffCarryover(
  beta = 0.2, n = NA,
  meanDiff = 0.5, stDev = 1,
  design = matrix(c(1, 4, 2, 3,
                    2, 1, 3, 4,
                    3, 2, 4, 1,
                    4, 3, 1, 2),
                  4, 4, byrow = TRUE),
  alpha = 0.025))
```

---

getDesignMeanDiffCarryoverEquiv

Power and Sample Size for Equivalence in Direct Treatment Effects in Crossover Trials

---

Description

Obtains the power and sample size for equivalence in direct treatment effects in crossover trials accounting or without accounting for carryover effects.

Usage

```
getDesignMeanDiffCarryoverEquiv(
  beta = NA_real_,
  n = NA_real_,
  trtpair = NA_real_,
  carryover = TRUE,
  meanDiffLower = NA_real_,
  meanDiffUpper = NA_real_,
  meanDiff = 0,
  stDev = 1,
  corr = 0.5,
  design = NA_real_,
  cumdrop = NA_real_,
  allocationRatioPlanned = NA_real_,
```

```
    normalApproximation = FALSE,
    rounding = TRUE,
    alpha = 0.025
)
```

Arguments

beta	The type II error.
n	The total sample size.
trtpair	The treatment pair of interest to power the study. If not given, it defaults to comparing the first treatment to the last treatment.
carryover	Whether to account for carryover effects in the power calculation. Defaults to TRUE.
meanDiffLower	The lower equivalence limit of mean difference for the treatment pair of interest.
meanDiffUpper	The upper equivalence limit of mean difference for the treatment pair of interest.
meanDiff	The mean difference under the alternative hypothesis,
stDev	The standard deviation for within-subject random error.
corr	The intra-subject correlation due to subject random effect.
design	The crossover design represented by a matrix with rows indexing the sequences, columns indexing the periods, and matrix entries indicating the treatments.
cumdrop	The cumulative dropout rate over periods.
allocationRatioPlanned	
	Allocation ratio for the sequences. Defaults to equal randomization if not provided.
normalApproximation	
	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
rounding	Whether to round up the sample size. Defaults to TRUE for sample size rounding.
alpha	The one-sided significance level. Defaults to 0.025.

Details

The linear mixed-effects model to assess the direct treatment effects in the presence of carryover treatment effects is given by

$$y_{ijk} = \mu + \alpha_i + b_{ij} + \gamma_k + \tau_{d(i,k)} + \lambda_{c(i,k-1)} + e_{ijk},$$

$$i = 1, \ldots, n; j = 1, \ldots, r_i; k = 1, \ldots, p; d, c = 1, \ldots, t,$$

where μ is the general mean, α_i is the effect of the ith treatment sequence, b_{ij} is the random effect with variance σ_b^2 for the jth subject of the ith treatment sequence, γ_k is the period effect, and e_{ijk} is the random error with variance σ^2 for the subject in period k. The direct effect of the treatment administered in period k of sequence i is $\tau_{d(i,k)}$, and $\lambda_{c(i,k-1)}$ is the carryover effect of the treatment administered in period $k-1$ of sequence i. The value of the carryover effect for the

observed response in the first period is $\lambda_{c(i,0)} = 0$ since there is no carryover effect in the first period. The intra-subject correlation due to the subject random effect is

$$\rho = \frac{\sigma_b^2}{\sigma_b^2 + \sigma^2}.$$

Therefore, `stDev` $= \sigma^2$ and `corr` $= \rho$. By constructing the design matrix X for the linear model with a compound symmetry covariance matrix for the response vector of a subject, we can obtain

$$Var(\hat{\beta}) = (X'V^{-1}X)^{-1}.$$

The covariance matrix for the direct treatment effects and carryover treatment effects can be extracted from the appropriate sub-matrices. The covariance matrix for the direct treatment effects without accounting for the carryover treatment effects can be obtained by omitting the carryover effect terms from the model.

The power is for the direct treatment effect for the treatment pair of interest with or without accounting for carryover effects as determined by the input parameter `carryover`. The relative efficiency is for the direct treatment effect for the treatment pair of interest accounting for carryover effects relative to that without accounting for carryover effects.

The degrees of freedom for the t-test accounting for carryover effects can be calculated as the total number of observations minus the number of subjects minus $p - 1$ minus $2(t - 1)$ to account for the subject effect, period effect, and direct and carryover treatment effects. The degrees of freedom for the t-test without accounting for carryover effects is equal to the total number of observations minus the number of subjects minus $p - 1$ minus $t - 1$ to account for the subject effect, period effect, and direct treatment effects.

Value

An S3 class `designMeanDiffCarryover` object with the following components:

- `power`: The power to reject the null hypothesis.
- `alpha`: The one-sided significance level.
- `numberOfSubjects`: The maximum number of subjects.
- `trtpair`: The treatment pair of interest to power the study.
- `carryover`: Whether to account for carryover effects in the power calculation.
- `meanDiffLower`: The lower equivalence limit of mean difference for the treatment pair of interest.
- `meanDiffUpper`: The upper equivalence limit of mean difference for the treatment pair of interest.
- `meanDiff`: The mean difference for the treatment pair of interest under the alternative hypothesis.
- `stDev`: The standard deviation for within-subject random error.
- `corr`: The intra-subject correlation due to subject random effect.
- `design`: The crossover design represented by a matrix with rows indexing the sequences, columns indexing the periods, and matrix entries indicating the treatments.

- designMatrix: The design matrix accounting for intercept, sequence, period, direct treatment effects and carryover treatment effects when carryover = TRUE, or the design matrix accounting for intercept, sequence, period, and direct treatment effects when carryover = FALSE.

- nseq: The number of sequences.

- nprd: The number of periods.

- ntrt: The number of treatments.

- cumdrop: The cumulative dropout rate over periods.

- V_direct_only: The covariance matrix for direct treatment effects without accounting for carryover effects. The treatment comparisons for the covariance matrix are for the first $t - 1$ treatments relative to the last treatment.

- V_direct_carry: The covariance matrix for direct and carryover treatment effects.

- v_direct_only: The variance of the direct treatment effect for the treatment pair of interest without accounting for carryover effects.

- v_direct: The variance of the direct treatment effect for the treatment pair of interest accounting for carryover effects.

- v_carry: The variance of the carryover treatment effect for the treatment pair of interest.

- releff_direct: The relative efficiency of the design for estimating the direct treatment effect for the treatment pair of interest after accounting for carryover effects with respect to that without accounting for carryover effects. This is equal to v_direct_only/v_direct.

- releff_carry: The relative efficiency of the design for estimating the carryover effect for the treatment pair of interest. This is equal to v_direct_only/v_carry.

- allocationRatioPlanned: Allocation ratio for the sequences.

- normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.

- rounding: Whether to round up the sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Robert O. Kuehl. Design of Experiments: Statistical Principles of Research Design and Analysis. Brooks/Cole: Pacific Grove, CA. 2000.

Examples

```
# Williams design for 4 treatments

(design1 = getDesignMeanDiffCarryoverEquiv(
  beta = 0.2, n = NA,
  meanDiffLower = -1.3, meanDiffUpper = 1.3,
  meanDiff = 0, stDev = 2.2,
  design = matrix(c(1, 4, 2, 3,
```

```
                          2, 1, 3, 4,
                          3, 2, 4, 1,
                          4, 3, 1, 2),
                        4, 4, byrow = TRUE),
      alpha = 0.025))
```

---

getDesignMeanDiffEquiv

Group Sequential Design for Equivalence in Two-Sample Mean Difference

---

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in two-sample mean difference.

Usage

```
getDesignMeanDiffEquiv(
  beta = NA_real_,
  n = NA_real_,
  meanDiffLower = NA_real_,
  meanDiffUpper = NA_real_,
  meanDiff = 0,
  stDev = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
meanDiffLower	The lower equivalence limit of mean difference.
meanDiffUpper	The upper equivalence limit of mean difference.
meanDiff	The mean difference under the alternative hypothesis.
stDev	The standard deviation.

allocationRatioPlanned

    Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

normalApproximation

    The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

rounding   Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax   The maximum number of stages.

informationRates

    The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

alpha   The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending

    The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

    The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

    The user defined alpha spending. Cumulative alpha spent up to each stage.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designMeanDiffEquiv object with three components:

- overallResults: A data frame containing the following variables:
    - overallReject: The overall rejection probability.
    - alpha: The significance level for each of the two one-sided tests. Defaults to 0.05.
    - attainedAlpha: The attained significance level.
    - kMax: The number of stages.
    - information: The maximum information.
    - expectedInformationH1: The expected information under H1.
    - expectedInformationH0: The expected information under H0.
    - numberOfSubjects: The maximum number of subjects.
    - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
    - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
    - meanDiffLower: The lower equivalence limit of mean difference.
    - meanDiffUpper: The upper equivalence limit of mean difference.

  – meanDiff: The mean difference under the alternative hypothesis.

  – stDev: The standard deviation.

- byStageResults: A data frame containing the following variables:

  – informationRates: The information rates.

  – efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.

  – rejectPerStage: The probability for efficacy stopping.

  – cumulativeRejection: The cumulative probability for efficacy stopping.

  – cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.

  – cumulativeAttainedAlpha: The cumulative probability for efficacy stopping under H0.

  – efficacyMeanDiffLower: The efficacy boundaries on the mean difference scale for the one-sided null hypothesis on the lower equivalence limit.

  – efficacyMeanDiffUpper: The efficacy boundaries on the mean difference scale for the one-sided null hypothesis on the upper equivalence limit.

  – efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.

  – information: The cumulative information.

  – numberOfSubjects: The number of subjects.

- settings: A list containing the following input parameters:

  – typeAlphaSpending: The type of alpha spending.

  – parameterAlphaSpending: The parameter value for alpha spending.

  – userAlphaSpending: The user defined alpha spending.

  – spendingTime: The error spending time at each analysis.

  – allocationRatioPlanned: Allocation ratio for the active treatment versus control.

  – normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

  – rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignMeanDiffEquiv(
  beta = 0.1, n = NA, meanDiffLower = -1.3, meanDiffUpper = 1.3,
  meanDiff = 0, stDev = 2.2,
  kMax = 4, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for t-test
(design2 <- getDesignMeanDiffEquiv(
  beta = 0.1, n = NA, meanDiffLower = -1.3, meanDiffUpper = 1.3,
  meanDiff = 0, stDev = 2.2,
  normalApproximation = FALSE, alpha = 0.05))
```

---

getDesignMeanDiffMMRM   *Group Sequential Design for Two-Sample Mean Difference From the*
                         MMRM Model

Description

Obtains the power and sample size for two-sample mean difference at the last time point from the
mixed-model for repeated measures (MMRM) model.

Usage

```
getDesignMeanDiffMMRM(
  beta = NA_real_,
  meanDiffH0 = 0,
  meanDiff = 0.5,
  k = 1,
  t = NA_real_,
  covar1 = diag(k),
  covar2 = NA_real_,
  accrualTime = 0,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0,
  gamma1 = 0,
  gamma2 = 0,
  accrualDuration = NA_real_,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta   The type II error.

meanDiffH0	The mean difference at the last time point under the null hypothesis. Defaults to 0.
meanDiff	The mean difference at the last time point under the alternative hypothesis.
k	The number of postbaseline time points.
t	The postbaseline time points.
covar1	The covariance matrix for the repeated measures given baseline for the active treatment group.
covar2	The covariance matrix for the repeated measures given baseline for the control group. If missing, it will be set equal to the covariance matrix for the active treatment group.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).
accrualIntensity	
	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	
	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.
gamma1	The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the active treatment group.
gamma2	The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the control group.
accrualDuration	
	Duration of the enrollment period.
allocationRatioPlanned	
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
normalApproximation	
	The type of computation of the p-values. If `TRUE`, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The degrees of freedom for the t-distribution is the total effective sample size minus 2. The exact calculation using the t distribution is only implemented for the fixed design.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	
	The information rates. Defaults to `(1:kMax) / kMax` if left unspecified.
efficacyStopping	
	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	
	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha   The significance level. Defaults to 0.025.

typeAlphaSpending

        The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

        The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

        The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

        The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

        The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

        The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designMeanDiffMMRM object with three components:

- overallResults: A data frame containing the following variables:
    - overallReject: The overall rejection probability.
    - alpha: The overall significance level.
    - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
    - kMax: The number of stages.
    - theta: The parameter value.
    - information: The maximum information.
    - expectedInformationH1: The expected information under H1.
    - expectedInformationH0: The expected information under H0.

- – drift: The drift parameter, equal to theta*sqrt(information).
- – inflationFactor: The inflation factor (relative to the fixed design).
- – numberOfSubjects: The maximum number of subjects.
- – studyDuration: The maximum study duration.
- – expectedNumberOfSubjectsH1: The expected number of subjects under H1.
- – expectedNumberOfSubjectsH0: The expected number of subjects under H0.
- – expectedStudyDurationH1: The expected study duration under H1.
- – expectedStudyDurationH0: The expected study duration under H0.
- – accrualDuration: The accrual duration.
- – followupTime: The follow-up time.
- – fixedFollowup: Whether a fixed follow-up design is used.
- – meanDiffH0: The mean difference under H0.
- – meanDiff: The mean difference under H1.

- byStageResults: A data frame containing the following variables:

  - – informationRates: The information rates.
  - – efficacyBounds: The efficacy boundaries on the Z-scale.
  - – futilityBounds: The futility boundaries on the Z-scale.
  - – rejectPerStage: The probability for efficacy stopping.
  - – futilityPerStage: The probability for futility stopping.
  - – cumulativeRejection: The cumulative probability for efficacy stopping.
  - – cumulativeFutility: The cumulative probability for futility stopping.
  - – cumulativeAlphaSpent: The cumulative alpha spent.
  - – efficacyP: The efficacy boundaries on the p-value scale.
  - – futilityP: The futility boundaries on the p-value scale.
  - – information: The cumulative information.
  - – efficacyStopping: Whether to allow efficacy stopping.
  - – futilityStopping: Whether to allow futility stopping.
  - – rejectPerStageH0: The probability for efficacy stopping under H0.
  - – futilityPerStageH0: The probability for futility stopping under H0.
  - – cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - – cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - – efficacyMeanDiff: The efficacy boundaries on the mean difference scale.
  - – futilityMeanDiff: The futility boundaries on the mean difference scale.
  - – numberOfSubjects: The number of subjects.
  - – analysisTime: The average time since trial start.

- settings: A list containing the following input parameters:

  - – typeAlphaSpending: The type of alpha spending.
  - – parameterAlphaSpending: The parameter value for alpha spending.
  - – userAlphaSpending: The user defined alpha spending.
  - – typeBetaSpending: The type of beta spending.
  - – parameterBetaSpending: The parameter value for beta spending.

- userBetaSpending: The user defined beta spending.
- spendingTime: The error spending time at each analysis.
- allocationRatioPlanned: The allocation ratio for the active treatment versus control.
- accrualTime: A vector that specifies the starting time of piecewise Poisson enrollment time intervals.
- accrualIntensity: A vector of accrual intensities. One for each accrual time interval.
- piecewiseSurvivalTime: A vector that specifies the starting time of piecewise exponential survival time intervals.
- gamma1: The hazard rate for exponential dropout or a vector of hazard rates for piecewise exponential dropout for the active treatment group.
- gamma2: The hazard rate for exponential dropout or a vector of hazard rates for piecewise exponential dropout for the control group.
- k: The number of postbaseline time points.
- t: The postbaseline time points.
- covar1: The covariance matrix for the repeated measures given baseline for the active treatment group.
- covar2: The covariance matrix for the repeated measures given baseline for the control group.
- normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
- rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# function to generate the AR(1) correlation matrix
ar1_cor <- function(n, corr) {
  exponent <- abs(matrix((1:n) - 1, n, n, byrow = TRUE) - ((1:n) - 1))
  corr^exponent
}

(design1 = getDesignMeanDiffMMRM(
  beta = 0.2,
  meanDiffH0 = 0,
  meanDiff = 0.5,
  k = 4,
  t = c(1,2,3,4),
  covar1 = ar1_cor(4, 0.7),
  accrualIntensity = 10,
  gamma1 = 0.02634013,
  gamma2 = 0.02634013,
  accrualDuration = NA,
  allocationRatioPlanned = 1,
  kMax = 3,
  alpha = 0.025,
  typeAlphaSpending = "sfOF"))
```

---

getDesignMeanDiffXO   *Group Sequential Design for Mean Difference in 2x2 Crossover*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample mean difference in 2x2 crossover.

Usage

```
getDesignMeanDiffXO(
  beta = NA_real_,
  n = NA_real_,
  meanDiffH0 = 0,
  meanDiff = 0.5,
  stDev = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
meanDiffH0	The mean difference under the null hypothesis. Defaults to 0.
meanDiff	The mean difference under the alternative hypothesis.
stDev	The standard deviation for within-subject random error.
allocationRatioPlanned	
	Allocation ratio for sequence A/B versus sequence B/A. Defaults to 1 for equal randomization.

normalApproximation

> The type of computation of the p-values. If `TRUE`, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

rounding   Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax   The maximum number of stages.

informationRates

> The information rates. Fixed prior to the trial. Defaults to `(1:kMax) / kMax` if left unspecified.

efficacyStopping

> Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

> Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues   Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha   The significance level. Defaults to 0.025.

typeAlphaSpending

> The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

> The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

> The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds   Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., `kMax-1`. Defaults to `rep(-6, kMax-1)` if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

> The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

> The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

> The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime   A vector of length `kMax` for the error spending time at each analysis. Defaults to missing, in which case, it is the same as `informationRates`.

Value

An S3 class designMeanDiffXO object with three components:

- overallResults: A data frame containing the following variables:
    - overallReject: The overall rejection probability.
    - alpha: The overall significance level.
    - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
    - kMax: The number of stages.
    - theta: The parameter value.
    - information: The maximum information.
    - expectedInformationH1: The expected information under H1.
    - expectedInformationH0: The expected information under H0.
    - drift: The drift parameter, equal to theta*sqrt(information).
    - inflationFactor: The inflation factor (relative to the fixed design).
    - numberOfSubjects: The maximum number of subjects.
    - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
    - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
    - meanDiffH0: The mean difference under the null hypothesis.
    - meanDiff: The mean difference under the alternative hypothesis.
    - stDev: The standard deviation for within-subject random error.
- byStageResults: A data frame containing the following variables:
    - informationRates: The information rates.
    - efficacyBounds: The efficacy boundaries on the Z-scale.
    - futilityBounds: The futility boundaries on the Z-scale.
    - rejectPerStage: The probability for efficacy stopping.
    - futilityPerStage: The probability for futility stopping.
    - cumulativeRejection: The cumulative probability for efficacy stopping.
    - cumulativeFutility: The cumulative probability for futility stopping.
    - cumulativeAlphaSpent: The cumulative alpha spent.
    - efficacyP: The efficacy boundaries on the p-value scale.
    - futilityP: The futility boundaries on the p-value scale.
    - information: The cumulative information.
    - efficacyStopping: Whether to allow efficacy stopping.
    - futilityStopping: Whether to allow futility stopping.
    - rejectPerStageH0: The probability for efficacy stopping under H0.
    - futilityPerStageH0: The probability for futility stopping under H0.
    - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
    - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
    - efficacyMeanDiff: The efficacy boundaries on the mean difference scale.
    - futilityMeanDiff: The futility boundaries on the mean difference scale.
    - numberOfSubjects: The number of subjects.

- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - allocationRatioPlanned: Allocation ratio for sequence A/B versus sequence B/A.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
  - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignMeanDiffXO(
  beta = 0.2, n = NA, meanDiff = 75, stDev = 150,
  normalApproximation = FALSE, alpha = 0.05))
```

getDesignMeanDiffXOEquiv

Group Sequential Design for Equivalence in Mean Difference in 2x2 Crossover

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in mean difference in 2x2 crossover.

Usage

```
getDesignMeanDiffXOEquiv(
  beta = NA_real_,
  n = NA_real_,
  meanDiffLower = NA_real_,
  meanDiffUpper = NA_real_,
  meanDiff = 0,
  stDev = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
```

```
  kMax = 1L,
  informationRates = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
meanDiffLower	The lower equivalence limit of mean difference.
meanDiffUpper	The upper equivalence limit of mean difference.
meanDiff	The mean difference under the alternative hypothesis.
stDev	The standard deviation for within-subject random error.
allocationRatioPlanned	
	Allocation ratio for sequence A/B versus sequence B/A. Defaults to 1 for equal randomization.
normalApproximation	
	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	
	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
alpha	The significance level for each of the two one-sided tests. Defaults to 0.05.
typeAlphaSpending	
	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	
	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	
	The user defined alpha spending. Cumulative alpha spent up to each stage.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designMeanDiffXOEquiv object with three components:

- overallResults: A data frame containing the following variables:
    - overallReject: The overall rejection probability.
    - alpha: The overall significance level.
    - attainedAlpha: The attained significance level.
    - kMax: The number of stages.
    - information: The maximum information.
    - expectedInformationH1: The expected information under H1.
    - expectedInformationH0: The expected information under H0.
    - numberOfSubjects: The maximum number of subjects.
    - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
    - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
    - meanDiffLower: The lower equivalence limit of mean difference.
    - meanDiffUpper: The upper equivalence limit of mean difference.
    - meanDiff: The mean difference under the alternative hypothesis.
    - stDev: The standard deviation for within-subject random error.
- byStageResults: A data frame containing the following variables:
    - informationRates: The information rates.
    - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
    - rejectPerStage: The probability for efficacy stopping.
    - cumulativeRejection: The cumulative probability for efficacy stopping.
    - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
    - cumulativeAttainedAlpha: The cumulative probability for efficacy stopping under H0.
    - efficacyMeanDiffLower: The efficacy boundaries on the mean difference scale for the one-sided null hypothesis on the lower equivalence limit.
    - efficacyMeanDiffUpper: The efficacy boundaries on the mean difference scale for the one-sided null hypothesis on the upper equivalence limit.
    - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
    - information: The cumulative information.
    - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
    - typeAlphaSpending: The type of alpha spending.
    - parameterAlphaSpending: The parameter value for alpha spending.
    - userAlphaSpending: The user defined alpha spending.
    - spendingTime: The error spending time at each analysis.
    - allocationRatioPlanned: Allocation ratio for sequence A/B versus sequence B/A.
    - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
    - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignMeanDiffXOEquiv(
  beta = 0.1, n = NA, meanDiffLower = -1.3, meanDiffUpper = 1.3,
  meanDiff = 0, stDev = 2.2,
  kMax = 4, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for t-test
(design2 <- getDesignMeanDiffXOEquiv(
  beta = 0.1, n = NA, meanDiffLower = -1.3, meanDiffUpper = 1.3,
  meanDiff = 0, stDev = 2.2,
  normalApproximation = FALSE, alpha = 0.05))
```

---

getDesignMeanRatio   *Group Sequential Design for Two-Sample Mean Ratio*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample mean ratio.

Usage

```
getDesignMeanRatio(
  beta = NA_real_,
  n = NA_real_,
  meanRatioH0 = 1,
  meanRatio = 1.25,
  CV = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
```

```
    parameterBetaSpending = NA_real_,
    userBetaSpending = NA_real_,
    spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
meanRatioH0	The mean ratio under the null hypothesis. Defaults to 1.
meanRatio	The mean ratio under the alternative hypothesis.
CV	The coefficient of variation. The standard deviation on the log scale is equal to sqrt(log(1 + CV^2)).
allocationRatioPlanned	
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
normalApproximation	
	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	
	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
efficacyStopping	
	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	
	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	
	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	
	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	
	The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds   Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designMeanRatio object with three components:

- overallResults: A data frame containing the following variables:
    - overallReject: The overall rejection probability.
    - alpha: The overall significance level.
    - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
    - kMax: The number of stages.
    - theta: The parameter value.
    - information: The maximum information.
    - expectedInformationH1: The expected information under H1.
    - expectedInformationH0: The expected information under H0.
    - drift: The drift parameter, equal to theta*sqrt(information).
    - inflationFactor: The inflation factor (relative to the fixed design).
    - numberOfSubjects: The maximum number of subjects.
    - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
    - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
    - meanRatioH0: The mean ratio under the null hypothesis.
    - meanRatio: The mean ratio under the alternative hypothesis.
    - CV: The coefficient of variation.
- byStageResults: A data frame containing the following variables:
    - informationRates: The information rates.
    - efficacyBounds: The efficacy boundaries on the Z-scale.
    - futilityBounds: The futility boundaries on the Z-scale.
    - rejectPerStage: The probability for efficacy stopping.

- – futilityPerStage: The probability for futility stopping.
  - – cumulativeRejection: The cumulative probability for efficacy stopping.
  - – cumulativeFutility: The cumulative probability for futility stopping.
  - – cumulativeAlphaSpent: The cumulative alpha spent.
  - – efficacyP: The efficacy boundaries on the p-value scale.
  - – futilityP: The futility boundaries on the p-value scale.
  - – information: The cumulative information.
  - – efficacyStopping: Whether to allow efficacy stopping.
  - – futilityStopping: Whether to allow futility stopping.
  - – rejectPerStageH0: The probability for efficacy stopping under H0.
  - – futilityPerStageH0: The probability for futility stopping under H0.
  - – cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - – cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - – numberOfSubjects: The number of subjects.
  - – efficacyMeanRatio: The efficacy boundaries on the mean ratio scale.
  - – futilityMeanRatio: The futility boundaries on the mean ratio scale.

- settings: A list containing the following input parameters:

  - – typeAlphaSpending: The type of alpha spending.
  - – parameterAlphaSpending: The parameter value for alpha spending.
  - – userAlphaSpending: The user defined alpha spending.
  - – typeBetaSpending: The type of beta spending.
  - – parameterBetaSpending: The parameter value for beta spending.
  - – userBetaSpending: The user defined beta spending.
  - – spendingTime: The error spending time at each analysis.
  - – allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - – normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
  - – rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignMeanRatio(
  beta = 0.1, n = NA, meanRatio = 1.25, CV = 0.25,
  alpha = 0.05, normalApproximation = FALSE))
```

getDesignMeanRatioEquiv

Group Sequential Design for Equivalence in Two-Sample Mean Ratio

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in two-sample mean ratio.

Usage

```
getDesignMeanRatioEquiv(
  beta = NA_real_,
  n = NA_real_,
  meanRatioLower = NA_real_,
  meanRatioUpper = NA_real_,
  meanRatio = 1,
  CV = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
meanRatioLower	The lower equivalence limit of mean ratio.
meanRatioUpper	The upper equivalence limit of mean ratio.
meanRatio	The mean ratio under the alternative hypothesis.
CV	The coefficient of variation.
allocationRatioPlanned	
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
normalApproximation	
	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

rounding   Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax   The maximum number of stages.

informationRates

                  The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if
                  left unspecified.

alpha   The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending

                  The type of alpha spending. One of the following: "OF" for O'Brien-Fleming
                  boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries,
                  "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spend-
                  ing function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang,
                  Shi & DeCani spending function, "user" for user defined spending, and "none"
                  for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

                  The parameter value for the alpha spending. Corresponds to Delta for "WT",
                  rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

                  The user defined alpha spending. Cumulative alpha spent up to each stage.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to
                  missing, in which case, it is the same as informationRates.

Value

An S3 class designMeanRatioEquiv object with three components:

- overallResults: A data frame containing the following variables:
    - overallReject: The overall rejection probability.
    - alpha: The significance level for each of the two one-sided tests. Defaults to 0.05.
    - attainedAlpha: The attained significance level.
    - kMax: The number of stages.
    - information: The maximum information.
    - expectedInformationH1: The expected information under H1.
    - expectedInformationH0: The expected information under H0.
    - numberOfSubjects: The maximum number of subjects.
    - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
    - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
    - meanRatioLower: The lower equivalence limit of mean ratio.
    - meanRatioUpper: The upper equivalence limit of mean ratio.
    - meanRatio: The mean ratio under the alternative hypothesis.
    - CV: The coefficient of variation.
- byStageResults: A data frame containing the following variables:
    - informationRates: The information rates.
    - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided
      tests.

– rejectPerStage: The probability for efficacy stopping.

– cumulativeRejection: The cumulative probability for efficacy stopping.

– cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.

– cumulativeAttainedAlpha: The cumulative probability for efficacy stopping under H0.

– efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.

– information: The cumulative information.

– numberOfSubjects: The number of subjects.

– efficacyMeanRatioLower: The efficacy boundaries on the mean ratio scale for the one-sided null hypothesis on the lower equivalence limit.

– efficacyMeanRatioUpper: The efficacy boundaries on the mean ratio scale for the one-sided null hypothesis on the upper equivalence limit.

• settings: A list containing the following input parameters:

– typeAlphaSpending: The type of alpha spending.

– parameterAlphaSpending: The parameter value for alpha spending.

– userAlphaSpending: The user defined alpha spending.

– spendingTime: The error spending time at each analysis.

– allocationRatioPlanned: Allocation ratio for the active treatment versus control.

– normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

– rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignMeanRatioEquiv(
  beta = 0.1, n = NA, meanRatioLower = 0.8, meanRatioUpper = 1.25,
  meanRatio = 1, CV = 0.35,
  kMax = 4, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for t-test
(design2 <- getDesignMeanRatioEquiv(
  beta = 0.1, n = NA, meanRatioLower = 0.8, meanRatioUpper = 1.25,
  meanRatio = 1, CV = 0.35,
  normalApproximation = FALSE, alpha = 0.05))
```

---

getDesignMeanRatioXO   *Group Sequential Design for Mean Ratio in 2x2 Crossover*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample mean ratio in 2x2 crossover.

Usage

```
getDesignMeanRatioXO(
  beta = NA_real_,
  n = NA_real_,
  meanRatioH0 = 1,
  meanRatio = 1.25,
  CV = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
meanRatioH0	The mean ratio under the null hypothesis. Defaults to 1.
meanRatio	The mean ratio under the alternative hypothesis.
CV	The coefficient of variation. The standard deviation on the log scale is equal to $sqrt(log(1 + CV^2))$.
allocationRatioPlanned	
	Allocation ratio for sequence A/B versus sequence B/A. Defaults to 1 for equal randomization.

normalApproximation

> The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

rounding   Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax   The maximum number of stages.

informationRates

> The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

> Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

> Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues   Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha   The significance level. Defaults to 0.025.

typeAlphaSpending

> The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

> The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

> The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds   Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

> The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

> The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

> The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designMeanRatioXO object with three components:

- overallResults: A data frame containing the following variables:
    - overallReject: The overall rejection probability.
    - alpha: The overall significance level.
    - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
    - kMax: The number of stages.
    - theta: The parameter value.
    - information: The maximum information.
    - expectedInformationH1: The expected information under H1.
    - expectedInformationH0: The expected information under H0.
    - drift: The drift parameter, equal to theta*sqrt(information).
    - inflationFactor: The inflation factor (relative to the fixed design).
    - numberOfSubjects: The maximum number of subjects.
    - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
    - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
    - meanRatioH0: The mean ratio under the null hypothesis.
    - meanRatio: The mean ratio under the alternative hypothesis.
    - CV: The coefficient of variation.
- byStageResults: A data frame containing the following variables:
    - informationRates: The information rates.
    - efficacyBounds: The efficacy boundaries on the Z-scale.
    - futilityBounds: The futility boundaries on the Z-scale.
    - rejectPerStage: The probability for efficacy stopping.
    - futilityPerStage: The probability for futility stopping.
    - cumulativeRejection: The cumulative probability for efficacy stopping.
    - cumulativeFutility: The cumulative probability for futility stopping.
    - cumulativeAlphaSpent: The cumulative alpha spent.
    - efficacyMeanRatio: The efficacy boundaries on the mean ratio scale.
    - futilityMeanRatio: The futility boundaries on the mean ratio scale.
    - efficacyP: The efficacy boundaries on the p-value scale.
    - futilityP: The futility boundaries on the p-value scale.
    - information: The cumulative information.
    - efficacyStopping: Whether to allow efficacy stopping.
    - futilityStopping: Whether to allow futility stopping.
    - rejectPerStageH0: The probability for efficacy stopping under H0.
    - futilityPerStageH0: The probability for futility stopping under H0.
    - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
    - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
    - numberOfSubjects: The number of subjects.

- settings: A list containing the following input parameters:
    - typeAlphaSpending: The type of alpha spending.
    - parameterAlphaSpending: The parameter value for alpha spending.
    - userAlphaSpending: The user defined alpha spending.
    - typeBetaSpending: The type of beta spending.
    - parameterBetaSpending: The parameter value for beta spending.
    - userBetaSpending: The user defined beta spending.
    - spendingTime: The error spending time at each analysis.
    - allocationRatioPlanned: Allocation ratio for sequence A/B versus sequence B/A.
    - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
    - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignMeanRatioXO(
  beta = 0.1, n = NA, meanRatio = 1.25, CV = 0.25,
  alpha = 0.05, normalApproximation = FALSE))
```

---

getDesignMeanRatioXOEquiv

Group Sequential Design for Equivalence in Mean Ratio in 2x2 Crossover

---

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence mean ratio in 2x2 crossover.

Usage

```
getDesignMeanRatioXOEquiv(
  beta = NA_real_,
  n = NA_real_,
  meanRatioLower = NA_real_,
  meanRatioUpper = NA_real_,
  meanRatio = 1,
  CV = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
```

```
    kMax = 1L,
    informationRates = NA_real_,
    alpha = 0.05,
    typeAlphaSpending = "sfOF",
    parameterAlphaSpending = NA_real_,
    userAlphaSpending = NA_real_,
    spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
meanRatioLower	The lower equivalence limit of mean ratio.
meanRatioUpper	The upper equivalence limit of mean ratio.
meanRatio	The mean ratio under the alternative hypothesis.
CV	The coefficient of variation.

allocationRatioPlanned

Allocation ratio for sequence A/B versus sequence B/A. Defaults to 1 for equal randomization.

normalApproximation

The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.

informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

alpha	The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class `designMeanRatioEquiv` object with three components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The overall significance level.
  - `attainedAlpha`: The attained significance level.
  - `kMax`: The number of stages.
  - `information`: The maximum information.
  - `expectedInformationH1`: The expected information under H1.
  - `expectedInformationH0`: The expected information under H0.
  - `numberOfSubjects`: The maximum number of subjects.
  - `expectedNumberOfSubjectsH1`: The expected number of subjects under H1.
  - `expectedNumberOfSubjectsH0`: The expected number of subjects under H0.
  - `meanRatioLower`: The lower equivalence limit of mean ratio.
  - `meanRatioUpper`: The upper equivalence limit of mean ratio.
  - `meanRatio`: The mean ratio under the alternative hypothesis.
  - `CV`: The coefficient of variation.
- `byStageResults`: A data frame containing the following variables:
  - `informationRates`: The information rates.
  - `efficacyBounds`: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - `rejectPerStage`: The probability for efficacy stopping.
  - `cumulativeRejection`: The cumulative probability for efficacy stopping.
  - `cumulativeAlphaSpent`: The cumulative alpha for each of the two one-sided tests.
  - `cumulativeAttainedAlpha`: The cumulative probability for efficacy stopping under H0.
  - `efficacyMeanRatioLower`: The efficacy boundaries on the mean ratio scale for the one-sided null hypothesis on the lower equivalence limit.
  - `efficacyMeanRatioUpper`: The efficacy boundaries on the mean ratio scale for the one-sided null hypothesis on the upper equivalence limit.
  - `efficacyP`: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - `information`: The cumulative information.
  - `numberOfSubjects`: The number of subjects.
- `settings`: A list containing the following input parameters:
  - `typeAlphaSpending`: The type of alpha spending.
  - `parameterAlphaSpending`: The parameter value for alpha spending.
  - `userAlphaSpending`: The user defined alpha spending.
  - `spendingTime`: The error spending time at each analysis.
  - `allocationRatioPlanned`: Allocation ratio for sequence A/B versus sequence B/A.
  - `normalApproximation`: The type of computation of the p-values. If `TRUE`, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
  - `rounding`: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignMeanRatioXOEquiv(
  beta = 0.1, n = NA, meanRatioLower = 0.8, meanRatioUpper = 1.25,
  meanRatio = 1, CV = 0.35,
  kMax = 4, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for t-test
(design2 <- getDesignMeanRatioXOEquiv(
  beta = 0.1, n = NA, meanRatioLower = 0.8, meanRatioUpper = 1.25,
  meanRatio = 1, CV = 0.35,
  normalApproximation = FALSE, alpha = 0.05))
```

---

getDesignOddsRatio   *Group Sequential Design for Two-Sample Odds Ratio*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample odds ratio.

Usage

```
getDesignOddsRatio(
  beta = NA_real_,
  n = NA_real_,
  oddsRatioH0 = 1,
  pi1 = NA_real_,
  pi2 = NA_real_,
  nullVariance = FALSE,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
```

```
    parameterBetaSpending = NA_real_,
    userBetaSpending = NA_real_,
    spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
oddsRatioH0	The odds ratio under the null hypothesis. Defaults to 1.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
nullVariance	Whether to use the variance under the null or the empirical variance under the alternative.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.

informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds   Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending
>   The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming
>   type spending function, "sfP" for Pocock type spending function, "sfKD" for
>   Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spend-
>   ing function, "user" for user defined spending, and "none" for no early futility
>   stopping. Defaults to "none".

parameterBetaSpending
>   The parameter value for the beta spending. Corresponds to rho for "sfKD", and
>   gamma for "sfHSD".

userBetaSpending
>   The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime
>   A vector of length kMax for the error spending time at each analysis. Defaults to
>   missing, in which case, it is the same as informationRates.

Value

An S3 class designOddsRatio object with three components:

- overallResults: A data frame containing the following variables:

  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall sig-
    nificance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - oddsRatioH0: The odds ratio under the null hypothesis.
  - pi1: The assumed probability for the active treatment group.
  - pi2: The assumed probability for the control group.

- byStageResults: A data frame containing the following variables:

  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.

- – `cumulativeAlphaSpent`: The cumulative alpha spent.

- – `efficacyP`: The efficacy boundaries on the p-value scale.

- – `futilityP`: The futility boundaries on the p-value scale.

- – `information`: The cumulative information.

- – `efficacyStopping`: Whether to allow efficacy stopping.

- – `futilityStopping`: Whether to allow futility stopping.

- – `rejectPerStageH0`: The probability for efficacy stopping under H0.

- – `futilityPerStageH0`: The probability for futility stopping under H0.

- – `cumulativeRejectionH0`: The cumulative probability for efficacy stopping under H0.

- – `cumulativeFutilityH0`: The cumulative probability for futility stopping under H0.

- – `efficacyOdddsRatio`: The efficacy boundaries on the odds ratio scale.

- – `futilityOddsRatio`: The futility boundaries on the odds ratio scale.

- – `numberOfSubjects`: The number of subjects.

- `settings`: A list containing the following input parameters:

  - – `typeAlphaSpending`: The type of alpha spending.

  - – `parameterAlphaSpending`: The parameter value for alpha spending.

  - – `userAlphaSpending`: The user defined alpha spending.

  - – `typeBetaSpending`: The type of beta spending.

  - – `parameterBetaSpending`: The parameter value for beta spending.

  - – `userBetaSpending`: The user defined beta spending.

  - – `spendingTime`: The error spending time at each analysis.

  - – `varianceRatio`: The ratio of the variance under H0 to the variance under H1.

  - – `nullVariance`: Whether to use the variance under the null or the empirical variance under the alternative.

  - – `allocationRatioPlanned`: Allocation ratio for the active treatment versus control.

  - – `rounding`: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignOddsRatio(
  beta = 0.1, n = NA, pi1 = 0.5, pi2 = 0.3,
  alpha = 0.05))
```

---

getDesignOddsRatioEquiv

Group Sequential Design for Equivalence in Two-Sample Odds Ratio

---

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in two-sample odds ratio.

Usage

```
getDesignOddsRatioEquiv(
  beta = NA_real_,
  n = NA_real_,
  oddsRatioLower = NA_real_,
  oddsRatioUpper = NA_real_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
oddsRatioLower	The lower equivalence limit of odds ratio.
oddsRatioUpper	The upper equivalence limit of odds ratio.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
allocationRatioPlanned	
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.

informationRates

  The information rates. Fixed prior to the trial. Defaults to `(1:kMax) / kMax` if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending

  The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

  The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

  The user defined alpha spending. Cumulative alpha spent up to each stage.

spendingTime A vector of length `kMax` for the error spending time at each analysis. Defaults to missing, in which case, it is the same as `informationRates`.

Value

An S3 class `designOddsRatioEquiv` object with three components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The significance level for each of the two one-sided tests. Defaults to 0.05.
  - `attainedAlphaH10`: The attained significance level under H10.
  - `attainedAlphaH20`: The attained significance level under H20.
  - `kMax`: The number of stages.
  - `information`: The maximum information.
  - `expectedInformationH1`: The expected information under H1.
  - `expectedInformationH10`: The expected information under H10.
  - `expectedInformationH20`: The expected information under H20.
  - `numberOfSubjects`: The maximum number of subjects.
  - `expectedNumberOfSubjectsH1`: The expected number of subjects under H1.
  - `expectedNumberOfSubjectsH10`: The expected number of subjects under H10.
  - `expectedNumberOfSubjectsH20`: The expected number of subjects under H20.
  - `oddsRatioLower`: The lower equivalence limit of odds ratio.
  - `oddsRatioUpper`: The upper equivalence limit of odds ratio.
  - `pi1`: The assumed probability for the active treatment group.
  - `pi2`: The assumed probability for the control group.
  - `oddsRatio`: The odds ratio.
- `byStageResults`: A data frame containing the following variables:

- – `informationRates`: The information rates.
- – `efficacyBounds`: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
- – `rejectPerStage`: The probability for efficacy stopping.
- – `cumulativeRejection`: The cumulative probability for efficacy stopping.
- – `cumulativeAlphaSpent`: The cumulative alpha for each of the two one-sided tests.
- – `cumulativeAttainedAlphaH10`: The cumulative alpha attained under H10.
- – `cumulativeAttainedAlphaH20`: The cumulative alpha attained under H20.
- – `efficacyOddsRatioLower`: The efficacy boundaries on the odds ratio scale for the one-sided null hypothesis on the lower equivalence limit.
- – `efficacyOddsRatioUpper`: The efficacy boundaries on the odds ratio scale for the one-sided null hypothesis on the upper equivalence limit.
- – `efficacyP`: The efficacy bounds on the p-value scale for each of the two one-sided tests.
- – `information`: The cumulative information.
- – `numberOfSubjects`: The number of subjects.
- `settings`: A list containing the following input parameters:
  - – `typeAlphaSpending`: The type of alpha spending.
  - – `parameterAlphaSpending`: The parameter value for alpha spending.
  - – `userAlphaSpending`: The user defined alpha spending.
  - – `spendingTime`: The error spending time at each analysis.
  - – `allocationRatioPlanned`: Allocation ratio for the active treatment versus control.
  - – `rounding`: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignOddsRatioEquiv(
  beta = 0.2, n = NA, oddsRatioLower = 0.8,
  oddsRatioUpper = 1.25, pi1 = 0.12, pi2 = 0.12,
  kMax = 3, alpha = 0.05, typeAlphaSpending = "sfOF"))
```

---

getDesignOneMean   *Group Sequential Design for One-Sample Mean*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for one-sample mean.

Usage

```
getDesignOneMean(
  beta = NA_real_,
  n = NA_real_,
  meanH0 = 0,
  mean = 0.5,
  stDev = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

`beta`	The type II error.
`n`	The total sample size.
`meanH0`	The mean under the null hypothesis. Defaults to 0.
`mean`	The mean under the alternative hypothesis.
`stDev`	The standard deviation.
`normalApproximation`	
	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
`rounding`	Whether to round up sample size. Defaults to 1 for sample size rounding.
`kMax`	The maximum number of stages.
`informationRates`	
	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
`efficacyStopping`	
	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
`futilityStopping`	
	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues   Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha   The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds   Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designOneMean object with three components:

- overallResults: A data frame containing the following variables:
    - overallReject: The overall rejection probability.
    - alpha: The overall significance level.
    - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
    - kMax: The number of stages.
    - theta: The parameter value.
    - information: The maximum information.
    - expectedInformationH1: The expected information under H1.
    - expectedInformationH0: The expected information under H0.

- **drift**: The drift parameter, equal to `theta*sqrt(information)`.
        - **inflationFactor**: The inflation factor (relative to the fixed design).
        - **numberOfSubjects**: The maximum number of subjects.
        - **expectedNumberOfSubjectsH1**: The expected number of subjects under H1.
        - **expectedNumberOfSubjectsH0**: The expected number of subjects under H0.
        - **meanH0**: The mean under the null hypothesis.
        - **mean**: The mean under the alternative hypothesis.
        - **stDev**: The standard deviation.
- **byStageResults**: A data frame containing the following variables:
        - **informationRates**: The information rates.
        - **efficacyBounds**: The efficacy boundaries on the Z-scale.
        - **futilityBounds**: The futility boundaries on the Z-scale.
        - **rejectPerStage**: The probability for efficacy stopping.
        - **futilityPerStage**: The probability for futility stopping.
        - **cumulativeRejection**: The cumulative probability for efficacy stopping.
        - **cumulativeFutility**: The cumulative probability for futility stopping.
        - **cumulativeAlphaSpent**: The cumulative alpha spent.
        - **efficacyP**: The efficacy boundaries on the p-value scale.
        - **futilityP**: The futility boundaries on the p-value scale.
        - **information**: The cumulative information.
        - **efficacyStopping**: Whether to allow efficacy stopping.
        - **futilityStopping**: Whether to allow futility stopping.
        - **rejectPerStageH0**: The probability for efficacy stopping under H0.
        - **futilityPerStageH0**: The probability for futility stopping under H0.
        - **cumulativeRejectionH0**: The cumulative probability for efficacy stopping under H0.
        - **cumulativeFutilityH0**: The cumulative probability for futility stopping under H0.
        - **efficacyMean**: The efficacy boundaries on the mean scale.
        - **futilityMean**: The futility boundaries on the mean scale.
        - **numberOfSubjects**: The number of subjects.
- **settings**: A list containing the following input parameters:
        - **typeAlphaSpending**: The type of alpha spending.
        - **parameterAlphaSpending**: The parameter value for alpha spending.
        - **userAlphaSpending**: The user defined alpha spending.
        - **typeBetaSpending**: The type of beta spending.
        - **parameterBetaSpending**: The parameter value for beta spending.
        - **userBetaSpending**: The user defined beta spending.
        - **spendingTime**: The error spending time at each analysis.
        - **normalApproximation**: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
        - **rounding**: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignOneMean(
  beta = 0.1, n = NA, meanH0 = 7, mean = 6, stDev = 2.5,
  kMax = 5, alpha = 0.025, typeAlphaSpending = "sfOF",
  typeBetaSpending = "sfP"))

# Example 2: sample size calculation for one-sample t-test
(design2 <- getDesignOneMean(
  beta = 0.1, n = NA, meanH0 = 7, mean = 6, stDev = 2.5,
  normalApproximation = FALSE, alpha = 0.025))
```

---

getDesignOneMultinom   *Power and Sample Size for One-Sample Multinomial Response*

Description

Obtains the power given sample size or obtains the sample size given power for one-sample multinomial response.

Usage

```
getDesignOneMultinom(
  beta = NA_real_,
  n = NA_real_,
  ncats = NA_integer_,
  piH0 = NA_real_,
  pi = NA_real_,
  rounding = TRUE,
  alpha = 0.05
)
```

Arguments

beta	The type II error.
n	The total sample size.
ncats	The number of categories of the multinomial response.
piH0	The prevalence of each category under the null hypothesis. Only need to provide the values for the first ncats-1 categories.
pi	The prevalence of each category. Only need to provide the values for the first ncats-1 categories.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.

Value

An S3 class designOneMultinom object with the following components:

- power: The power to reject the null hypothesis.
- alpha: The two-sided significance level.
- n: The maximum number of subjects.
- ncats: The number of categories of the multinomial response.
- piH0: The prevalence of each category under the null hypothesis.
- pi: The prevalence of each category.
- effectsize: The effect size for the chi-square test.
- rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignOneMultinom(
  beta = 0.1, ncats = 3, piH0 = c(0.25, 0.25),
  pi = c(0.3, 0.4), alpha = 0.05))
```

---

getDesignOneProportion

Group Sequential Design for One-Sample Proportion

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for one-sample proportion.

Usage

```
getDesignOneProportion(
  beta = NA_real_,
  n = NA_real_,
  piH0 = 0.1,
  pi = 0.2,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
```

```
    criticalValues = NA_real_,
    alpha = 0.025,
    typeAlphaSpending = "sfOF",
    parameterAlphaSpending = NA_real_,
    userAlphaSpending = NA_real_,
    futilityBounds = NA_real_,
    typeBetaSpending = "none",
    parameterBetaSpending = NA_real_,
    userBetaSpending = NA_real_,
    spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
piH0	The response probability under the null hypothesis.
pi	The response probability under the alternative hypothesis.
normalApproximation	
	The type of computation of the p-values. If TRUE, the normal approximation will be used, otherwise the calculations are performed with the binomial distribution. The exact calculation using the binomial distribution is only implemented for the fixed design.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	
	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
efficacyStopping	
	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	
	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	
	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	
	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending
: The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds
: Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending
: The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending
: The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending
: The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime
: A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designOneProportion object with three components:

- overallResults: A data frame containing the following variables:
    - overallReject: The overall rejection probability.
    - alpha: The overall significance level.
    - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping as well as for the binomial exact test in a fixed design.
    - kMax: The number of stages.
    - theta: The parameter value.
    - information: The maximum information.
    - expectedInformationH1: The expected information under H1.
    - expectedInformationH0: The expected information under H0.
    - drift: The drift parameter, equal to theta*sqrt(information).
    - inflationFactor: The inflation factor (relative to the fixed design).
    - numberOfSubjects: The maximum number of subjects.
    - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
    - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
    - piH0: The response probability under the null hypothesis.
    - pi: The response probability under the alternative hypothesis.
- byStageResults: A data frame containing the following variables:
    - informationRates: The information rates.
    - efficacyBounds: The efficacy boundaries on the Z-scale.
    - futilityBounds: The futility boundaries on the Z-scale.

  – rejectPerStage: The probability for efficacy stopping.
  – futilityPerStage: The probability for futility stopping.
  – cumulativeRejection: The cumulative probability for efficacy stopping.
  – cumulativeFutility: The cumulative probability for futility stopping.
  – cumulativeAlphaSpent: The cumulative alpha spent.
  – efficacyP: The efficacy boundaries on the p-value scale.
  – futilityP: The futility boundaries on the p-value scale.
  – information: The cumulative information.
  – efficacyStopping: Whether to allow efficacy stopping.
  – futilityStopping: Whether to allow futility stopping.
  – rejectPerStageH0: The probability for efficacy stopping under H0.
  – futilityPerStageH0: The probability for futility stopping under H0.
  – cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  – cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  – efficacyResponses: The efficacy boundaries on the number of responses scale.
  – futilityResponses: The futility boundaries on the number of responses scale.
  – numberOfSubjects: The number of subjects.
• settings: A list containing the following input parameters:
  – typeAlphaSpending: The type of alpha spending.
  – parameterAlphaSpending: The parameter value for alpha spending.
  – userAlphaSpending: The user defined alpha spending.
  – typeBetaSpending: The type of beta spending.
  – parameterBetaSpending: The parameter value for beta spending.
  – userBetaSpending: The user defined beta spending.
  – spendingTime: The error spending time at each analysis.
  – normalApproximation: The type of computation of the p-values. If TRUE, the variance
    is assumed to be known, otherwise the calculations are performed with the binomial
    distribution.
  – rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignOneProportion(
  beta = 0.2, n = NA, piH0 = 0.15, pi = 0.25,
  kMax = 3, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for one-sample binomial exact test
(design2 <- getDesignOneProportion(
  beta = 0.2, n = NA, piH0 = 0.15, pi = 0.25,
  normalApproximation = FALSE, alpha = 0.05))
```

---

getDesignOneRateExact   *Power and Sample Size for One-Sample Poisson Rate Exact Test*

Description

Obtains the power given sample size or obtains the sample size given power for one-sample Poisson rate.

Usage

```
getDesignOneRateExact(
  beta = NA_real_,
  n = NA_real_,
  lambdaH0 = NA_real_,
  lambda = NA_real_,
  D = 1,
  alpha = 0.025
)
```

Arguments

beta	The type II error.
n	The total sample size.
lambdaH0	The Poisson rate under the null hypothesis.
lambda	The Poisson rate under the alternative hypothesis.
D	The average exposure per subject.
alpha	The one-sided significance level. Defaults to 0.025.

Value

A data frame containing the following variables:

- alpha: The specified significance level.
- attainedAlpha: The attained type I error of the exact test.
- power: The actual power of the exact test.
- n: The sample size.
- lambdaH0: The Poisson rate under the null hypothesis.
- lambda: The Poisson rate under the alternative hypothesis.
- D: The average exposure per subject.
- r: The critical value of the number of events for rejecting the null hypothesis. Reject H0 if Y >= r for upper-tailed test, and reject H0 if Y <= r for lower-tailed test.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: power calculation
(design1 <- getDesignOneRateExact(
  n = 525, lambdaH0 = 0.049, lambda = 0.012,
  D = 0.5, alpha = 0.025))

# Example 2: sample size calculation
(design2 <- getDesignOneRateExact(
  beta = 0.2, lambdaH0 = 0.2, lambda = 0.3,
  D = 1, alpha = 0.05))
```

---

getDesignOneSlope   *Group Sequential Design for One-Sample Slope*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential
design for one-sample slope.

Usage

```
getDesignOneSlope(
  beta = NA_real_,
  n = NA_real_,
  slopeH0 = 0,
  slope = 0.5,
  stDev = 1,
  stDevCovariate = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
slopeH0	The slope under the null hypothesis. Defaults to 0.
slope	The slope under the alternative hypothesis.
stDev	The standard deviation of the residual.
stDevCovariate	The standard deviation of the covariate.

normalApproximation

The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.

informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

>   The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

>   The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designOneSlope object with three components:

- overallResults: A data frame containing the following variables:
    - overallReject: The overall rejection probability.
    - alpha: The overall significance level.
    - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
    - kMax: The number of stages.
    - theta: The parameter value.
    - information: The maximum information.
    - expectedInformationH1: The expected information under H1.
    - expectedInformationH0: The expected information under H0.
    - drift: The drift parameter, equal to theta*sqrt(information).
    - inflationFactor: The inflation factor (relative to the fixed design).
    - numberOfSubjects: The maximum number of subjects.
    - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
    - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
    - slopeH0: The slope under the null hypothesis.
    - slope: The slope under the alternative hypothesis.
    - stDev: The standard deviation of the residual.
    - stDevCovariate: The standard deviation of the covariate.
- byStageResults: A data frame containing the following variables:
    - informationRates: The information rates.
    - efficacyBounds: The efficacy boundaries on the Z-scale.
    - futilityBounds: The futility boundaries on the Z-scale.
    - rejectPerStage: The probability for efficacy stopping.
    - futilityPerStage: The probability for futility stopping.
    - cumulativeRejection: The cumulative probability for efficacy stopping.
    - cumulativeFutility: The cumulative probability for futility stopping.
    - cumulativeAlphaSpent: The cumulative alpha spent.
    - efficacyP: The efficacy boundaries on the p-value scale.
    - futilityP: The futility boundaries on the p-value scale.
    - information: The cumulative information.
    - efficacyStopping: Whether to allow efficacy stopping.

- **–** futilityStopping: Whether to allow futility stopping.
- **–** rejectPerStageH0: The probability for efficacy stopping under H0.
- **–** futilityPerStageH0: The probability for futility stopping under H0.
- **–** cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
- **–** cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
- **–** efficacySlope: The efficacy boundaries on the slope scale.
- **–** futilitySlope: The futility boundaries on the slope scale.
- **–** numberOfSubjects: The number of subjects.

- settings: A list containing the following input parameters:

  - **–** typeAlphaSpending: The type of alpha spending.
  - **–** parameterAlphaSpending: The parameter value for alpha spending.
  - **–** userAlphaSpending: The user defined alpha spending.
  - **–** typeBetaSpending: The type of beta spending.
  - **–** parameterBetaSpending: The parameter value for beta spending.
  - **–** userBetaSpending: The user defined beta spending.
  - **–** spendingTime: The error spending time at each analysis.
  - **–** normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
  - **–** rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignOneSlope(
  beta = 0.1, n = NA, slope = 0.5,
  stDev = 15, stDevCovariate = 9,
  normalApproximation = FALSE,
  alpha = 0.025))
```

---

getDesignOrderedBinom   *Power and Sample Size for Cochran-Armitage Trend Test for Ordered Multi-Sample Binomial Response*

Description

Obtains the power given sample size or obtains the sample size given power for the Cochran-Armitage trend test for ordered multi-sample binomial response.

Usage

```
getDesignOrderedBinom(
  beta = NA_real_,
  n = NA_real_,
  ngroups = NA_integer_,
  pi = NA_real_,
  w = NA_real_,
  allocationRatioPlanned = NA_integer_,
  rounding = TRUE,
  alpha = 0.05
)
```

Arguments

beta	The type II error.
n	The total sample size.
ngroups	The number of treatment groups.
pi	The response probabilities for the treatment groups.
w	The scores assigned to the treatment groups. This should reflect the ordinal nature of the treatment groups, e.g. dose levels. Defaults to equally spaced scores.
allocationRatioPlanned	
	Allocation ratio for the treatment groups.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.

Value

An S3 class designOrderedBinom object with the following components:

- power: The power to reject the null hypothesis.
- alpha: The two-sided significance level.
- n: The maximum number of subjects.
- ngroups: The number of treatment groups.
- pi: The response probabilities for the treatment groups.
- w: The scores assigned to the treatment groups.
- trendstat: The Cochran-Armitage trend test statistic.
- allocationRatioPlanned: Allocation ratio for the treatment groups.
- rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignOrderedBinom(
  beta = 0.1, ngroups = 3, pi = c(0.1, 0.25, 0.5), alpha = 0.05))
```

---

getDesignPairedMeanDiff

Group Sequential Design for Paired Mean Difference

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for paired mean difference.

Usage

```
getDesignPairedMeanDiff(
  beta = NA_real_,
  n = NA_real_,
  pairedDiffH0 = 0,
  pairedDiff = 0.5,
  stDev = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
pairedDiffH0	The paired difference under the null hypothesis. Defaults to 0.
pairedDiff	The paired difference under the alternative hypothesis.

stDev   The standard deviation for paired difference.

normalApproximation

                      The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

rounding   Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax   The maximum number of stages.

informationRates

                      The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

                      Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

                      Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues   Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha   The significance level. Defaults to 0.025.

typeAlphaSpending

                      The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

                      The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

                      The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds   Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

                      The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

                      The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

                      The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designPairedMeanDiff object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - pairedDiffH0: The paired difference under the null hypothesis.
  - pairedDiff: The paired difference under the alternative hypothesis.
  - stDev: The standard deviation for paired difference.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacyPairedDiff: The efficacy boundaries on the paired difference scale.
  - futilityPairedDiff: The futility boundaries on the paired difference scale.
  - numberOfSubjects: The number of subjects.

- settings: A list containing the following input parameters:
    - typeAlphaSpending: The type of alpha spending.
    - parameterAlphaSpending: The parameter value for alpha spending.
    - userAlphaSpending: The user defined alpha spending.
    - typeBetaSpending: The type of beta spending.
    - parameterBetaSpending: The parameter value for beta spending.
    - userBetaSpending: The user defined beta spending.
    - spendingTime: The error spending time at each analysis.
    - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
    - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignPairedMeanDiff(
  beta = 0.1, n = NA, pairedDiffH0 = 0, pairedDiff = -2, stDev = 5,
  kMax = 5, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for one-sample t-test
(design2 <- getDesignPairedMeanDiff(
  beta = 0.1, n = NA, pairedDiffH0 = 0, pairedDiff = -2, stDev = 5,
  normalApproximation = FALSE, alpha = 0.025))
```

---

getDesignPairedMeanDiffEquiv

Group Sequential Design for Equivalence in Paired Mean Difference

---

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in paired mean difference.

Usage

```
getDesignPairedMeanDiffEquiv(
  beta = NA_real_,
  n = NA_real_,
  pairedDiffLower = NA_real_,
  pairedDiffUpper = NA_real_,
  pairedDiff = 0,
  stDev = 1,
```

```
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
pairedDiffLower	
	The lower equivalence limit of paired difference.
pairedDiffUpper	
	The upper equivalence limit of paired difference.
pairedDiff	The paired difference under the alternative hypothesis.
stDev	The standard deviation for paired difference.
normalApproximation	
	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	
	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
alpha	The significance level for each of the two one-sided tests. Defaults to 0.05.
typeAlphaSpending	
	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	
	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	
	The user defined alpha spending. Cumulative alpha spent up to each stage.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designPairedMeanDiffEquiv object with three components:

- overallResults: A data frame containing the following variables:
    - overallReject: The overall rejection probability.
    - alpha: The significance level for each of the two one-sided tests. Defaults to 0.05.
    - attainedAlpha: The attained significance level under H0.
    - kMax: The number of stages.
    - information: The maximum information.
    - expectedInformationH1: The expected information under H1.
    - expectedInformationH0: The expected information under H0.
    - numberOfSubjects: The maximum number of subjects.
    - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
    - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
    - pairedDiffLower: The lower equivalence limit of paired difference.
    - pairedDiffUpper: The upper equivalence limit of paired difference.
    - pairedDiff: The paired difference under the alternative hypothesis.
    - stDev: The standard deviation for paired difference.
- byStageResults: A data frame containing the following variables:
    - informationRates: The information rates.
    - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
    - rejectPerStage: The probability for efficacy stopping.
    - cumulativeRejection: The cumulative probability for efficacy stopping.
    - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
    - cumulativeAttainedAlpha: The cumulative probability for efficacy stopping under H0.
    - efficacyPairedDiffLower: The efficacy boundaries on the paired difference scale for the one-sided null hypothesis on the lower equivalence limit.
    - efficacyPairedDiffUpper: The efficacy boundaries on the paired difference scale for the one-sided null hypothesis on the upper equivalence limit.
    - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
    - information: The cumulative information.
    - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
    - typeAlphaSpending: The type of alpha spending.
    - parameterAlphaSpending: The parameter value for alpha spending.
    - userAlphaSpending: The user defined alpha spending.
    - spendingTime: The error spending time at each analysis.
    - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
    - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignPairedMeanDiffEquiv(
  beta = 0.1, n = NA, pairedDiffLower = -1.3, pairedDiffUpper = 1.3,
  pairedDiff = 0, stDev = 2.2,
  kMax = 4, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for t-test
(design2 <- getDesignPairedMeanDiffEquiv(
  beta = 0.1, n = NA, pairedDiffLower = -1.3, pairedDiffUpper = 1.3,
  pairedDiff = 0, stDev = 2.2,
  normalApproximation = FALSE, alpha = 0.05))
```

---

getDesignPairedMeanRatio

Group Sequential Design for Paired Mean Ratio

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for paired mean ratio.

Usage

```
getDesignPairedMeanRatio(
  beta = NA_real_,
  n = NA_real_,
  pairedRatioH0 = 1,
  pairedRatio = 1.2,
  CV = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
```

```
    parameterBetaSpending = NA_real_,
    userBetaSpending = NA_real_,
    spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
pairedRatioH0	The paired ratio under the null hypothesis.
pairedRatio	The paired ratio under the alternative hypothesis.
CV	The coefficient of variation for paired ratio.
normalApproximation	
	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	
	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
efficacyStopping	
	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	
	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	
	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	
	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	
	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

>The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

>The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

>The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designPairedMeanRatio object with three components:

- overallResults: A data frame containing the following variables:
    - overallReject: The overall rejection probability.
    - alpha: The overall significance level.
    - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
    - kMax: The number of stages.
    - theta: The parameter value.
    - information: The maximum information.
    - expectedInformationH1: The expected information under H1.
    - expectedInformationH0: The expected information under H0.
    - drift: The drift parameter, equal to theta*sqrt(information).
    - inflationFactor: The inflation factor (relative to the fixed design).
    - numberOfSubjects: The maximum number of subjects.
    - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
    - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
    - pairedRatioH0: The paired ratio under the null hypothesis.
    - pairedRatio: The paired ratio under the alternative hypothesis.
    - CV: The coefficient of variation for paired ratio.
- byStageResults: A data frame containing the following variables:
    - informationRates: The information rates.
    - efficacyBounds: The efficacy boundaries on the Z-scale.
    - futilityBounds: The futility boundaries on the Z-scale.
    - rejectPerStage: The probability for efficacy stopping.
    - futilityPerStage: The probability for futility stopping.
    - cumulativeRejection: The cumulative probability for efficacy stopping.
    - cumulativeFutility: The cumulative probability for futility stopping.

- **–** cumulativeAlphaSpent: The cumulative alpha spent.
- **–** efficacyP: The efficacy boundaries on the p-value scale.
- **–** futilityP: The futility boundaries on the p-value scale.
- **–** information: The cumulative information.
- **–** efficacyStopping: Whether to allow efficacy stopping.
- **–** futilityStopping: Whether to allow futility stopping.
- **–** rejectPerStageH0: The probability for efficacy stopping under H0.
- **–** futilityPerStageH0: The probability for futility stopping under H0.
- **–** cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
- **–** cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
- **–** numberOfSubjects: The number of subjects.
- **–** efficacyPairedRatio: The efficacy boundaries on the paired ratio scale.
- **–** futilityPairedRatio: The futility boundaries on the paired ratio scale.
- **•** settings: A list containing the following input parameters:
  - **–** typeAlphaSpending: The type of alpha spending.
  - **–** parameterAlphaSpending: The parameter value for alpha spending.
  - **–** userAlphaSpending: The user defined alpha spending.
  - **–** typeBetaSpending: The type of beta spending.
  - **–** parameterBetaSpending: The parameter value for beta spending.
  - **–** userBetaSpending: The user defined beta spending.
  - **–** spendingTime: The error spending time at each analysis.
  - **–** normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
  - **–** rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignPairedMeanRatio(
  beta = 0.1, n = NA, pairedRatio = 1.2, CV = 0.35,
  kMax = 5, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for one-sample t-test
(design2 <- getDesignPairedMeanRatio(
  beta = 0.1, n = NA, pairedRatio = 1.2, CV = 0.35,
  normalApproximation = FALSE, alpha = 0.05))
```

---

getDesignPairedMeanRatioEquiv

Group Sequential Design for Equivalence in Paired Mean Ratio

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in paired mean ratio.

Usage

```
getDesignPairedMeanRatioEquiv(
  beta = NA_real_,
  n = NA_real_,
  pairedRatioLower = NA_real_,
  pairedRatioUpper = NA_real_,
  pairedRatio = 1,
  CV = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
pairedRatioLower	
	The lower equivalence limit of paired ratio.
pairedRatioUpper	
	The upper equivalence limit of paired ratio.
pairedRatio	The paired ratio under the alternative hypothesis.
CV	The coefficient of variation for paired ratio.
normalApproximation	
	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.

informationRates

> The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

alpha   The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending

> The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

> The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

> The user defined alpha spending. Cumulative alpha spent up to each stage.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designPairedMeanRatioEquiv object with three components:

- overallResults: A data frame containing the following variables:
    - overallReject: The overall rejection probability.
    - alpha: The significance level for each of the two one-sided tests. Defaults to 0.05.
    - attainedAlpha: The attained significance level under H0.
    - kMax: The number of stages.
    - information: The maximum information.
    - expectedInformationH1: The expected information under H1.
    - expectedInformationH0: The expected information under H0.
    - numberOfSubjects: The maximum number of subjects.
    - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
    - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
    - pairedRatioLower: The lower equivalence limit of paired ratio.
    - pairedRatioUpper: The upper equivalence limit of paired ratio.
    - pairedRatio: The paired ratio under the alternative hypothesis.
    - CV: The coefficient of variation for paired ratios.
- byStageResults: A data frame containing the following variables:
    - informationRates: The information rates.
    - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
    - rejectPerStage: The probability for efficacy stopping.
    - cumulativeRejection: The cumulative probability for efficacy stopping.

- – cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
    - – cumulativeAttainedAlpha: The cumulative alpha attained under H0.
    - – efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
    - – information: The cumulative information.
    - – numberOfSubjects: The number of subjects.
    - – efficacyPairedRatioLower: The efficacy boundaries on the paired ratio scale for the one-sided null hypothesis on the lower equivalence limit.
    - – efficacyPairedRatioUpper: The efficacy boundaries on the paired ratio scale for the one-sided null hypothesis on the upper equivalence limit.
- settings: A list containing the following input parameters:
    - – typeAlphaSpending: The type of alpha spending.
    - – parameterAlphaSpending: The parameter value for alpha spending.
    - – userAlphaSpending: The user defined alpha spending.
    - – spendingTime: The error spending time at each analysis.
    - – normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
    - – rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignPairedMeanRatioEquiv(
  beta = 0.1, n = NA, pairedRatioLower = 0.8, pairedRatioUpper = 1.25,
  pairedRatio = 1, CV = 0.35,
  kMax = 4, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for t-test
(design2 <- getDesignPairedMeanRatioEquiv(
  beta = 0.1, n = NA, pairedRatioLower = 0.8, pairedRatioUpper = 1.25,
  pairedRatio = 1, CV = 0.35,
  normalApproximation = FALSE, alpha = 0.05))
```

---

getDesignPairedPropMcNemar

Group Sequential Design for McNemar's Test for Paired Proportions

---

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for McNemar's test for paired proportions.

Usage

```
getDesignPairedPropMcNemar(
  beta = NA_real_,
  n = NA_real_,
  pDiscordant = NA_real_,
  riskDiff = NA_real_,
  nullVariance = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
pDiscordant	The proportion of discordant pairs (xi = pi01 + pi10).
riskDiff	The risk difference between the active and control treatments (delta = pi_t - pi_c = pi01 - pi10)
nullVariance	Whether to use the variance under the null or the variance under the alternative.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	
	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
efficacyStopping	
	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	
	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.

typeAlphaSpending

> The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

> The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

> The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds

> Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

> The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

> The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

> The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime

> A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designPairedPropMcNemar object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.

- **–** expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - **–** expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - **–** pDiscordant: The proportion of discordant pairs (xi = pi01 + pi10).
  - **–** riskDiff: The risk difference between the active and control treatments (delta = pi_t - pi_c = pi01 - pi10)
- byStageResults: A data frame containing the following variables:
  - **–** informationRates: The information rates.
  - **–** efficacyBounds: The efficacy boundaries on the Z-scale.
  - **–** futilityBounds: The futility boundaries on the Z-scale.
  - **–** rejectPerStage: The probability for efficacy stopping.
  - **–** futilityPerStage: The probability for futility stopping.
  - **–** cumulativeRejection: The cumulative probability for efficacy stopping.
  - **–** cumulativeFutility: The cumulative probability for futility stopping.
  - **–** cumulativeAlphaSpent: The cumulative alpha spent.
  - **–** efficacyP: The efficacy boundaries on the p-value scale.
  - **–** futilityP: The futility boundaries on the p-value scale.
  - **–** information: The cumulative information.
  - **–** efficacyStopping: Whether to allow efficacy stopping.
  - **–** futilityStopping: Whether to allow futility stopping.
  - **–** rejectPerStageH0: The probability for efficacy stopping under H0.
  - **–** futilityPerStageH0: The probability for futility stopping under H0.
  - **–** cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - **–** cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - **–** efficacyRiskDiff: The efficacy boundaries on the risk difference scale.
  - **–** futilityRiskDiff: The futility boundaries on the risk difference scale.
  - **–** numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - **–** typeAlphaSpending: The type of alpha spending.
  - **–** parameterAlphaSpending: The parameter value for alpha spending.
  - **–** userAlphaSpending: The user defined alpha spending.
  - **–** typeBetaSpending: The type of beta spending.
  - **–** parameterBetaSpending: The parameter value for beta spending.
  - **–** userBetaSpending: The user defined beta spending.
  - **–** spendingTime: The error spending time at each analysis.
  - **–** varianceRatio: The ratio of the variance under H0 to the variance under H1.
  - **–** rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: fixed design
(design1 <- getDesignPairedPropMcNemar(
  beta = 0.1, n = NA, pDiscordant = 0.16, riskDiff = 0.1,
  alpha = 0.025))

# Example 2: group sequential design
(design2 <- getDesignPairedPropMcNemar(
  beta = 0.1, n = NA, pDiscordant = 0.16, riskDiff = 0.1,
  alpha = 0.025, kMax = 3, typeAlphaSpending = "sfOF"))
```

---

getDesignRepeatedANOVA

Power and Sample Size for Repeated-Measures ANOVA

Description

Obtains the power and sample size for one-way repeated measures analysis of variance. Each subject takes all treatments in the longitudinal study.

Usage

```
getDesignRepeatedANOVA(
  beta = NA_real_,
  n = NA_real_,
  ngroups = 2,
  means = NA_real_,
  stDev = 1,
  corr = 0,
  rounding = TRUE,
  alpha = 0.05
)
```

Arguments

beta	The type II error.
n	The total sample size.
ngroups	The number of treatment groups.
means	The treatment group means.
stDev	The total standard deviation.
corr	The correlation among the repeated measures.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.

Details

Let y_{ij} denote the measurement under treatment condition $j(j = 1, \ldots, k)$ for subject $i(i = 1, \ldots, n)$. Then

$$y_{ij} = \alpha + \beta_j + b_i + e_{ij},$$

where b_i denotes the subject random effect, $b_i \sim N(0, \sigma_b^2)$, and $e_{ij} \sim N(0, \sigma_e^2)$ denotes the within-subject residual. If we set $\beta_k = 0$, then α is the mean of the last treatment (control), and β_j is the difference in means between the jth treatment and the control for $j = 1, \ldots, k - 1$.

The repeated measures have a compound symmetry covariance structure. Let $\sigma^2 = \sigma_b^2 + \sigma_e^2$, and $\rho = \frac{\sigma_b^2}{\sigma_b^2 + \sigma_e^2}$. Then $Var(y_i) = \sigma^2 \{(1 - \rho)I_k + \rho 1_k 1_k^T\}$. Let X_i denote the design matrix for subject i. Let $\theta = (\alpha, \beta_1, \ldots, \beta_{k-1})^T$. It follows that

$$Var(\hat{\theta}) = \left(\sum_{i=1}^{n} X_i^T V_i^{-1} X_i \right)^{-1}.$$

It can be shown that

$$Var(\hat{\beta}) = \frac{\sigma^2 (1 - \rho)}{n} (I_{k-1} + 1_{k-1} 1_{k-1}^T).$$

It follows that $\hat{\beta}^T \hat{V}_{\hat{\beta}}^{-1} \hat{\beta} \sim F_{k-1,(n-1)(k-1),\lambda}$, where the noncentrality parameter for the F distribution is

$$\lambda = \beta^T V_{\hat{\beta}}^{-1} \beta = \frac{n \sum_{j=1}^{k} (\mu_j - \bar{\mu})^2}{\sigma^2 (1 - \rho)}.$$

Value

An S3 class `designRepeatedANOVA` object with the following components:

- `power`: The power to reject the null hypothesis that there is no difference among the treatment groups.
- `alpha`: The two-sided significance level.
- `n`: The number of subjects.
- `ngroups`: The number of treatment groups.
- `means`: The treatment group means.
- `stDev`: The total standard deviation.
- `corr`: The correlation among the repeated measures.
- `effectsize`: The effect size.
- `rounding`: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignRepeatedANOVA(
  beta = 0.1, ngroups = 4, means = c(1.5, 2.5, 2, 0),
  stDev = 5, corr = 0.2, alpha = 0.05))
```

getDesignRepeatedANOVAContrast

Power and Sample Size for One-Way Repeated Measures ANOVA Contrast

Description

Obtains the power and sample size for a single contrast in one-way repeated measures analysis of variance.

Usage

```
getDesignRepeatedANOVAContrast(
  beta = NA_real_,
  n = NA_real_,
  ngroups = 2,
  means = NA_real_,
  stDev = 1,
  corr = 0,
  contrast = NA_real_,
  meanContrastH0 = 0,
  rounding = TRUE,
  alpha = 0.025
)
```

Arguments

beta	The type II error.
n	The total sample size.
ngroups	The number of treatment groups.
means	The treatment group means.
stDev	The total standard deviation.
corr	The correlation among the repeated measures.
contrast	The coefficients for the single contrast.
meanContrastH0	The mean of the contrast under the null hypothesis.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The one-sided significance level. Defaults to 0.025.

Value

An S3 class designRepeatedANOVAContrast object with the following components:

- power: The power to reject the null hypothesis for the treatment contrast.
- alpha: The one-sided significance level.

- n: The number of subjects.
- ngroups: The number of treatment groups.
- means: The treatment group means.
- stDev: The total standard deviation.
- corr: The correlation among the repeated measures.
- contrast: The coefficients for the single contrast.
- meanContrastH0: The mean of the contrast under the null hypothesis.
- meanContrast: The mean of the contrast under the alternative hypothesis.
- effectsize: The effect size.
- rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignRepeatedANOVAContrast(
  beta = 0.1, ngroups = 4, means = c(1.5, 2.5, 2, 0),
  stDev = 5, corr = 0.2, contrast = c(1, 1, 1, -3)/3,
  alpha = 0.025))
```

---

getDesignRiskDiff　　　　　　*Group Sequential Design for Two-Sample Risk Difference*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample risk difference.

Usage

```
getDesignRiskDiff(
  beta = NA_real_,
  n = NA_real_,
  riskDiffH0 = 0,
  pi1 = NA_real_,
  pi2 = NA_real_,
  nullVariance = TRUE,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
```

```
        futilityStopping = NA_integer_,
        criticalValues = NA_real_,
        alpha = 0.025,
        typeAlphaSpending = "sfOF",
        parameterAlphaSpending = NA_real_,
        userAlphaSpending = NA_real_,
        futilityBounds = NA_real_,
        typeBetaSpending = "none",
        parameterBetaSpending = NA_real_,
        userBetaSpending = NA_real_,
        spendingTime = NA_real_
    )
```

Arguments

beta	The type II error.
n	The total sample size.
riskDiffH0	The risk difference under the null hypothesis. Defaults to 0.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
nullVariance	Whether to use the variance under the null or the empirical variance under the alternative.
allocationRatioPlanned	
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	
	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
efficacyStopping	
	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	
	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	
	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

> The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

> The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds   Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

> The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

> The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

> The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designRiskDiff object with three components:

- overallResults: A data frame containing the following variables:
    - overallReject: The overall rejection probability.
    - alpha: The overall significance level.
    - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
    - kMax: The number of stages.
    - theta: The parameter value.
    - information: The maximum information.
    - expectedInformationH1: The expected information under H1.
    - expectedInformationH0: The expected information under H0.
    - drift: The drift parameter, equal to theta*sqrt(information).
    - inflationFactor: The inflation factor (relative to the fixed design).
    - numberOfSubjects: The maximum number of subjects.
    - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
    - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
    - riskDiffH0: The risk difference under the null hypothesis.
    - pi1: The assumed probability for the active treatment group.
    - pi2: The assumed probability for the control group.
- byStageResults: A data frame containing the following variables:

- – informationRates: The information rates.
- – efficacyBounds: The efficacy boundaries on the Z-scale.
- – futilityBounds: The futility boundaries on the Z-scale.
- – rejectPerStage: The probability for efficacy stopping.
- – futilityPerStage: The probability for futility stopping.
- – cumulativeRejection: The cumulative probability for efficacy stopping.
- – cumulativeFutility: The cumulative probability for futility stopping.
- – cumulativeAlphaSpent: The cumulative alpha spent.
- – efficacyRiskDiff: The efficacy boundaries on the risk difference scale.
- – futilityRiskDiff: The futility boundaries on the risk difference scale.
- – efficacyP: The efficacy boundaries on the p-value scale.
- – futilityP: The futility boundaries on the p-value scale.
- – information: The cumulative information.
- – efficacyStopping: Whether to allow efficacy stopping.
- – futilityStopping: Whether to allow futility stopping.
- – rejectPerStageH0: The probability for efficacy stopping under H0.
- – futilityPerStageH0: The probability for futility stopping under H0.
- – cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
- – cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
- – numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - – typeAlphaSpending: The type of alpha spending.
  - – parameterAlphaSpending: The parameter value for alpha spending.
  - – userAlphaSpending: The user defined alpha spending.
  - – typeBetaSpending: The type of beta spending.
  - – parameterBetaSpending: The parameter value for beta spending.
  - – userBetaSpending: The user defined beta spending.
  - – spendingTime: The error spending time at each analysis.
  - – varianceRatio: The ratio of the variance under H0 to the variance under H1.
  - – nullVariance: Whether to use the variance under the null or the empirical variance under the alternative.
  - – allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - – rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignRiskDiff(
  beta = 0.2, n = NA, pi1 = 0.1, pi2 = 0.15,
  kMax = 3, alpha = 0.025, typeAlphaSpending = "sfOF",
  nullVariance = 0))
```

---

getDesignRiskDiffEquiv

> *Group Sequential Design for Equivalence in Two-Sample Risk Difference*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in two-sample risk difference.

Usage

```
getDesignRiskDiffEquiv(
  beta = NA_real_,
  n = NA_real_,
  riskDiffLower = NA_real_,
  riskDiffUpper = NA_real_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
riskDiffLower	The lower equivalence limit of risk difference.
riskDiffUpper	The upper equivalence limit of risk difference.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
allocationRatioPlanned	
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.

informationRates

    The information rates. Fixed prior to the trial. Defaults to `(1:kMax) / kMax` if left unspecified.

criticalValues   Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha   The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending

    The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

    The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

    The user defined alpha spending. Cumulative alpha spent up to each stage.

spendingTime   A vector of length `kMax` for the error spending time at each analysis. Defaults to missing, in which case, it is the same as `informationRates`.

Value

An S3 class designRiskDiffEquiv object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The significance level for each of the two one-sided tests. Defaults to 0.05.
  - attainedAlphaH10: The attained significance level under H10.
  - attainedAlphaH20: The attained significance level under H20.
  - kMax: The number of stages.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH10: The expected information under H10.
  - expectedInformationH20: The expected information under H20.
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH10: The expected number of subjects under H10.
  - expectedNumberOfSubjectsH20: The expected number of subjects under H20.
  - riskDiffLower: The lower equivalence limit of risk difference.
  - riskDiffUpper: The upper equivalence limit of risk difference.
  - pi1: The assumed probability for the active treatment group.
  - pi2: The assumed probability for the control group.
  - riskDiff: The risk difference.
- byStageResults: A data frame containing the following variables:

- informationRates: The information rates.
- efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
- rejectPerStage: The probability for efficacy stopping.
- cumulativeRejection: The cumulative probability for efficacy stopping.
- cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
- cumulativeAttainedAlphaH10: The cumulative alpha attained under H10.
- cumulativeAttainedAlphaH20: The cumulative alpha attained under H20.
- efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
- information: The cumulative information.
- efficacyRiskDiffLower: The efficacy boundaries on the risk difference scale for the one-sided null hypothesis on the lower equivalence limit.
- efficacyRiskDiffUpper: The efficacy boundaries on the risk difference scale for the one-sided null hypothesis on the upper equivalence limit.
- numberOfSubjects: The number of subjects.

- settings: A list containing the following input parameters:

  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - spendingTime: The error spending time at each analysis.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignRiskDiffEquiv(
  beta = 0.2, n = NA, riskDiffLower = -0.1,
  riskDiffUpper = 0.1, pi1 = 0.12, pi2 = 0.12,
  kMax = 3, alpha = 0.05, typeAlphaSpending = "sfOF"))
```

getDesignRiskDiffExact

Power and Sample Size for Exact Unconditional Test for Risk Difference

Description

Obtains the power given sample size or obtains the sample size given power for exact unconditional test of risk difference.

Usage

```
getDesignRiskDiffExact(
  beta = NA_real_,
  n = NA_real_,
  riskDiffH0 = 0,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  alpha = 0.025
)
```

Arguments

beta	The type II error.
n	The total sample size.
riskDiffH0	The risk difference under the null hypothesis. Defaults to 0.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
allocationRatioPlanned	
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
alpha	The one-sided significance level. Defaults to 0.025.

Value

A data frame with the following variables:

- alpha: The specified one-sided significance level.
- attainedAlpha: The attained one-sided significance level.
- power: The power.
- n: The sample size.
- riskDiffH0: The risk difference under the null hypothesis.
- pi1: The assumed probability for the active treatment group.
- pi2: The assumed probability for the control group.
- allocationRatioPlanned: Allocation ratio for the active treatment versus control.
- zstatRiskDiffBound: The critical value on the scale of score test statistic for risk difference.
- pi2star: The response probability in the control group at which the critical value of the test statistic is attained.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Superiority test

getDesignRiskDiffExact(n = 50, pi1 = 0.6, pi2 = 0.25, alpha = 0.025)


# Non-inferiority test

getDesignRiskDiffExact(beta = 0.2, riskDiffH0 = -0.3,
                       pi1 = 0.9, pi2 = 0.9, alpha = 0.025)
```

---

getDesignRiskDiffExactEquiv

Power and Sample Size for Exact Unconditional Test for Equivalence in Risk Difference

---

Description

Obtains the power given sample size or obtains the sample size given power for exact unconditional test of equivalence in risk difference.

Usage

```
getDesignRiskDiffExactEquiv(
  beta = NA_real_,
  n = NA_real_,
  riskDiffLower = NA_real_,
  riskDiffUpper = NA_real_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  alpha = 0.05
)
```

Arguments

beta	The type II error.
n	The total sample size.
riskDiffLower	The lower equivalence limit of risk difference.
riskDiffUpper	The upper equivalence limit of risk difference.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
allocationRatioPlanned	
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
alpha	The significance level for each of the two one-sided tests. Defaults to 0.05.

Value

A data frame with the following variables:

- alpha: The specified significance level for each of the two one-sided tests.

- attainedAlpha: The attained significance level.

- power: The power.

- n: The sample size.

- riskDiffLower: The lower equivalence limit of risk difference.

- riskDiffUpper: The upper equivalence limit of risk difference.

- pi1: The assumed probability for the active treatment group.

- pi2: The assumed probability for the control group.

- riskDiff: The risk difference.

- allocationRatioPlanned: Allocation ratio for the active treatment versus control.

- zstatRiskDiffLower: The efficacy boundaries on the z-test statistic scale for the one-sided null hypothesis on the lower equivalence limit.

- zstatRiskDiffUpper: The efficacy boundaries on the z-test statistic scale for the one-sided null hypothesis on the upper equivalence limit.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
getDesignRiskDiffExactEquiv(
  n = 200, riskDiffLower = -0.2, riskDiffUpper = 0.2,
  pi1 = 0.775, pi2 = 0.775, alpha = 0.05)
```

---

getDesignRiskRatio   *Group Sequential Design for Two-Sample Risk Ratio*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample risk ratio.

Usage

```
getDesignRiskRatio(
  beta = NA_real_,
  n = NA_real_,
  riskRatioH0 = 1,
  pi1 = NA_real_,
  pi2 = NA_real_,
  nullVariance = TRUE,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
riskRatioH0	The risk ratio under the null hypothesis. Defaults to 1.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
nullVariance	Whether to use the variance under the null or the empirical variance under the alternative.
allocationRatioPlanned	
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	
	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
efficacyStopping	
	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

        Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues   Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha   The significance level. Defaults to 0.025.

typeAlphaSpending

        The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

        The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

        The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds   Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

        The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

        The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

        The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designRiskRatio object with three components:

- overallResults: A data frame containing the following variables:
    - overallReject: The overall rejection probability.
    - alpha: The overall significance level.
    - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
    - kMax: The number of stages.
    - theta: The parameter value.
    - information: The maximum information.

- **expectedInformationH1**: The expected information under H1.
- **expectedInformationH0**: The expected information under H0.
- **drift**: The drift parameter, equal to `theta*sqrt(information)`.
- **inflationFactor**: The inflation factor (relative to the fixed design).
- **numberOfSubjects**: The maximum number of subjects.
- **expectedNumberOfSubjectsH1**: The expected number of subjects under H1.
- **expectedNumberOfSubjectsH0**: The expected number of subjects under H0.
- **riskRatioH0**: The risk ratio under the null hypothesis.
- **pi1**: The assumed probability for the active treatment group.
- **pi2**: The assumed probability for the control group.
- **byStageResults**: A data frame containing the following variables:
  - **informationRates**: The information rates.
  - **efficacyBounds**: The efficacy boundaries on the Z-scale.
  - **futilityBounds**: The futility boundaries on the Z-scale.
  - **rejectPerStage**: The probability for efficacy stopping.
  - **futilityPerStage**: The probability for futility stopping.
  - **cumulativeRejection**: The cumulative probability for efficacy stopping.
  - **cumulativeFutility**: The cumulative probability for futility stopping.
  - **cumulativeAlphaSpent**: The cumulative alpha spent.
  - **efficacyP**: The efficacy boundaries on the p-value scale.
  - **futilityP**: The futility boundaries on the p-value scale.
  - **information**: The cumulative information.
  - **efficacyStopping**: Whether to allow efficacy stopping.
  - **futilityStopping**: Whether to allow futility stopping.
  - **rejectPerStageH0**: The probability for efficacy stopping under H0.
  - **futilityPerStageH0**: The probability for futility stopping under H0.
  - **cumulativeRejectionH0**: The cumulative probability for efficacy stopping under H0.
  - **cumulativeFutilityH0**: The cumulative probability for futility stopping under H0.
  - **efficacyRiskRatio**: The efficacy boundaries on the risk ratio scale.
  - **futilityRiskRatio**: The futility boundaries on the risk ratio scale.
  - **numberOfSubjects**: The number of subjects.
- **settings**: A list containing the following input parameters:
  - **typeAlphaSpending**: The type of alpha spending.
  - **parameterAlphaSpending**: The parameter value for alpha spending.
  - **userAlphaSpending**: The user defined alpha spending.
  - **typeBetaSpending**: The type of beta spending.
  - **parameterBetaSpending**: The parameter value for beta spending.
  - **userBetaSpending**: The user defined beta spending.
  - **spendingTime**: The error spending time at each analysis.
  - **varianceRatio**: The ratio of the variance under H0 to the variance under H1.
  - **nullVariance**: Whether to use the variance under the null or the empirical variance under the alternative.
  - **allocationRatioPlanned**: Allocation ratio for the active treatment versus control.
  - **rounding**: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignRiskRatio(
  beta = 0.1, n = NA, pi1 = 0.5, pi2 = 0.3,
  alpha = 0.05))
```

---

getDesignRiskRatioEquiv

Group Sequential Design for Equivalence in Two-Sample Risk Ratio

---

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in two-sample risk ratio.

Usage

```
getDesignRiskRatioEquiv(
  beta = NA_real_,
  n = NA_real_,
  riskRatioLower = NA_real_,
  riskRatioUpper = NA_real_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
riskRatioLower	The lower equivalence limit of risk ratio.
riskRatioUpper	The upper equivalence limit of risk ratio.

pi1   The assumed probability for the active treatment group.

pi2   The assumed probability for the control group.

allocationRatioPlanned

                     Allocation ratio for the active treatment versus control. Defaults to 1 for equal
                     randomization.

rounding   Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax   The maximum number of stages.

informationRates

                     The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if
                     left unspecified.

criticalValues   Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha   The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending

                     The type of alpha spending. One of the following: "OF" for O'Brien-Fleming
                     boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries,
                     "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spend-
                     ing function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang,
                     Shi & DeCani spending function, "user" for user defined spending, and "none"
                     for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

                     The parameter value for the alpha spending. Corresponds to Delta for "WT",
                     rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

                     The user defined alpha spending. Cumulative alpha spent up to each stage.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to
                     missing, in which case, it is the same as informationRates.

Value

An S3 class designRiskRatioEquiv object with three components:

- overallResults: A data frame containing the following variables:
    - overallReject: The overall rejection probability.
    - alpha: The significance level for each of the two one-sided tests. Defaults to 0.05.
    - attainedAlphaH10: The attained significance level under H10.
    - attainedAlphaH20: The attained significance level under H20.
    - kMax: The number of stages.
    - information: The maximum information.
    - expectedInformationH1: The expected information under H1.
    - expectedInformationH10: The expected information under H10.
    - expectedInformationH20: The expected information under H20.
    - numberOfSubjects: The maximum number of subjects.
    - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
    - expectedNumberOfSubjectsH10: The expected number of subjects under H10.

- expectedNumberOfSubjectsH20: The expected number of subjects under H20.
        - riskRatioLower: The lower equivalence limit of risk ratio.
        - riskRatioUpper: The upper equivalence limit of risk ratio.
        - pi1: The assumed probability for the active treatment group.
        - pi2: The assumed probability for the control group.
        - riskRatio: The risk ratio.

- byStageResults: A data frame containing the following variables:

    - informationRates: The information rates.
    - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
    - rejectPerStage: The probability for efficacy stopping.
    - cumulativeRejection: The cumulative probability for efficacy stopping.
    - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
    - cumulativeAttainedAlphaH10: The cumulative alpha attained under H10.
    - cumulativeAttainedAlphaH20: The cumulative alpha attained under H20.
    - efficacyRiskRatioLower: The efficacy boundaries on the risk ratio scale for the one-sided null hypothesis on the lower equivalence limit.
    - efficacyRiskRatioUpper: The efficacy boundaries on the risk ratio scale for the one-sided null hypothesis on the upper equivalence limit.
    - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
    - information: The cumulative information.
    - numberOfSubjects: The number of subjects.

- settings: A list containing the following input parameters:

    - typeAlphaSpending: The type of alpha spending.
    - parameterAlphaSpending: The parameter value for alpha spending.
    - userAlphaSpending: The user defined alpha spending.
    - spendingTime: The error spending time at each analysis.
    - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
    - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignRiskRatioEquiv(
  beta = 0.2, n = NA, riskRatioLower = 0.8,
  riskRatioUpper = 1.25, pi1 = 0.12, pi2 = 0.12,
  kMax = 3, alpha = 0.05, typeAlphaSpending = "sfOF"))
```

---

getDesignRiskRatioExact

Power and Sample Size for Exact Unconditional Test for Risk Ratio

---

Description

Obtains the power given sample size or obtains the sample size given power for exact unconditional test of risk ratio.

Usage

```
getDesignRiskRatioExact(
  beta = NA_real_,
  n = NA_real_,
  riskRatioH0 = 1,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  alpha = 0.025
)
```

Arguments

beta	The type II error.
n	The total sample size.
riskRatioH0	The risk ratio under the null hypothesis. Defaults to 0.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
allocationRatioPlanned	
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
alpha	The one-sided significance level. Defaults to 0.025.

Value

A data frame with the following variables:

- alpha: The specified one-sided significance level.
- attainedAlpha: The attained one-sided significance level.
- power: The power.
- n: The sample size.
- riskRatioH0: The risk ratio under the null hypothesis.
- pi1: The assumed probability for the active treatment group.
- pi2: The assumed probability for the control group.

- allocationRatioPlanned: Allocation ratio for the active treatment versus control.
- zstatRiskRatioBound: The critical value on the scale of score test statistic for risk ratio.
- pi2star: The response probability in the control group at which the critical value of the test statistic is attained.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Non-inferiority test

getDesignRiskRatioExact(beta = 0.2, riskRatioH0 = 0.7,
                        pi1 = 0.95, pi2 = 0.95, alpha = 0.025)
```

---

getDesignRiskRatioExactEquiv

Power and Sample Size for Exact Unconditional Test for Equivalence in Risk Ratio

---

Description

Obtains the power given sample size or obtains the sample size given power for exact unconditional test of equivalence in risk ratio.

Usage

```
getDesignRiskRatioExactEquiv(
  beta = NA_real_,
  n = NA_real_,
  riskRatioLower = NA_real_,
  riskRatioUpper = NA_real_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  alpha = 0.05
)
```

Arguments

beta	The type II error.
n	The total sample size.
riskRatioLower	The lower equivalence limit of risk ratio.
riskRatioUpper	The upper equivalence limit of risk ratio.

pi1   The assumed probability for the active treatment group.

pi2   The assumed probability for the control group.

allocationRatioPlanned

                     Allocation ratio for the active treatment versus control. Defaults to 1 for equal
                     randomization.

alpha   The significance level for each of the two one-sided tests. Defaults to 0.05.

Value

A data frame with the following variables:

- alpha: The specified significance level for each of the two one-sided tests.

- attainedAlpha: The attained significance level.

- power: The power.

- n: The sample size.

- riskRatioLower: The lower equivalence limit of risk ratio.

- riskRatioUpper: The upper equivalence limit of risk ratio.

- pi1: The assumed probability for the active treatment group.

- pi2: The assumed probability for the control group.

- riskRatio: The risk ratio.

- allocationRatioPlanned: Allocation ratio for the active treatment versus control.

- zstatRiskRatioLower: The efficacy boundaries on the z-test statistic scale for the one-sided
  null hypothesis on the lower equivalence limit.

- zstatRiskRatioUpper: The efficacy boundaries on the z-test statistic scale for the one-sided
  null hypothesis on the upper equivalence limit.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
getDesignRiskRatioExactEquiv(
  n = 200, riskRatioLower = 0.8, riskRatioUpper = 1.25,
  pi1 = 0.775, pi2 = 0.775, alpha = 0.05)
```

---

getDesignRiskRatioFM   *Group Sequential Design for Two-Sample Risk Ratio Based on the Farrington-Manning Score Test*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample risk ratio based on the Farrington-Manning score test

Usage

```
getDesignRiskRatioFM(
  beta = NA_real_,
  n = NA_real_,
  riskRatioH0 = 1,
  pi1 = NA_real_,
  pi2 = NA_real_,
  nullVariance = TRUE,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
riskRatioH0	The risk ratio under the null hypothesis. Defaults to 1.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
nullVariance	Whether to use the variance under the null or the empirical variance under the alternative.

allocationRatioPlanned

        Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

rounding   Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax   The maximum number of stages.

informationRates

        The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

        Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

        Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues   Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha   The significance level. Defaults to 0.025.

typeAlphaSpending

        The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

        The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

        The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds   Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

        The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

        The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

        The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designRiskRatioFM object with three components:

- overallResults: A data frame containing the following variables:
    - overallReject: The overall rejection probability.
    - alpha: The overall significance level.
    - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
    - kMax: The number of stages.
    - theta: The parameter value.
    - information: The maximum information.
    - expectedInformationH1: The expected information under H1.
    - expectedInformationH0: The expected information under H0.
    - drift: The drift parameter, equal to theta*sqrt(information).
    - inflationFactor: The inflation factor (relative to the fixed design).
    - numberOfSubjects: The maximum number of subjects.
    - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
    - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
    - riskRatioH0: The risk ratio under the null hypothesis.
    - pi1: The assumed probability for the active treatment group.
    - pi2: The assumed probability for the control group.
- byStageResults: A data frame containing the following variables:
    - informationRates: The information rates.
    - efficacyBounds: The efficacy boundaries on the Z-scale.
    - futilityBounds: The futility boundaries on the Z-scale.
    - rejectPerStage: The probability for efficacy stopping.
    - futilityPerStage: The probability for futility stopping.
    - cumulativeRejection: The cumulative probability for efficacy stopping.
    - cumulativeFutility: The cumulative probability for futility stopping.
    - cumulativeAlphaSpent: The cumulative alpha spent.
    - efficacyP: The efficacy boundaries on the p-value scale.
    - futilityP: The futility boundaries on the p-value scale.
    - information: The cumulative information.
    - efficacyStopping: Whether to allow efficacy stopping.
    - futilityStopping: Whether to allow futility stopping.
    - rejectPerStageH0: The probability for efficacy stopping under H0.
    - futilityPerStageH0: The probability for futility stopping under H0.
    - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
    - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
    - efficacyRiskRatioScore: The efficacy boundaries on the score test pi1 - riskRatioH0*pi2 score.
    - futilityRiskRatioScore: The futility boundaries on the score test pi1 - riskRatioH0*pi2 scale.

- – numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - – typeAlphaSpending: The type of alpha spending.
  - – parameterAlphaSpending: The parameter value for alpha spending.
  - – userAlphaSpending: The user defined alpha spending.
  - – typeBetaSpending: The type of beta spending.
  - – parameterBetaSpending: The parameter value for beta spending.
  - – userBetaSpending: The user defined beta spending.
  - – spendingTime: The error spending time at each analysis.
  - – varianceRatio: The ratio of the variance under H0 to the variance under H1.
  - – nullVariance: Whether to use the variance under the null or the empirical variance under the alternative.
  - – allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - – rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignRiskRatioFM(
  beta = 0.2, riskRatioH0 = 1.3, pi1 = 0.125, pi2 = 0.125,
  alpha = 0.05))
```

---

getDesignSlopeDiff   *Group Sequential Design for Two-Sample Slope Difference*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample slope difference.

Usage

```
getDesignSlopeDiff(
  beta = NA_real_,
  n = NA_real_,
  slopeDiffH0 = 0,
  slopeDiff = 0.5,
  stDev = 1,
  stDevCovariate = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
```

```
    kMax = 1L,
    informationRates = NA_real_,
    efficacyStopping = NA_integer_,
    futilityStopping = NA_integer_,
    criticalValues = NA_real_,
    alpha = 0.025,
    typeAlphaSpending = "sfOF",
    parameterAlphaSpending = NA_real_,
    userAlphaSpending = NA_real_,
    futilityBounds = NA_real_,
    typeBetaSpending = "none",
    parameterBetaSpending = NA_real_,
    userBetaSpending = NA_real_,
    spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
slopeDiffH0	The slope difference under the null hypothesis. Defaults to 0.
slopeDiff	The slope difference under the alternative hypothesis.
stDev	The standard deviation of the residual.
stDevCovariate	The standard deviation of the covariate.
allocationRatioPlanned	
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
normalApproximation	
	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	
	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
efficacyStopping	
	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	
	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.

typeAlphaSpending

> The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

> The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

> The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds   Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

> The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

> The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

> The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designSlopeDiff object with three components:

- overallResults: A data frame containing the following variables:
    - overallReject: The overall rejection probability.
    - alpha: The overall significance level.
    - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
    - kMax: The number of stages.
    - theta: The parameter value.
    - information: The maximum information.
    - expectedInformationH1: The expected information under H1.
    - expectedInformationH0: The expected information under H0.
    - drift: The drift parameter, equal to theta*sqrt(information).
    - inflationFactor: The inflation factor (relative to the fixed design).
    - numberOfSubjects: The maximum number of subjects.

- expectedNumberOfSubjectsH1: The expected number of subjects under H1.
- expectedNumberOfSubjectsH0: The expected number of subjects under H0.
- slopeDiffH0: The slope difference under the null hypothesis.
- slopeDiff: The slope difference under the alternative hypothesis.
- stDev: The standard deviation of the residual.
- stDevCovariate: The standard deviation of the covariate.

- byStageResults: A data frame containing the following variables:

  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacySlopeDiff: The efficacy boundaries on the slope difference scale.
  - futilitySlopeDiff: The futility boundaries on the slope difference scale.
  - numberOfSubjects: The number of subjects.

- settings: A list containing the following input parameters:

  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
  - rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignSlopeDiff(
  beta = 0.1, n = NA, slopeDiff = -0.5,
  stDev = 10, stDevCovariate = 6,
  normalApproximation = FALSE, alpha = 0.025))
```

getDesignSlopeDiffMMRM

Group Sequential Design for Two-Sample Slope Difference From the MMRM Model

Description

Obtains the power given sample size or obtains the sample size given power for two-sample slope difference from the growth curve MMRM model.

Usage

```
getDesignSlopeDiffMMRM(
  beta = NA_real_,
  slopeDiffH0 = 0,
  slopeDiff = 0.5,
  stDev = 1,
  stDevIntercept = 1,
  stDevSlope = 1,
  corrInterceptSlope = 0.5,
  w = NA_real_,
  N = NA_real_,
  accrualTime = 0,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0,
  gamma1 = 0,
  gamma2 = 0,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
```

```
    userAlphaSpending = NA_real_,
    futilityBounds = NA_real_,
    typeBetaSpending = "none",
    parameterBetaSpending = NA_real_,
    userBetaSpending = NA_real_,
    spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
slopeDiffH0	The slope difference under the null hypothesis. Defaults to 0.
slopeDiff	The slope difference under the alternative hypothesis.
stDev	The standard deviation of the residual.
stDevIntercept	The standard deviation of the random intercept.
stDevSlope	The standard deviation of the random slope.
corrInterceptSlope	
	The correlation between the random intercept and random slope.
w	The number of time units per measurement visit in a period.
N	The number of measurement visits in a period.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).
accrualIntensity	
	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	
	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.
gamma1	The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the active treatment group.
gamma2	The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the control group.
accrualDuration	
	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
allocationRatioPlanned	
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
normalApproximation	
	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The degrees of freedom for the t-distribution for testing the slope difference is calculated using the containment method, and is equal to the total number of observations minus two times the total number of subjects. The exact calculation using the t distribution is only implemented for the fixed design.

rounding   Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax   The maximum number of stages.

informationRates

                  The information rates. Defaults to `(1:kMax) / kMax` if left unspecified.

efficacyStopping

                  Indicators of whether efficacy stopping is allowed at each stage. Defaults to true
                  if left unspecified.

futilityStopping

                  Indicators of whether futility stopping is allowed at each stage. Defaults to true
                  if left unspecified.

criticalValues   Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha   The significance level. Defaults to 0.025.

typeAlphaSpending

                  The type of alpha spending. One of the following: "OF" for O'Brien-Fleming
                  boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries,
                  "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spend-
                  ing function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang,
                  Shi & DeCani spending function, "user" for user defined spending, and "none"
                  for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

                  The parameter value for the alpha spending. Corresponds to Delta for "WT",
                  rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

                  The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds   Lower boundaries on the z-test statistic scale for stopping for futility at stages 1,
                  ..., kMax-1. Defaults to `rep(-6, kMax-1)` if left unspecified. The futility bounds
                  are non-binding for the calculation of critical values.

typeBetaSpending

                  The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming
                  type spending function, "sfP" for Pocock type spending function, "sfKD" for
                  Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spend-
                  ing function, "user" for user defined spending, and "none" for no early futility
                  stopping. Defaults to "none".

parameterBetaSpending

                  The parameter value for the beta spending. Corresponds to rho for "sfKD", and
                  gamma for "sfHSD".

userBetaSpending

                  The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to
                  missing, in which case, it is the same as informationRates.

Details

We use the following random-effects model to compare two slopes:

$$y_{ij} = \alpha + (\beta + \gamma x_i)t_j + a_i + b_i t_j + e_{ij},$$

where

- α: overall intercept common across treatment groups due to randomization
- β: slope for the control group
- γ: difference in slopes between the active treatment and control groups
- x_i: treatment indicator for subject i, 1 for the active treatment and 0 for the control
- t_j: time point j for repeated measurements, $t_1 = 0 < t_2 < \ldots < t_k$
- (a_i, b_i): random intercept and random slope for subject i, $Var(a_i) = \sigma_a^2$, $Var(b_i) = \sigma_b^2$, $Corr(a_i, b_i) = \rho$
- e_{ij}: within-subject residual with variance σ_e^2

By accounting for randomization, we improve the efficiency for estimating the difference in slopes. We also allow for non-equal spacing of the time points and missing data due to dropouts.

Value

An S3 class `designSlopeDiffMMRM` object with three components:

- `overallResults`: A data frame containing the following variables:
    - `overallReject`: The overall rejection probability.
    - `alpha`: The overall significance level.
    - `attainedAlpha`: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
    - `kMax`: The number of stages.
    - `theta`: The parameter value.
    - `information`: The maximum information.
    - `expectedInformationH1`: The expected information under H1.
    - `expectedInformationH0`: The expected information under H0.
    - `drift`: The drift parameter, equal to `theta*sqrt(information)`.
    - `inflationFactor`: The inflation factor (relative to the fixed design).
    - `numberOfSubjects`: The maximum number of subjects.
    - `studyDuration`: The maximum study duration.
    - `expectedNumberOfSubjectsH1`: The expected number of subjects under H1.
    - `expectedNumberOfSubjectsH0`: The expected number of subjects under H0.
    - `expectedStudyDurationH1`: The expected study duration under H1.
    - `expectedStudyDurationH0`: The expected study duration under H0.
    - `accrualDuration`: The accrual duration.
    - `followupTime`: The follow-up time.
    - `fixedFollowup`: Whether a fixed follow-up design is used.
    - `slopeDiffH0`: The slope difference under H0.
    - `slopeDiff`: The slope difference under H1.
- `byStageResults`: A data frame containing the following variables:
    - `informationRates`: The information rates.
    - `efficacyBounds`: The efficacy boundaries on the Z-scale.
    - `futilityBounds`: The futility boundaries on the Z-scale.

- – rejectPerStage: The probability for efficacy stopping.
- – futilityPerStage: The probability for futility stopping.
- – cumulativeRejection: The cumulative probability for efficacy stopping.
- – cumulativeFutility: The cumulative probability for futility stopping.
- – cumulativeAlphaSpent: The cumulative alpha spent.
- – efficacyP: The efficacy boundaries on the p-value scale.
- – futilityP: The futility boundaries on the p-value scale.
- – information: The cumulative information.
- – efficacyStopping: Whether to allow efficacy stopping.
- – futilityStopping: Whether to allow futility stopping.
- – rejectPerStageH0: The probability for efficacy stopping under H0.
- – futilityPerStageH0: The probability for futility stopping under H0.
- – cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
- – cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
- – efficacySlopeDiff: The efficacy boundaries on the slope difference scale.
- – futilitySlopeDiff: The futility boundaries on the slope difference scale.
- – numberOfSubjects: The number of subjects.
- – analysisTime: The average time since trial start.
- settings: A list containing the following input parameters:
  - – typeAlphaSpending: The type of alpha spending.
  - – parameterAlphaSpending: The parameter value for alpha spending.
  - – userAlphaSpending: The user defined alpha spending.
  - – typeBetaSpending: The type of beta spending.
  - – parameterBetaSpending: The parameter value for beta spending.
  - – userBetaSpending: The user defined beta spending.
  - – spendingTime: The error spending time at each analysis.
  - – allocationRatioPlanned: The allocation ratio for the active treatment versus control.
  - – accrualTime: A vector that specifies the starting time of piecewise Poisson enrollment time intervals.
  - – accrualIntensity: A vector of accrual intensities. One for each accrual time interval.
  - – piecewiseSurvivalTime: A vector that specifies the starting time of piecewise exponential survival time intervals.
  - – gamma1: The hazard rate for exponential dropout or a vector of hazard rates for piecewise exponential dropout for the active treatment group.
  - – gamma2: The hazard rate for exponential dropout or a vector of hazard rates for piecewise exponential dropout for the control group.
  - – w: The number of time units per measurement visit in a period.
  - – N: The number of measurement visits in a period.
  - – stdDev: The standard deviation of the residual.
  - – G: The covariance matrix for the random intercept and random slope.
  - – normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
  - – rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Daniel O. Scharfstein, Anastasios A. Tsiatis, and James M. Robins. Semiparametric efficiency and its implication on the design and analysis of group-sequential studies. Journal of the American Statistical Association 1997; 92:1342-1350.

Examples

```
(design1 <- getDesignSlopeDiffMMRM(
  beta = 0.2, slopeDiff = log(1.15)/52,
  stDev = sqrt(.182),
  stDevIntercept = sqrt(.238960),
  stDevSlope = sqrt(.000057),
  corrInterceptSlope = .003688/sqrt(.238960*.000057),
  w = 8,
  N = 10000,
  accrualIntensity = 15,
  gamma1 = 1/(4.48*52),
  gamma2 = 1/(4.48*52),
  accrualDuration = NA,
  followupTime = 8,
  alpha = 0.025))
```

---

getDesignTwoMultinom | *Power and Sample Size for Difference in Two-Sample Multinomial Responses*

Description

Obtains the power given sample size or obtains the sample size given power for difference in two-sample multinomial responses.

Usage

```
getDesignTwoMultinom(
  beta = NA_real_,
  n = NA_real_,
  ncats = NA_integer_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  alpha = 0.05
)
```

Arguments

beta	The type II error.
n	The total sample size.
ncats	The number of categories of the multinomial response.
pi1	The prevalence of each category for the treatment group. Only need to specify the valued for the first ncats-1 categories.
pi2	The prevalence of each category for the control group. Only need to specify the valued for the first ncats-1 categories.
allocationRatioPlanned	
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.

Value

An S3 class designTwoMultinom object with the following components:

- power: The power to reject the null hypothesis.
- alpha: The two-sided significance level.
- n: The maximum number of subjects.
- ncats: The number of categories of the multinomial response.
- pi1: The prevalence of each category for the treatment group.
- pi2: The prevalence of each category for the control group.
- effectsize: The effect size for the chi-square test.
- allocationRatioPlanned: Allocation ratio for the active treatment versus control.
- rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignTwoMultinom(
  beta = 0.1, ncats = 3, pi1 = c(0.3, 0.35),
  pi2 = c(0.2, 0.3), alpha = 0.05))
```

---

getDesignTwoOrdinal | *Power and Sample Size for the Wilcoxon Test for Two-Sample Ordinal Response*

Description

Obtains the power given sample size or obtains the sample size given power for the Wilcoxon test for two-sample ordinal response.

Usage

```
getDesignTwoOrdinal(
  beta = NA_real_,
  n = NA_real_,
  ncats = NA_integer_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  alpha = 0.05
)
```

Arguments

beta	The type II error.
n	The total sample size.
ncats	The number of categories of the ordinal response.
pi1	The prevalence of each category for the treatment group. Only need to specify the valued for the first ncats-1 categories.
pi2	The prevalence of each category for the control group. Only need to specify the valued for the first ncats-1 categories.
allocationRatioPlanned	
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The significance level. Defaults to 0.025.

Value

An S3 class designTwoOrdinal object with the following components:

- power: The power to reject the null hypothesis.
- alpha: The two-sided significance level.
- n: The maximum number of subjects.

- `ncats`: The number of categories of the ordinal response.
- `pi1`: The prevalence of each category for the treatment group.
- `pi2`: The prevalence of each category for the control group.
- `meanscore1`: The mean midrank score for the treatment group.
- `meanscore2`: The mean midrank score for the control group.
- `allocationRatioPlanned`: Allocation ratio for the active treatment versus control.
- `rounding`: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignTwoOrdinal(
  beta = 0.1, ncats = 4, pi1 = c(0.55, 0.3, 0.1),
  pi2 = c(0.214, 0.344, 0.251), alpha = 0.025))
```

---

getDesignTwoWayANOVA   *Power and Sample Size for Two-Way ANOVA*

Description

Obtains the power and sample size for two-way analysis of variance.

Usage

```
getDesignTwoWayANOVA(
  beta = NA_real_,
  n = NA_real_,
  nlevelsA = 2,
  nlevelsB = 2,
  means = NA_real_,
  stDev = 1,
  rounding = TRUE,
  alpha = 0.05
)
```

Arguments

beta	The type II error.
n	The total sample size.
nlevelsA	The number of groups for Factor A.
nlevelsB	The number of levels for Factor B.

means	The matrix of treatment means for Factors A and B combination.
stDev	The common standard deviation.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.

Value

An S3 class `designTwoWayANOVA` object with the following components:

- `alpha`: The two-sided significance level.
- `nlevelsA`: The number of levels for Factor A.
- `nlevelsB`: The number of levels for Factor B.
- `means`: The matrix of treatment group means.
- `stDev`: The common standard deviation.
- `effectsizeA`: The effect size for Factor A.
- `effectsizeB`: The effect size for Factor B.
- `effectsizeAB`: The effect size for Factor A and Factor B interaction.
- `rounding`: Whether to round up sample size.
- `powerdf`: The data frame containing the power and sample size results. It has the following variables:
  - `n`: The sample size.
  - `powerA`: The power to reject the null hypothesis that there is no difference among Factor A levels.
  - `powerB`: The power to reject the null hypothesis that there is no difference among Factor B levels.
  - `powerAB`: The power to reject the null hypothesis that there is no interaction between Factor A and Factor B.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignTwoWayANOVA(
  beta = 0.1, nlevelsA = 2, nlevelsB = 2,
  means = matrix(c(0.5, 4.7, 0.4, 6.9), 2, 2, byrow = TRUE),
  stDev = 2, alpha = 0.05))
```

---

getDesignUnorderedBinom

> *Power and Sample Size for Unordered Multi-Sample Binomial Response*

Description

Obtains the power given sample size or obtains the sample size given power for the chi-square test for unordered multi-sample binomial response.

Usage

```
getDesignUnorderedBinom(
  beta = NA_real_,
  n = NA_real_,
  ngroups = NA_integer_,
  pi = NA_real_,
  allocationRatioPlanned = NA_integer_,
  rounding = TRUE,
  alpha = 0.05
)
```

Arguments

beta	The type II error.
n	The total sample size.
ngroups	The number of treatment groups.
pi	The response probabilities for the treatment groups.
allocationRatioPlanned	
	Allocation ratio for the treatment groups.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.

Value

An S3 class designUnorderedBinom object with the following components:

- power: The power to reject the null hypothesis.
- alpha: The two-sided significance level.
- n: The maximum number of subjects.
- ngroups: The number of treatment groups.
- pi: The response probabilities for the treatment groups.
- effectsize: The effect size for the chi-square test.
- allocationRatioPlanned: Allocation ratio for the treatment groups.
- rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignUnorderedBinom(
  beta = 0.1, ngroups = 3, pi = c(0.1, 0.25, 0.5), alpha = 0.05))
```

---

getDesignUnorderedMultinom

Power and Sample Size for Unordered Multi-Sample Multinomial Response

---

Description

Obtains the power given sample size or obtains the sample size given power for the chi-square test for unordered multi-sample multinomial response.

Usage

```
getDesignUnorderedMultinom(
  beta = NA_real_,
  n = NA_real_,
  ngroups = NA_integer_,
  ncats = NA_integer_,
  pi = NA_real_,
  allocationRatioPlanned = NA_integer_,
  rounding = TRUE,
  alpha = 0.05
)
```

Arguments

beta	The type II error.
n	The total sample size.
ngroups	The number of treatment groups.
ncats	The number of categories of the multinomial response.
pi	The matrix of response probabilities for the treatment groups. It should have ngroups rows and ncats-1 or ncats columns.
allocationRatioPlanned	
	Allocation ratio for the treatment groups.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.

Value

An S3 class designUnorderedMultinom object with the following components:

- power: The power to reject the null hypothesis.
- alpha: The two-sided significance level.
- n: The maximum number of subjects.
- ngroups: The number of treatment groups.
- ncats: The number of categories of the multinomial response.
- pi: The response probabilities for the treatment groups.
- effectsize: The effect size for the chi-square test.
- allocationRatioPlanned: Allocation ratio for the treatment groups.
- rounding: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(design1 <- getDesignUnorderedMultinom(
  beta = 0.1, ngroups = 3, ncats = 4,
  pi = matrix(c(0.230, 0.320, 0.272,
                0.358, 0.442, 0.154,
                0.142, 0.036, 0.039),
              3, 3, byrow = TRUE),
  allocationRatioPlanned = c(2, 2, 1),
  alpha = 0.05))
```

---

getDesignWilcoxon   *Group Sequential Design for Two-Sample Wilcoxon Test*

Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample Wilcoxon test.

Usage

```
getDesignWilcoxon(
  beta = NA_real_,
  n = NA_real_,
  pLarger = 0.6,
  allocationRatioPlanned = 1,
  rounding = TRUE,
```

```
    kMax = 1L,
    informationRates = NA_real_,
    efficacyStopping = NA_integer_,
    futilityStopping = NA_integer_,
    criticalValues = NA_real_,
    alpha = 0.025,
    typeAlphaSpending = "sfOF",
    parameterAlphaSpending = NA_real_,
    userAlphaSpending = NA_real_,
    futilityBounds = NA_real_,
    typeBetaSpending = "none",
    parameterBetaSpending = NA_real_,
    userBetaSpending = NA_real_,
    spendingTime = NA_real_
)
```

Arguments

beta	The type II error.
n	The total sample size.
pLarger	The probability that a randomly chosen sample from the treatment group is larger than a randomly chosen sample from the control group under the alternative hypothesis.
allocationRatioPlanned	
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	
	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
efficacyStopping	
	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	
	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	
	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

> The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

> The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds   Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

> The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

> The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

> The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Value

An S3 class designWilcoxon object with three components:

- overallResults: A data frame containing the following variables:
    - overallReject: The overall rejection probability.
    - alpha: The overall significance level.
    - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping..
    - kMax: The number of stages.
    - theta: The parameter value.
    - information: The maximum information.
    - expectedInformationH1: The expected information under H1.
    - expectedInformationH0: The expected information under H0.
    - drift: The drift parameter, equal to theta*sqrt(information).
    - inflationFactor: The inflation factor (relative to the fixed design).
    - numberOfSubjects: The maximum number of subjects.
    - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
    - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
    - pLarger: The probability that a randomly chosen sample from the treatment group is larger than a randomly chosen sample from the control group under the alternative hypothesis.
- byStageResults: A data frame containing the following variables:

- – `informationRates`: The information rates.
- – `efficacyBounds`: The efficacy boundaries on the Z-scale.
- – `futilityBounds`: The futility boundaries on the Z-scale.
- – `rejectPerStage`: The probability for efficacy stopping.
- – `futilityPerStage`: The probability for futility stopping.
- – `cumulativeRejection`: The cumulative probability for efficacy stopping.
- – `cumulativeFutility`: The cumulative probability for futility stopping.
- – `cumulativeAlphaSpent`: The cumulative alpha spent.
- – `efficacyP`: The efficacy boundaries on the p-value scale.
- – `futilityP`: The futility boundaries on the p-value scale.
- – `information`: The cumulative information.
- – `efficacyStopping`: Whether to allow efficacy stopping.
- – `futilityStopping`: Whether to allow futility stopping.
- – `rejectPerStageH0`: The probability for efficacy stopping under H0.
- – `futilityPerStageH0`: The probability for futility stopping under H0.
- – `cumulativeRejectionH0`: The cumulative probability for efficacy stopping under H0.
- – `cumulativeFutilityH0`: The cumulative probability for futility stopping under H0.
- – `efficacyPLarger`: The efficacy boundaries on the proportion of pairs of samples from the two treatment groups with the sample from the treatment group greater than that from the control group.
- – `futilityPLarger`: The futility boundaries on the proportion of pairs of samples from the two treatment groups with the sample from the treatment group greater than that from the control group.
- – `numberOfSubjects`: The number of subjects.
- `settings`: A list containing the following input parameters:
  - – `typeAlphaSpending`: The type of alpha spending.
  - – `parameterAlphaSpending`: The parameter value for alpha spending.
  - – `userAlphaSpending`: The user defined alpha spending.
  - – `typeBetaSpending`: The type of beta spending.
  - – `parameterBetaSpending`: The parameter value for beta spending.
  - – `userBetaSpending`: The user defined beta spending.
  - – `spendingTime`: The error spending time at each analysis.
  - – `allocationRatioPlanned`: Allocation ratio for the active treatment versus control.
  - – `rounding`: Whether to round up sample size.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: fixed design
(design1 <- getDesignWilcoxon(
  beta = 0.1, n = NA,
```

```
  pLarger = pnorm((8 - 2)/sqrt(2*25^2)), alpha = 0.025))

# Example 2: group sequential design
(design2 <- getDesignWilcoxon(
  beta = 0.1, n = NA,
  pLarger = pnorm((8 - 2)/sqrt(2*25^2)), alpha = 0.025,
  kMax = 3, typeAlphaSpending = "sfOF"))
```

getDurationFromNevents

Range of Accrual Duration for Target Number of Events

Description

Obtains a range of accrual duration to reach the target number of events.

Usage

```
getDurationFromNevents(
  nevents = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  npoints = 23L
)
```

Arguments

nevents   The target number of events.

allocationRatioPlanned

                    Allocation ratio for the active treatment versus control. Defaults to 1 for equal
                    randomization.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time
                    intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual
                    intervals: [0, 3) and [3, Inf).

accrualIntensity

                    A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

> A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

> A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1   A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.

lambda2   A vector of hazard rates for the event in each analysis time interval by stratum for the control group.

gamma1   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.

gamma2   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

followupTime   Follow-up time for the last enrolled subjects. Must be provided for fixed follow-up design.

fixedFollowup   Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

npoints   The number of accrual duration time points. Defaults to 23.

Value

A data frame of the following variables:

- nevents: The target number of events.
- fixedFollowup: Whether a fixed follow-up design is used.
- accrualDuration: The accrual duration.
- subjects: The total number of subjects.
- followupTime: The follow-up time for the last enrolled subject.
- studyDuration: The study duration.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Piecewise accrual, piecewise exponential survivals, and 5% dropout by
# the end of 1 year.

getDurationFromNevents(
  nevents = 80, allocationRatioPlanned = 1,
  accrualTime = seq(0, 8),
  accrualIntensity = 26/9*seq(1, 9),
```

```
    piecewiseSurvivalTime = c(0, 6),
    lambda1 = c(0.0533, 0.0309),
    lambda2 = c(0.0533, 0.0533),
    gamma1 = -log(1-0.05)/12,
    gamma2 = -log(1-0.05)/12,
    fixedFollowup = FALSE)
```

getNeventsFromHazardRatio

Required Number of Events Given Hazard Ratio

Description

Obtains the required number of events given the hazard ratios under the null and alternative hypotheses for a group sequential design.

Usage

```
getNeventsFromHazardRatio(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_,
  hazardRatioH0 = 1,
  hazardRatio = NA_real_,
  allocationRatioPlanned = 1,
  rounding = 1L
)
```

Arguments

beta   Type II error. Defaults to 0.2.

kMax   The maximum number of stages.

informationRates

                The information rates in terms of number of events. Fixed prior to the trial.
                Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

    Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

    Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues   Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha   The significance level. Defaults to 0.025.

typeAlphaSpending

    The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

    The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

    The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds   Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

    The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

    The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

    The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

hazardRatioH0   Hazard ratio under the null hypothesis for the active treatment versus control. Defaults to 1 for superiority test.

hazardRatio   Hazard ratio under the alternative hypothesis for the active treatment versus control.

allocationRatioPlanned

    Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

rounding   Whether to round up the number of events. Defaults to 1 for rounding.

Value

The required number of events.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
getNeventsFromHazardRatio(
  beta = 0.2, kMax = 2,
  informationRates = c(0.5,1),
  alpha = 0.025, typeAlphaSpending = "sfOF",
  typeBetaSpending = "sfP",
  hazardRatio = 0.673)
```

getRCI   *Repeated Confidence Interval for Group Sequential Design*

Description

Obtains the repeated confidence interval for a group sequential trial.

Usage

```
getRCI(
  L = NA_integer_,
  zL = NA_real_,
  IMax = NA_real_,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

Arguments

L	The look of interest.
zL	The z-test statistic at the look.
IMax	The maximum information of the trial.
informationRates	
	The information rates up to look L.

efficacyStopping

> Indicators of whether efficacy stopping is allowed at each stage up to look L. Defaults to true if left unspecified.

criticalValues The upper boundaries on the z-test statistic scale for efficacy stopping up to look L.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending

> The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

> The parameter value of alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

spendingTime The error spending time up to look L. Defaults to missing, in which case, it is the same as informationRates.

Value

A data frame with the following components:

- pvalue: Repeated p-value for rejecting the null hypothesis.
- thetahat: Point estimate of the parameter.
- cilevel: Confidence interval level.
- lower: Lower bound of repeated confidence interval.
- upper: Upper bound of repeated confidence interval.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Christopher Jennison and Bruce W. Turnbull. Interim analyses: the repeated confidence interval approach (with discussion). J R Stat Soc Series B. 1989;51:305-361.

Examples

```
# group sequential design with 90% power to detect delta = 6
delta = 6
sigma = 17
n = 282
(des1 = getDesign(IMax = n/(4*sigma^2), theta = delta, kMax = 3,
                  alpha = 0.05, typeAlphaSpending = "sfHSD",
                  parameterAlphaSpending = -4))
```

```
# results at the second look
L = 2
n1 = n*2/3
delta1 = 7
sigma1 = 20
zL = delta1/sqrt(4/n1*sigma1^2)

# repeated confidence interval
getRCI(L = L, zL = zL, IMax = n/(4*sigma1^2),
       informationRates = c(1/3, 2/3), alpha = 0.05,
       typeAlphaSpending = "sfHSD", parameterAlphaSpending = -4)
```

---

heart   *Stanford heart transplant data from the survival package*

Description

Survival of patients on the waiting list for the Stanford heart transplant program.

start, stop, event entry and exit time and status for the time interval

age age-48 years

year year of acceptance (in years after Nov 1, 1967)

surgery prior bypass surgery 1=yes, 0=no

transplant received transplant 1=yes, 0=no

id patient id

Usage

heart

Format

An object of class data.frame with 172 rows and 8 columns.

---

hedgesg   *Hedges' g Effect Size*

Description

Obtains Hedges' g estimate and confidence interval of effect size.

Usage

```
hedgesg(tstat, m, ntilde, cilevel = 0.95)
```

Arguments

tstat	The value of the t-test statistic for comparing two treatment conditions.
m	The degrees of freedom for the t-test.
ntilde	The normalizing sample size to convert the standardized treatment difference to the t-test statistic, i.e., tstat = sqrt(ntilde)*meanDiff/stDev.
cilevel	The confidence interval level. Defaults to 0.95.

Details

Hedges' g is an effect size measure commonly used in meta-analysis to quantify the difference between two groups. It's an improvement over Cohen's d, particularly when dealing with small sample sizes.

The formula for Hedges' g is

$$g = c(m)d,$$

where d is Cohen's d effect size estimate, and $c(m)$ is the bias correction factor,

$$d = (\hat{\mu}_1 - \hat{\mu}_2)/\hat{\sigma},$$

$$c(m) = 1 - \frac{3}{4m - 1}.$$

Since $c(m) < 1$, Cohen's d overestimates the true effect size. $\delta = (\mu_1 - \mu_2)/\sigma$. Since

$$t = \sqrt{\tilde{n}}d,$$

we have

$$g = \frac{c(m)}{\sqrt{\tilde{n}}}t,$$

where t has a noncentral t distribution with m degrees of freedom and noncentrality parameter $\sqrt{\tilde{n}}\delta$.

The asymptotic variance of g can be approximated by

$$Var(g) = \frac{1}{\tilde{n}} + \frac{g^2}{2m}.$$

The confidence interval for δ can be constructed using normal approximation.

For two-sample mean difference with sample size n_1 for the treatment group and n_2 for the control group, we have $\tilde{n} = \frac{n_1 n_2}{n_1 + n_2}$ and $m = n_1 + n_2 - 2$ for pooled variance estimate.

Value

A data frame with the following variables:

- tstat: The value of the t test statistic.
- m: The degrees of freedom for the t-test.
- ntilde: The normalizing sample size to convert the standardized treatment difference to the t-test statistic.
- g: Hedges' g effect size estimate.

- `varg`: Variance of g.
- `lower`: The lower confidence limit for effect size.
- `upper`: The upper confidence limit for effect size.
- `cilevel`: The confidence interval level.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Larry V. Hedges. Distribution theory for Glass's estimator of effect size and related estimators. Journal of Educational Statistics 1981; 6:107-128.

Examples

```
n1 = 7
n2 = 8
meanDiff = 0.444
stDev = 1.201
m = n1+n2-2
ntilde = n1*n2/(n1+n2)
tstat = sqrt(ntilde)*meanDiff/stDev

hedgesg(tstat, m, ntilde)
```

---

immdef   *Simulated CONCORDE trial data from the rpsftm package*

Description

Patients were randomly assigned to receive treatment immediately or deferred, and those in the deferred arm could cross over and receive treatment. The primary endpoint was time to disease progression.

`id` Patient identification number

`def` Indicator that the participant was assigned to the deferred treatment arm

`imm` Indicator that the participant was assigned to the immediate treatment arm

`censyrs` The censoring time, in years, corresponding to the close of study minus the time of entry for each patient

`xo` Indicator that crossover occurred

`xoyrs` The time, in years, from entry to switching, or 0 for patients in the immediate arm

`prog` Indicator of disease progression (1), or censoring (0)

`progyrs` Time, in years, from entry to disease progression or censoring

`entry` The time of entry into the study, measured in years from the date of randomisation

Usage

```
immdef
```

Format

An object of class data.frame with 1000 rows and 9 columns.

---

ingots   *The binary data from Cox and Snell (1989, pp. 10-11).*

Description

The dataset consits of the number of ingots not ready for rolling and the number of ingots ready for rolling for a number of combinations of heating time and soaking time.

Usage

```
ingots
```

Format

An object of class tbl_df (inherits from tbl, data.frame) with 25 rows and 4 columns.

Details

Heat The heating time

Soak The soaking time

NotReady Response indicator, with a value 1 for units not ready for rolling (event) and a value of 0 for units ready for rolling (nonevent)

Freq The frequency of occurrence of each combination of Heat, Soak, and NotReady

---

kmdiff   *Estimate of Milestone Survival Difference*

Description

Obtains the estimate of milestone survival difference between two treatment groups.

Usage

```
kmdiff(
  data,
  rep = "",
  stratum = "",
  treat = "treat",
  time = "time",
  event = "event",
  milestone = NA_real_,
  survDiffH0 = 0,
  conflev = 0.95
)
```

Arguments

data	The input data frame that contains the following variables:

- rep: The replication for by-group processing.
- stratum: The stratum.
- treat: The treatment.
- time: The possibly right-censored survival time.
- event: The event indicator.

rep	The name of the replication variable in the input data.
stratum	The name of the stratum variable in the input data.
treat	The name of the treatment variable in the input data.
time	The name of the time variable in the input data.
event	The name of the event variable in the input data.
milestone	The milestone time at which to calculate the survival probability.
survDiffH0	The difference in milestone survival probabilities under the null hypothesis. Defaults to 0 for superiority test.
conflev	The level of the two-sided confidence interval for the difference in milestone survival probabilities. Defaults to 0.95.

Value

A data frame with the following variables:

- rep: The replication.
- milestone: The milestone time relative to randomization.
- survDiffH0: The difference in milestone survival probabilities under the null hypothesis.
- surv1: The estimated milestone survival probability for the treatment group.
- surv2: The estimated milestone survival probability for the control group.
- survDiff: The estimated difference in milestone survival probabilities.
- vsurv1: The variance for surv1.

- vsurv2: The variance for surv2.

- vsurvDiff: The variance for survDiff.

- survDiffZ: The Z-statistic value.

- survDiffPValue: The one-sided p-value.

- lower: The lower bound of confidence interval.

- upper: The upper bound of confidence interval.

- conflev: The level of confidence interval.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
df <- kmdiff(data = rawdata, rep = "iterationNumber",
            stratum = "stratum", treat = "treatmentGroup",
            time = "timeUnderObservation", event = "event",
            milestone = 12)
head(df)
```

---

kmest   *Kaplan-Meier Estimates of Survival Curve*

Description

Obtains the Kaplan-Meier estimates of the survival curve.

Usage

```
kmest(
  data,
  rep = "",
  stratum = "",
  time = "time",
  event = "event",
  conftype = "log-log",
  conflev = 0.95,
  keep_censor = 0L
)
```

Arguments

`data`	The input data frame that contains the following variables:

- `rep`: The replication for by-group processing.
- `stratum`: The stratum.
- `time`: The possibly right-censored survival time.
- `event`: The event indicator.

`rep`	The name(s) of the replication variable(s) in the input data.
`stratum`	The name(s) of the stratum variable(s) in the input data.
`time`	The name of the time variable in the input data.
`event`	The name of the event variable in the input data.
`conftype`	The type of the confidence interval. One of "none", "plain", "log", "log-log" (the default), or "arcsin". The arcsin option bases the intervals on asin(sqrt(survival)).
`conflev`	The level of the two-sided confidence interval for the survival probabilities. Defaults to 0.95.
`keep_censor`	Whether to retain the censoring time in the output data frame.

Value

A data frame with the following variables:

- `size`: The number of subjects in the stratum.
- `time`: The event time.
- `nrisk`: The number of subjects at risk.
- `nevent`: The number of subjects having the event.
- `ncensor`: The number of censored subjects.
- `survival`: The Kaplan-Meier estimate of the survival probability.
- `stderr`: The standard error of the estimated survival probability based on the Greendwood formula.
- `lower`: The lower bound of confidence interval if requested.
- `upper`: The upper bound of confidence interval if requested.
- `conflev`: The level of confidence interval if requested.
- `conftype`: The type of confidence interval if requested.
- `stratum`: The stratum.
- `rep`: The replication.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
kmest(data = aml, stratum = "x", time = "time", event = "status")
```

kmpower   *Power for Difference in Milestone Survival Probabilities*

Description

Estimates the power for testing the difference in milestone survival probabilities in a two-sample survival design.

Usage

```
kmpower(
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  milestone = NA_real_,
  survDiffH0 = 0,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  spendingTime = NA_real_,
  studyDuration = NA_real_
)
```

Arguments

kMax   The maximum number of stages.

informationRates

            The information rates. Defaults to `(1:kMax) / kMax` if left unspecified.

efficacyStopping

        Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

        Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues   Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha   The significance level. Defaults to 0.025.

typeAlphaSpending

        The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

        The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

        The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds   Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

        The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

        The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

milestone   The milestone time at which to calculate the survival probability.

survDiffH0   The difference in milestone survival probabilities under the null hypothesis. Defaults to 0 for superiority test.

allocationRatioPlanned

        Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

        A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

        A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

    A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1   A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.

lambda2   A vector of hazard rates for the event in each analysis time interval by stratum for the control group.

gamma1   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.

gamma2   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration

    Duration of the enrollment period.

followupTime   Follow-up time for the last enrolled subject.

fixedFollowup   Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

studyDuration   Study duration for fixed follow-up design. Defaults to missing, which is to be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and followupTime.

Value

An S3 class kmpower object with 4 components:

- overallResults: A data frame containing the following variables:
    - overallReject: The overall rejection probability.
    - alpha: The overall significance level.
    - numberOfEvents: The total number of events.
    - numbeOfSubjects: The total number of subjects.
    - studyDuration: The total study duration.
    - information: The maximum information.
    - expectedNumberOfEvents: The expected number of events.
    - expectedNumberOfSubjects: The expected number of subjects.
    - expectedStudyDuration: The expected study duration.
    - expectedInformation: The expected information.
    - accrualDuration: The accrual duration.
    - followupTime: The follow-up duration.
    - fixedFollowup: Whether a fixed follow-up design is used.
    - kMax: The number of stages.
    - milestone: The milestone time relative to randomization.

- – survDiffH0: The difference in milestone survival probabilities under the null hypothesis.
- – surv1: The milestone survival probability for the treatment group.
- – surv2: The milestone survival probability for the control group.
- – survDiff: The difference in milestone survival probabilities, equal to surv1 - surv2.

- byStageResults: A data frame containing the following variables:
  - – informationRates: The information rates.
  - – efficacyBounds: The efficacy boundaries on the Z-scale.
  - – futilityBounds: The futility boundaries on the Z-scale.
  - – rejectPerStage: The probability for efficacy stopping.
  - – futilityPerStage: The probability for futility stopping.
  - – cumulativeRejection: The cumulative probability for efficacy stopping.
  - – cumulativeFutility: The cumulative probability for futility stopping.
  - – cumulativeAlphaSpent: The cumulative alpha spent.
  - – numberOfEvents: The number of events.
  - – numberOfDropouts: The number of dropouts.
  - – numberOfSubjects: The number of subjects.
  - – numberOfMilestone: The number of subjects reaching milestone.
  - – analysisTime: The average time since trial start.
  - – efficacySurvDiff: The efficacy boundaries on the survival difference scale.
  - – futilitySurvDiff: The futility boundaries on the survival difference scale.
  - – efficacyP: The efficacy boundaries on the p-value scale.
  - – futilityP: The futility boundaries on the p-value scale.
  - – information: The cumulative information.
  - – efficacyStopping: Whether to allow efficacy stopping.
  - – futilityStopping: Whether to allow futility stopping.

- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, typeBetaSpending, parameterBetaSpending, allocationRatioPlanned, accrualTime, accuralIntensity, piecewiseSurvivalTime, stratumFraction, lambda1, lambda2, gamma1, gamma2, and spendingTime.

- byTreatmentCounts: A list containing the following counts by treatment group:
  - – numberOfEvents1: The number of events by stage for the treatment group.
  - – numberOfDropouts1: The number of dropouts by stage for the treatment group.
  - – numberOfSubjects1: The number of subjects by stage for the treatment group.
  - – numberOfMilestone1: The number of subjects reaching milestone by stage for the active treatment group.
  - – numberOfEvents2: The number of events by stage for the control group.
  - – numberOfDropouts2: The number of dropouts by stage for the control group.
  - – numberOfSubjects2: The number of subjects by stage for the control group.
  - – numberOfMilestone2: The number of subjects reaching milestone by stage for the control group.
  - – expectedNumberOfEvents1: The expected number of events for the treatment group.
  - – expectedNumberOfDropouts1: The expected number of dropouts for the active treatment group.

- expectedNumberOfSubjects1: The expected number of subjects for the active treatment group.

- expectedNumberOfMilestone1: The expected number of subjects reaching milestone for the active treatment group.

- expectedNumberOfEvents2: The expected number of events for control group.

- expectedNumberOfDropouts2: The expected number of dropouts for the control group.

- expectedNumberOfSubjects2: The expected number of subjects for the control group.

- expectedNumberOfMilestone2: The expected number of subjects reaching milestone for the control group.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Piecewise accrual, piecewise exponential survival, and 5% dropout by
# the end of 1 year.

kmpower(kMax = 2, informationRates = c(0.8, 1),
        alpha = 0.025, typeAlphaSpending = "sfOF",
        milestone = 18,
        allocationRatioPlanned = 1, accrualTime = seq(0, 8),
        accrualIntensity = 26/9*seq(1, 9),
        piecewiseSurvivalTime = c(0, 6),
        stratumFraction = c(0.2, 0.8),
        lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
        lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
        gamma1 = -log(1-0.05)/12,
        gamma2 = -log(1-0.05)/12, accrualDuration = 22,
        followupTime = 18, fixedFollowup = FALSE)
```

---

kmpower1s   *Power for One-Sample Milestone Survival Probability*

Description

Estimates the power, stopping probabilities, and expected sample size in a one-group survival design.

Usage

```
kmpower1s(
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
```

```
    criticalValues = NA_real_,
    alpha = 0.025,
    typeAlphaSpending = "sfOF",
    parameterAlphaSpending = NA_real_,
    userAlphaSpending = NA_real_,
    futilityBounds = NA_real_,
    typeBetaSpending = "none",
    parameterBetaSpending = NA_real_,
    milestone = NA_real_,
    survH0 = NA_real_,
    accrualTime = 0L,
    accrualIntensity = NA_real_,
    piecewiseSurvivalTime = 0L,
    stratumFraction = 1L,
    lambda = NA_real_,
    gamma = 0L,
    accrualDuration = NA_real_,
    followupTime = NA_real_,
    fixedFollowup = 0L,
    spendingTime = NA_real_,
    studyDuration = NA_real_
)
```

Arguments

kMax   The maximum number of stages.

informationRates

                  The information rates. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

                  Indicators of whether efficacy stopping is allowed at each stage. Defaults to true
                  if left unspecified.

futilityStopping

                  Indicators of whether futility stopping is allowed at each stage. Defaults to true
                  if left unspecified.

criticalValues   Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha   The significance level. Defaults to 0.025.

typeAlphaSpending

                  The type of alpha spending. One of the following: "OF" for O'Brien-Fleming
                  boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries,
                  "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spend-
                  ing function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang,
                  Shi & DeCani spending function, "user" for user defined spending, and "none"
                  for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

                  The parameter value for the alpha spending. Corresponds to Delta for "WT",
                  rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds   Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

milestone   The milestone time at which to calculate the survival probability.

survH0   The milestone survival probability under the null hypothesis.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda   A vector of hazard rates for the event in each analysis time interval by stratum under the alternative hypothesis.

gamma   The hazard rate for exponential dropout or a vector of hazard rates for piecewise exponential dropout. Defaults to 0 for no dropout.

accrualDuration

Duration of the enrollment period.

followupTime   Follow-up time for the last enrolled subject.

fixedFollowup   Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

studyDuration   Study duration for fixed follow-up design. Defaults to missing, which is to be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and followupTime.

Value

An S3 class kmpower1s object with 3 components:

- `overallResults`: A data frame containing the following variables:
    - `overallReject`: The overall rejection probability.
    - `alpha`: The overall significance level.
    - `numberOfEvents`: The total number of events.
    - `numbeOfSubjects`: The total number of subjects.
    - `numberOfMilestone`: The total number of subjects reaching milestone.
    - `studyDuration`: The total study duration.
    - `information`: The maximum information.
    - `expectedNumberOfEvents`: The expected number of events.
    - `expectedNumberOfSubjects`: The expected number of subjects.
    - `expectedNumberOfMilestone`: The expected number of subjects reaching milestone.
    - `expectedStudyDuration`: The expected study duration.
    - `expectedInformation`: The expected information.
    - `accrualDuration`: The accrual duration.
    - `followupTime`: The follow-up duration.
    - `fixedFollowup`: Whether a fixed follow-up design is used.
    - `kMax`: The number of stages.
    - `milestone`: The milestone time to calculate the survival probability.
    - `survH0`: The milestone survival probability under the null hypothesis.
    - `surv`: The milestone survival probability under the alternative hypothesis.
- `byStageResults`: A data frame containing the following variables:
    - `informationRates`: The information rates.
    - `efficacyBounds`: The efficacy boundaries on the Z-scale.
    - `futilityBounds`: The futility boundaries on the Z-scale.
    - `rejectPerStage`: The probability for efficacy stopping.
    - `futilityPerStage`: The probability for futility stopping.
    - `cumulativeRejection`: The cumulative probability for efficacy stopping.
    - `cumulativeFutility`: The cumulative probability for futility stopping.
    - `cumulativeAlphaSpent`: The cumulative alpha spent.
    - `numberOfEvents`: The number of events.
    - `numberOfDropouts`: The number of dropouts.
    - `numberOfSubjects`: The number of subjects.
    - `numberOfMilestone`: The number of subjects reaching milestone.
    - `analysisTime`: The average time since trial start.
    - `efficacySurv`: The efficacy boundaries on the milestone survival probability scale.
    - `futilitySurv`: The futility boundaries on the milestone survival probability scale.
    - `efficacyP`: The efficacy boundaries on the p-value scale.
    - `futilityP`: The futility boundaries on the p-value scale.
    - `information`: The cumulative information.
    - `efficacyStopping`: Whether to allow efficacy stopping.
    - `futilityStopping`: Whether to allow futility stopping.
- `settings`: A list containing the following input parameters: `typeAlphaSpending`, `parameterAlphaSpending`, `userAlphaSpending`, `typeBetaSpending`, `parameterBetaSpending`, `accrualTime`, `accuralIntensity`, `piecewiseSurvivalTime`, `stratumFraction`, `lambda`, `gamma`, and `spendingTime`.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

See Also

kmstat

Examples

```
kmpower1s(kMax = 2, informationRates = c(0.8, 1),
          alpha = 0.025, typeAlphaSpending = "sfOF",
          milestone = 18, survH0 = 0.30,
          accrualTime = seq(0, 8),
          accrualIntensity = 26/9*seq(1, 9),
          piecewiseSurvivalTime = c(0, 6),
          stratumFraction = c(0.2, 0.8),
          lambda = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
          gamma = -log(1-0.05)/12, accrualDuration = 22,
          followupTime = 18, fixedFollowup = FALSE)
```

---

kmpowerequiv | *Power for Equivalence in Milestone Survival Probability Difference*

Description

Obtains the power for equivalence in milestone survival probability difference.

Usage

```
kmpowerequiv(
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  milestone = NA_real_,
  survDiffLower = NA_real_,
  survDiffUpper = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
```

```
    gamma1 = 0L,
    gamma2 = 0L,
    accrualDuration = NA_real_,
    followupTime = NA_real_,
    fixedFollowup = 0L,
    spendingTime = NA_real_,
    studyDuration = NA_real_
)
```

Arguments

kMax   The maximum number of stages.

informationRates
                     The information rates. Defaults to (1:kMax) / kMax if left unspecified.

criticalValues   Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha   The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending
                     The type of alpha spending. One of the following: "OF" for O'Brien-Fleming
                     boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries,
                     "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spend-
                     ing function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang,
                     Shi & DeCani spending function, "user" for user defined spending, and "none"
                     for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending
                     The parameter value for the alpha spending. Corresponds to Delta for "WT",
                     rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending
                     The user defined alpha spending. Cumulative alpha spent up to each stage.

milestone   The milestone time at which to calculate the survival probability.

survDiffLower   The lower equivalence limit of milestone survival probability difference.

survDiffUpper   The upper equivalence limit of milestone survival probability difference.

allocationRatioPlanned
                     Allocation ratio for the active treatment versus control. Defaults to 1 for equal
                     randomization.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time
                     intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual
                     intervals: [0, 3) and [3, Inf).

accrualIntensity
                     A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime
                     A vector that specifies the starting time of piecewise exponential survival time
                     intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event
                     intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction
                     A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
```

| lambda1 | A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group. |
|---|---|
| lambda2 | A vector of hazard rates for the event in each analysis time interval by stratum for the control group. |
| gamma1 | The hazard rate for exponential dropout, a vector of hazard rates for piece-wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group. |
| gamma2 | The hazard rate for exponential dropout, a vector of hazard rates for piece-wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group. |
| accrualDuration | |
| | Duration of the enrollment period. |
| followupTime | Follow-up time for the last enrolled subject. |
| fixedFollowup | Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up. |
| spendingTime | A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates. |
| studyDuration | Study duration for fixed follow-up design. Defaults to missing, which is to be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and followupTime. |

**Value**

An S3 class kmpowerequiv object with 4 components:

- overallResults: A data frame containing the following variables:
    - overallReject: The overall rejection probability.
    - alpha: The overall significance level.
    - numberOfEvents: The total number of events.
    - numberOfSubjects: The total number of subjects.
    - studyDuration: The total study duration.
    - information: The maximum information.
    - expectedNumberOfEvents: The expected number of events.
    - expectedNumberOfSubjects: The expected number of subjects.
    - expectedStudyDuration: The expected study duration.
    - expectedInformation: The expected information.
    - kMax: The number of stages.
    - milestone: The milestone time relative to randomization.
    - survDiffLower: The lower equivalence limit of milestone survival probability difference.
    - survDiffUpper: The upper equivalence limit of milestone survival probability difference.
    - surv1: The milestone survival probability for the treatment group.

- – surv2: The milestone survival probability for the control group.
- – survDiff: The milestone survival probability difference.
- – accrualDuration: The accrual duration.
- – followupTime: The follow-up duration.
- – fixedFollowup: Whether a fixed follow-up design is used.

- byStageResults: A data frame containing the following variables:
  - – informationRates: The information rates.
  - – efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - – rejectPerStage: The probability for efficacy stopping.
  - – cumulativeRejection: The cumulative probability for efficacy stopping.
  - – cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - – cumulativeAttainedAlphaH10: The cumulative alpha attained under H10.
  - – cumulativeAttainedAlphaH20: The cumulative alpha attained under H20.
  - – numberOfEvents: The number of events.
  - – numberOfDropouts: The number of dropouts.
  - – numberOfSubjects: The number of subjects.
  - – numberOfMilestone: The number of subjects reaching milestone.
  - – analysisTime: The average time since trial start.
  - – efficacySurvDiffLower: The efficacy boundaries on the milestone survival probability difference scale for the one-sided null hypothesis at the lower equivalence limit.
  - – efficacySurvDiffUpper: The efficacy boundaries on the milestone survival probability difference scale for the one-sided null hypothesis at the upper equivalence limit.
  - – efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - – information: The cumulative information.

- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, allocationRatioPlanned, accrualTime, accuralIntensity, piecewiseSurvivalTime, stratumFraction, lambda1, lambda2, gamma1, gamma2, and spendingTime.

- byTreatmentCounts: A list containing the following counts by treatment group:
  - – numberOfEvents1: The number of events by stage for the treatment group.
  - – numberOfDropouts1: The number of dropouts by stage for the treatment group.
  - – numberOfSubjects1: The number of subjects by stage for the treatment group.
  - – numberOfMilestone1: The number of subjects reaching milestone by stage for the active treatment group.
  - – numberOfEvents2: The number of events by stage for the control group.
  - – numberOfDropouts2: The number of dropouts by stage for the control group.
  - – numberOfSubjects2: The number of subjects by stage for the control group.
  - – numberOfMilestone2: The number of subjects reaching milestone by stage for the control group.
  - – expectedNumberOfEvents1: The expected number of events for the treatment group.
  - – expectedNumberOfDropouts1: The expected number of dropouts for the active treatment group.

  – expectedNumberOfSubjects1: The expected number of subjects for the active treatment group.

  – expectedNumberOfMilestone1: The expected number of subjects reaching milestone for the active treatment group.

  – expectedNumberOfEvents2: The expected number of events for control group.

  – expectedNumberOfDropouts2: The expected number of dropouts for the control group.

  – expectedNumberOfSubjects2: The expected number of subjects for the control group.

  – expectedNumberOfMilestone2: The expected number of subjects reaching milestone for the control group.

## Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

## See Also

[kmstat](kmstat)

## Examples

```
kmpowerequiv(kMax = 2, informationRates = c(0.5, 1),
             alpha = 0.05, typeAlphaSpending = "sfOF",
             milestone = 18,
             survDiffLower = -0.13, survDiffUpper = 0.13,
             allocationRatioPlanned = 1, accrualTime = seq(0, 8),
             accrualIntensity = 26/9*seq(1, 9),
             piecewiseSurvivalTime = c(0, 6),
             stratumFraction = c(0.2, 0.8),
             lambda1 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
             lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
             gamma1 = -log(1-0.05)/12,
             gamma2 = -log(1-0.05)/12, accrualDuration = 22,
             followupTime = 18, fixedFollowup = FALSE)
```

---

kmsamplesize   *Sample Size for Difference in Milestone Survival Probabilities*

Description

Obtains the needed accrual duration given power, accrual intensity, and follow-up time, the needed follow-up time given power, accrual intensity, and accrual duration, or the needed absolute accrual intensity given power, relative accrual intensity, accrual duration, and follow-up time in a two-group survival design.

Usage

```
kmsamplesize(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  milestone = NA_real_,
  survDiffH0 = 0,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  interval = as.numeric(c(0.001, 240)),
  spendingTime = NA_real_,
  rounding = 1L
)
```

Arguments

beta	Type II error. Defaults to 0.2.
kMax	The maximum number of stages.
informationRates	
	The information rates. Defaults to (1:kMax) / kMax if left unspecified.
efficacyStopping	
	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	
	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues   Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha   The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds   Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

milestone   The milestone time at which to calculate the survival probability.

survDiffH0   The difference in milestone survival probabilities under the null hypothesis. Defaults to 0 for superiority test.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1	A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.
lambda2	A vector of hazard rates for the event in each analysis time interval by stratum for the control group.
gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.
gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.
accrualDuration	
	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
interval	The interval to search for the solution of accrualDuration, followupTime, or the proportionality constant of accrualIntensity. Defaults to `c(0.001, 240)`.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as `informationRates`.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.

Value

A list of two components:

- `resultsUnderH1`: An S3 class kmpower object under the alternative hypothesis.
- `resultsUnderH0`: An S3 class kmpower object under the null hypothesis.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

See Also

kmpower

Examples

```
# Example 1: Obtains follow-up time given power, accrual intensity,
# and accrual duration for variable follow-up. Of note, the power
# reaches the maximum when the follow-up time equals milestone.

kmsamplesize(beta = 0.25, kMax = 2, informationRates = c(0.8, 1),
             alpha = 0.025, typeAlphaSpending = "sfOF",
             milestone = 18,
             allocationRatioPlanned = 1, accrualTime = seq(0, 8),
             accrualIntensity = 26/9*seq(1, 9),
             piecewiseSurvivalTime = c(0, 6),
```

```
                stratumFraction = c(0.2, 0.8),
                lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
                lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
                gamma1 = -log(1-0.05)/12,
                gamma2 = -log(1-0.05)/12, accrualDuration = 22,
                followupTime = NA, fixedFollowup = FALSE)

# Example 2: Obtains accrual intensity given power, accrual duration, and
# follow-up time for variable follow-up

kmsamplesize(beta = 0.2, kMax = 2, informationRates = c(0.8, 1),
                alpha = 0.025, typeAlphaSpending = "sfOF",
                milestone = 18,
                allocationRatioPlanned = 1, accrualTime = seq(0, 8),
                accrualIntensity = 26/9*seq(1, 9),
                piecewiseSurvivalTime = c(0, 6),
                stratumFraction = c(0.2, 0.8),
                lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
                lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
                gamma1 = -log(1-0.05)/12,
                gamma2 = -log(1-0.05)/12, accrualDuration = 22,
                followupTime = 18, fixedFollowup = FALSE)


# Example 3: Obtains accrual duration given power, accrual intensity, and
# follow-up time for fixed follow-up

kmsamplesize(beta = 0.2, kMax = 2, informationRates = c(0.8, 1),
                alpha = 0.025, typeAlphaSpending = "sfOF",
                milestone = 18,
                allocationRatioPlanned = 1, accrualTime = seq(0, 8),
                accrualIntensity = 26/9*seq(1, 9),
                piecewiseSurvivalTime = c(0, 6),
                stratumFraction = c(0.2, 0.8),
                lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
                lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
                gamma1 = -log(1-0.05)/12,
                gamma2 = -log(1-0.05)/12, accrualDuration = NA,
                followupTime = 18, fixedFollowup = TRUE)
```

---

kmsamplesize1s *Sample Size for One-Sample Milestone Survival Probability*

Description

Obtains the needed accrual duration given power and follow-up time, the needed follow-up time given power and accrual duration, or the needed absolute accrual rates given power, accrual duration, follow-up duration, and relative accrual rates in a one-group survival design.

Usage

```
kmsamplesize1s(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  milestone = NA_real_,
  survH0 = NA_real_,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda = NA_real_,
  gamma = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  interval = as.numeric(c(0.001, 240)),
  spendingTime = NA_real_,
  rounding = 1L
)
```

Arguments

beta	Type II error. Defaults to 0.2.
kMax	The maximum number of stages.
informationRates	
	The information rates. Defaults to (1:kMax) / kMax if left unspecified.
efficacyStopping	
	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	
	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.

typeAlphaSpending

    The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

    The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

    The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

    The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

    The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

    The user defined beta spending. Cumulative beta spent up to each stage.

milestone   The milestone time at which to calculate the survival probability.

survH0   The milestone survival probability under the null hypothesis.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

    A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

    A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

    A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda   A vector of hazard rates for the event in each analysis time interval by stratum under the alternative hypothesis.

gamma   The hazard rate for exponential dropout or a vector of hazard rates for piecewise exponential dropout. Defaults to 0 for no dropout.

accrualDuration

    Duration of the enrollment period.

followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
interval	The interval to search for the solution of accrualDuration, followupDuration, or the proportionality constant of accrualIntensity. Defaults to `c(0.001, 240)`.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as `informationRates`.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.

Value

A list of two components:

- resultsUnderH1: An S3 class kmpower1s object under the alternative hypothesis.
- resultsUnderH0: An S3 class kmpower1s object under the null hypothesis.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

See Also

kmpower1s

Examples

```
# Example 1: Obtains follow-up duration given power, accrual intensity,
# and accrual duration for variable follow-up

kmsamplesize1s(beta = 0.2, kMax = 2,
               informationRates = c(0.8, 1),
               alpha = 0.025, typeAlphaSpending = "sfOF",
               milestone = 18, survH0 = 0.30,
               accrualTime = seq(0, 8),
               accrualIntensity = 26/9*seq(1, 9),
               piecewiseSurvivalTime = c(0, 6),
               stratumFraction = c(0.2, 0.8),
               lambda = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
               gamma = -log(1-0.05)/12, accrualDuration = 22,
               followupTime = NA, fixedFollowup = FALSE)

# Example 2: Obtains accrual intensity given power, accrual duration, and
# follow-up duration for variable follow-up

kmsamplesize1s(beta = 0.2, kMax = 2,
               informationRates = c(0.8, 1),
               alpha = 0.025, typeAlphaSpending = "sfOF",
               milestone = 18, survH0 = 0.30,
               accrualTime = seq(0, 8),
               accrualIntensity = 26/9*seq(1, 9),
               piecewiseSurvivalTime = c(0, 6),
```

```
                    stratumFraction = c(0.2, 0.8),
                    lambda = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
                    gamma = -log(1-0.05)/12, accrualDuration = 22,
                    followupTime = 18, fixedFollowup = FALSE)


# Example 3: Obtains accrual duration given power, accrual intensity, and
# follow-up duration for fixed follow-up

kmsamplesize1s(beta = 0.2, kMax = 2,
                    informationRates = c(0.8, 1),
                    alpha = 0.025, typeAlphaSpending = "sfOF",
                    milestone = 18, survH0 = 0.30,
                    accrualTime = seq(0, 8),
                    accrualIntensity = 26/9*seq(1, 9),
                    piecewiseSurvivalTime = c(0, 6),
                    stratumFraction = c(0.2, 0.8),
                    lambda = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
                    gamma = -log(1-0.05)/12, accrualDuration = NA,
                    followupTime = 18, fixedFollowup = TRUE)
```

---

kmsamplesizeequiv   *Sample Size for Equivalence in Milestone Survival Probability Differ-*
                          ence

Description

Obtains the sample size for equivalence in milestone survival probability difference.

Usage

```
kmsamplesizeequiv(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  milestone = NA_real_,
  survDiffLower = NA_real_,
  survDiffUpper = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
```

```
    lambda1 = NA_real_,
    lambda2 = NA_real_,
    gamma1 = 0L,
    gamma2 = 0L,
    accrualDuration = NA_real_,
    followupTime = NA_real_,
    fixedFollowup = 0L,
    interval = as.numeric(c(0.001, 240)),
    spendingTime = NA_real_,
    rounding = 1L
)
```

Arguments

beta	The type II error.
kMax	The maximum number of stages.
informationRates	
	The information rates. Defaults to (1:kMax) / kMax if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level for each of the two one-sided tests. Defaults to 0.05.
typeAlphaSpending	
	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	
	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	
	The user defined alpha spending. Cumulative alpha spent up to each stage.
milestone	The milestone time at which to calculate the survival probability.
survDiffLower	The lower equivalence limit of milestone survival probability difference.
survDiffUpper	The upper equivalence limit of milestone survival probability difference.
allocationRatioPlanned	
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).
accrualIntensity	
	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	
	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

               A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1   A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.

lambda2   A vector of hazard rates for the event in each analysis time interval by stratum for the control group.

gamma1   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.

gamma2   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration

               Duration of the enrollment period.

followupTime   Follow-up time for the last enrolled subject.

fixedFollowup   Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

interval   The interval to search for the solution of accrualDuration, followupDuration, or the proportionality constant of accrualIntensity. Defaults to `c(0.001, 240)`.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as `informationRates`.

rounding   Whether to round up sample size. Defaults to 1 for sample size rounding.

Value

An S3 class kmpowerequiv object

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

See Also

kmpowerequiv

Examples

```
kmsamplesizeequiv(beta = 0.1, kMax = 2, informationRates = c(0.5, 1),
                  alpha = 0.05, typeAlphaSpending = "sfOF",
                  milestone = 18,
                  survDiffLower = -0.13, survDiffUpper = 0.13,
                  allocationRatioPlanned = 1, accrualTime = seq(0, 8),
                  accrualIntensity = 26/9*seq(1, 9),
                  piecewiseSurvivalTime = c(0, 6),
                  stratumFraction = c(0.2, 0.8),
                  lambda1 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
                  lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
```

```
                    gamma1 = -log(1-0.05)/12,
                    gamma2 = -log(1-0.05)/12, accrualDuration = NA,
                    followupTime = 18, fixedFollowup = FALSE)
```

---

kmstat   *Stratified Difference in Milestone Survival Probabilities*

Description

Obtains the stratified milestone survival probabilities and difference in milestone survival probabilities at given calendar times.

Usage

```
kmstat(
  time = NA_real_,
  milestone = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L
)
```

Arguments

time   A vector of calendar times for data cut.

milestone   The milestone time at which to calculate the survival probability.

allocationRatioPlanned
                        Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity
                        A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

  A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

  A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1   A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.

lambda2   A vector of hazard rates for the event in each analysis time interval by stratum for the control group.

gamma1   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.

gamma2   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration

  Duration of the enrollment period.

followupTime   Follow-up time for the last enrolled subject.

fixedFollowup   Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

Value

A data frame containing the following variables:

- time: The calendar time since trial start.
- subjects: The number of enrolled subjects.
- nevents: The total number of events.
- nevents1: The number of events in the active treatment group.
- nevents2: The number of events in the control group.
- ndropouts: The total number of dropouts.
- ndropouts1: The number of dropouts in the active treatment group.
- ndropouts2: The number of dropouts in the control group.
- milestone: The milestone time relative to randomization.
- nmilestone: The total number of subjects reaching milestone.
- nmilestone1: The number of subjects reaching milestone in the active treatment group.
- nmiletone2: The number of subjects reaching milestone in the control group.
- surv1: The milestone survival probability for the treatment group.
- surv2: The milestone survival probability for the control group.
- survDiff: The difference in milestone survival probabilities, i.e., surv1 - surv2.
- vsurv1: The variance for surv1.

- vsurv2: The variance for `surv2`.

- vsurvDiff: The variance for `survDiff`.

- information: The information for `survDiff`, equal to `1/vsurvDiff`.

- survDiffZ: The Z-statistic value, i.e., `survDiff/sqrt(vsurvDiff)`.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Piecewise accrual, piecewise exponential survivals, and 5% dropout by
# the end of 1 year.

kmstat(time = c(22, 40),
       milestone = 18,
       allocationRatioPlanned = 1,
       accrualTime = seq(0, 8),
       accrualIntensity = 26/9*seq(1, 9),
       piecewiseSurvivalTime = c(0, 6),
       stratumFraction = c(0.2, 0.8),
       lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
       lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
       gamma1 = -log(1-0.05)/12,
       gamma2 = -log(1-0.05)/12,
       accrualDuration = 22,
       followupTime = 18, fixedFollowup = FALSE)
```

---

liferegr　　　　　　　　　　*Parametric Regression Models for Failure Time Data*

Description

Obtains the parameter estimates from parametric regression models with uncensored, right censored, left censored, or interval censored data.

Usage

```
liferegr(
  data,
  rep = "",
  stratum = "",
  time = "time",
  time2 = "",
  event = "event",
  covariates = "",
  weight = "",
```

```
    offset = "",
    id = "",
    dist = "weibull",
    robust = FALSE,
    plci = FALSE,
    alpha = 0.05
)
```

Arguments

data	The input data frame that contains the following variables:

- `rep`: The replication for by-group processing.
- `stratum`: The stratum.
- `time`: The follow-up time for right censored data, or the left end of each interval for interval censored data.
- `time2`: The right end of each interval for interval censored data.
- `event`: The event indicator, 1=event, 0=no event.
- `covariates`: The values of baseline covariates.
- `weight`: The weight for each observation.
- `offset`: The offset for each observation.
- `id`: The optional subject ID to group the score residuals in computing the robust sandwich variance.

rep	The name(s) of the replication variable(s) in the input data.
stratum	The name(s) of the stratum variable(s) in the input data.
time	The name of the time variable or the left end of each interval for interval censored data in the input data.
time2	The name of the right end of each interval for interval censored data in the input data.
event	The name of the event variable in the input data for right censored data.
covariates	The vector of names of baseline covariates in the input data.
weight	The name of the weight variable in the input data.
offset	The name of the offset variable in the input data.
id	The name of the id variable in the input data.
dist	The assumed distribution for time to event. Options include "exponential", "weibull", "lognormal", and "loglogistic" to be modeled on the log-scale, and "normal" and "logistic" to be modeled on the original scale.
robust	Whether a robust sandwich variance estimate should be computed. In the presence of the id variable, the score residuals will be aggregated for each id when computing the robust sandwich variance estimate.
plci	Whether to obtain profile likelihood confidence interval.
alpha	The two-sided significance level.

Details

There are two ways to specify the model, one for right censored data through the time and event variables, and the other for interval censored data through the time (lower) and time2 (upper) variables. For the second form, we follow the convention used in SAS PROC LIFEREG:

- If lower is not missing, upper is not missing, and lower is equal to upper, then there is no censoring and the event occurred at time lower.

- If lower is not missing, upper is not missing, and lower < upper, then the event time is censored within the interval (lower, upper).

- If lower is missing, but upper is not missing, then upper will be used as the left censoring value.

- If lower is not missing, but upper is missing, then lower will be used as the right censoring value.

- If lower is not missing, upper is not missing, but lower > upper, or if both lower and upper are missing, then the observation will not be used.

Value

A list with the following components:

- `sumstat`: The data frame of summary statistics of model fit with the following variables:
    - `n`: The number of observations.
    - `nevents`: The number of events.
    - `loglik0`: The log-likelihood under null.
    - `loglik1`: The maximum log-likelihood.
    - `niter`: The number of Newton-Raphson iterations.
    - `dist`: The assumed distribution.
    - `p`: The number of parameters, including the intercept, regression coefficients associated with the covariates, and the log scale parameters for the strata.
    - `nvar`: The number of regression coefficients associated with the covariates (excluding the intercept).
    - `robust`: Whether the robust sandwich variance estimate is requested.
    - `rep`: The replication.

- `parest`: The data frame of parameter estimates with the following variables:
    - `param`: The name of the covariate for the parameter estimate.
    - `beta`: The parameter estimate.
    - `sebeta`: The standard error of parameter estimate.
    - `z`: The Wald test statistic for the parameter.
    - `expbeta`: The exponentiated parameter estimate.
    - `vbeta`: The covariance matrix for parameter estimates.
    - `lower`: The lower limit of confidence interval.
    - `upper`: The upper limit of confidence interval.
    - `p`: The p-value from the chi-square test.
    - `method`: The method to compute the confidence interval and p-value.

– `sebeta_naive`: The naive standard error of parameter estimate if robust variance is requested.

– `vbeta_naive`: The naive covariance matrix for parameter estimates if robust variance is requested.

– `rep`: The replication.

- `p`: The number of parameters.

- `nvar`: The number of columns of the design matrix excluding the intercept.

- `param`: The parameter names.

- `beta`: The parameter estimate.

- `vbeta`: The covariance matrix for parameter estimates.

- `vbeta_naive`: The naive covariance matrix for parameter estimates.

- `terms`: The terms object.

- `xlevels`: A record of the levels of the factors used in fitting.

- `data`: The input data.

- `rep`: The name(s) of the replication variable(s).

- `stratum`: The name(s) of the stratum variable(s).

- `time`: The name of the time variable.

- `time2`: The name of the time2 variable.

- `event`: The name of the event variable.

- `covariates`: The names of baseline covariates.

- `weight`: The name of the weight variable.

- `offset`: The name of the offset variable.

- `id`: The name of the id variable.

- `dist`: The assumed distribution for time to event.

- `robust`: Whether a robust sandwich variance estimate should be computed.

- `plci`: Whether to obtain profile likelihood confidence interval.

- `alpha`: The two-sided significance level.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

John D. Kalbfleisch and Ross L. Prentice. The Statistical Analysis of Failure Time Data. Wiley: New York, 1980.

Examples

```
library(dplyr)

# right censored data
(fit1 <- liferegr(
  data = rawdata %>% mutate(treat = 1*(treatmentGroup == 1)),
  rep = "iterationNumber", stratum = "stratum",
  time = "timeUnderObservation", event = "event",
  covariates = "treat", dist = "weibull"))

# tobit regression for left censored data
(fit2 <- liferegr(
  data = tobin %>% mutate(time = ifelse(durable>0, durable, NA)),
  time = "time", time2 = "durable",
  covariates = c("age", "quant"), dist = "normal"))
```

---

logisregr   *Logistic Regression Models for Binary Data*

Description

Obtains the parameter estimates from logistic regression models with binary data.

Usage

```
logisregr(
  data,
  rep = "",
  event = "event",
  covariates = "",
  freq = "",
  weight = "",
  offset = "",
  id = "",
  link = "logit",
  robust = FALSE,
  firth = FALSE,
  bc = FALSE,
  flic = FALSE,
  plci = FALSE,
  alpha = 0.05
)
```

Arguments

data   The input data frame that contains the following variables:

- rep: The replication for by-group processing.

- event: The event indicator, 1=event, 0=no event.
- covariates: The values of baseline covariates.
- freq: The frequency for each observation.
- weight: The weight for each observation.
- offset: The offset for each observation.
- id: The optional subject ID to group the score residuals in computing the robust sandwich variance.

rep	The name(s) of the replication variable(s) in the input data.
event	The name of the event variable in the input data.
covariates	The vector of names of baseline covariates in the input data.
freq	The name of the frequency variable in the input data. The frequencies must be the same for all observations within each cluster as indicated by the id. Thus freq is the cluster frequency.
weight	The name of the weight variable in the input data.
offset	The name of the offset variable in the input data.
id	The name of the id variable in the input data.
link	The link function linking the response probabilities to the linear predictors. Options include "logit" (default), "probit", and "cloglog" (complementary log-log).
robust	Whether a robust sandwich variance estimate should be computed. In the presence of the id variable, the score residuals will be aggregated for each id when computing the robust sandwich variance estimate.
firth	Whether the firth's bias reducing penalized likelihood should be used. The default is FALSE.
bc	Whether to apply firth's bias correction for noncanonical parameterization and weighted logistic regression. The default is FALSE, in which case, the penalized likelihood with Jeffreys prior will be used.
flic	Whether to apply intercept correction to obtain more accurate predicted probabilities. The default is FALSE.
plci	Whether to obtain profile likelihood confidence interval.
alpha	The two-sided significance level.

Details

Fitting a logistic regression model using Firth's bias reduction method is equivalent to penalization of the log-likelihood by the Jeffreys prior. Firth's penalized log-likelihood is given by

$$l(\beta) + \frac{1}{2} \log(\det(I(\beta)))$$

and the components of the gradient $g(\beta)$ are computed as

$$g(\beta_j) + \frac{1}{2}\text{trace}\left(I(\beta)^{-1}\frac{\partial I(\beta)}{\partial \beta_j}\right)$$

The Hessian matrix is not modified by this penalty.

Firth's method reduces bias in maximum likelihood estimates of coefficients, but it introduces a bias toward one-half in the predicted probabilities.

A straightforward modification to Firth's logistic regression to achieve unbiased average predicted probabilities involves a post hoc adjustment of the intercept. This approach, known as Firth's logistic regression with intercept correction (FLIC), preserves the bias-corrected effect estimates. By excluding the intercept from penalization, it ensures that we don't sacrifice the accuracy of effect estimates to improve the predictions.

Value

A list with the following components:

- `sumstat`: The data frame of summary statistics of model fit with the following variables:
  - `n`: The number of subjects.
  - `nevents`: The number of events.
  - `loglik0`: The (penalized) log-likelihood under null.
  - `loglik1`: The maximum (penalized) log-likelihood.
  - `niter`: The number of Newton-Raphson iterations.
  - `p`: The number of parameters, including the intercept, and regression coefficients associated with the covariates.
  - `link`: The link function.
  - `robust`: Whether a robust sandwich variance estimate should be computed.
  - `firth`: Whether the firth's penalized likelihood is used.
  - `bc`: Whether to apply firth's bias correction for noncanonical parameterization and weighted logistic regression.
  - `flic`: Whether to apply intercept correction.
  - `loglik0_unpenalized`: The unpenalized log-likelihood under null.
  - `loglik1_unpenalized`: The maximum unpenalized log-likelihood.
  - `rep`: The replication.
- `parest`: The data frame of parameter estimates with the following variables:
  - `param`: The name of the covariate for the parameter estimate.
  - `beta`: The parameter estimate.
  - `sebeta`: The standard error of parameter estimate.
  - `z`: The Wald test statistic for the parameter.
  - `expbeta`: The exponentiated parameter estimate.
  - `vbeta`: The covariance matrix for parameter estimates.
  - `lower`: The lower limit of confidence interval.
  - `upper`: The upper limit of confidence interval.
  - `p`: The p-value from the chi-square test.
  - `method`: The method to compute the confidence interval and p-value.
  - `sebeta_naive`: The naive standard error of parameter estimate.
  - `vbeta_naive`: The naive covariance matrix of parameter estimates.
  - `rep`: The replication.
- `fitted`: The data frame with the following variables:

- – linear_predictors: The linear fit on the logit scale.
    - – fitted_values: The fitted probabilities of having an event, obtained by transforming the linear predictors by the inverse of the logit link.
    - – rep: The replication.
- p: The number of parameters.
- link: The link function.
- param: The parameter names.
- beta: The parameter estimate.
- vbeta: The covariance matrix for parameter estimates.
- vbeta_naive: The naive covariance matrix for parameter estimates.
- linear_predictors: The linear fit on the logit scale.
- fitted_values: The fitted probabilities of having an event.
- terms: The terms object.
- xlevels: A record of the levels of the factors used in fitting.
- data: The input data.
- rep: The name(s) of the replication variable(s).
- event: The name of the event variable.
- covariates: The names of baseline covariates.
- freq: The name of the freq variable.
- weight: The name of the weight variable.
- offset: The name of the offset variable.
- id: The name of the id variable.
- robust: Whether a robust sandwich variance estimate should be computed.
- bc: Whether to apply firth's bias correction for noncanonical parameterization and weighted logistic regression.
- firth: Whether to use the firth's bias reducing penalized likelihood.
- flic: Whether to apply intercept correction.
- plci: Whether to obtain profile likelihood confidence interval.
- alpha: The two-sided significance level.

Author(s)

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References

David Firth. Bias Reduction of Maximum Likelihood Estimates. Biometrika 1993; 80:27–38.

Georg Heinze and Michael Schemper. A solution to the problem of separation in logistic regression. Statistics in Medicine 2002;21:2409–2419.

Rainer Puhr, Georg Heinze, Mariana Nold, Lara Lusa, and Angelika Geroldinger. Firth's logistic regression with rare events: accurate effect estimates and predictions? Statistics in Medicine 2017; 36:2302-2317.

Examples

```
(fit1 <- logisregr(
  ingots, event = "NotReady", covariates = "Heat*Soak", freq = "Freq"))
```

---

lrpower   *Log-Rank Test Power*

Description

Estimates the power, stopping probabilities, and expected sample size in a two-group survival design.

Usage

```
lrpower(
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  hazardRatioH0 = 1,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  rho1 = 0,
  rho2 = 0,
  estimateHazardRatio = 1L,
  typeOfComputation = "direct",
  spendingTime = NA_real_,
  studyDuration = NA_real_
)
```

Arguments

kMax	The maximum number of stages.
informationRates	
	The information rates in terms of number of events for the conventional log-rank test and in terms of the actual information for weighted log-rank tests. Defaults to (1:kMax) / kMax if left unspecified.
efficacyStopping	
	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	
	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	
	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	
	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	
	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.
typeBetaSpending	
	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	
	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
hazardRatioH0	Hazard ratio under the null hypothesis for the active treatment versus control. Defaults to 1 for superiority test.
allocationRatioPlanned	
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

> A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

> A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

> A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1   A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.

lambda2   A vector of hazard rates for the event in each analysis time interval by stratum for the control group.

gamma1   The hazard rate for exponential dropout, a vector of hazard rates for piece-wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.

gamma2   The hazard rate for exponential dropout, a vector of hazard rates for piece-wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration

> Duration of the enrollment period.

followupTime   Follow-up time for the last enrolled subject.

fixedFollowup   Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

rho1   The first parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

rho2   The second parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

estimateHazardRatio

> Whether to estimate the hazard ratio from weighted Cox regression model and report the stopping boundaries on the hazard ratio scale.

typeOfComputation

> The type of computation, either "direct" for the direct approximation method, or "schoenfeld" for the Schoenfeld method. Defaults to "direct". Can use "Schoenfeld" under proportional hazards and conventional log-rank test.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

studyDuration   Study duration for fixed follow-up design. Defaults to missing, which is to be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and followupTime.

Value

An S3 class lrpower object with 4 components:

- overallResults: A data frame containing the following variables:

- – overallReject: The overall rejection probability.
- – alpha: The overall significance level.
- – numberOfEvents: The total number of events.
- – numberOfDropouts: The total number of dropouts.
- – numbeOfSubjects: The total number of subjects.
- – studyDuration: The total study duration.
- – information: The maximum information.
- – expectedNumberOfEvents: The expected number of events.
- – expectedNumberOfDropouts: The expected number of dropouts.
- – expectedNumberOfSubjects: The expected number of subjects.
- – expectedStudyDuration: The expected study duration.
- – expectedInformation: The expected information.
- – accrualDuration: The accrual duration.
- – followupTime: The follow-up time.
- – fixedFollowup: Whether a fixed follow-up design is used.
- – rho1: The first parameter of the Fleming-Harrington family of weighted log-rank test.
- – rho2: The second parameter of the Fleming-Harrington family of weighted log-rank test.
- – kMax: The number of stages.
- – hazardRatioH0: The hazard ratio under the null hypothesis.
- – typeOfComputation: The type of computation, either "direct" for the direct approximation method, or "schoenfeld" for the Schoenfeld method.
- byStageResults: A data frame containing the following variables:
  - – informationRates: The information rates.
  - – efficacyBounds: The efficacy boundaries on the Z-scale.
  - – futilityBounds: The futility boundaries on the Z-scale.
  - – rejectPerStage: The probability for efficacy stopping.
  - – futilityPerStage: The probability for futility stopping.
  - – cumulativeRejection: The cumulative probability for efficacy stopping.
  - – cumulativeFutility: The cumulative probability for futility stopping.
  - – cumulativeAlphaSpent: The cumulative alpha spent.
  - – numberOfEvents: The number of events.
  - – numberOfDropouts: The number of dropouts.
  - – numberOfSubjects: The number of subjects.
  - – analysisTime: The average time since trial start.
  - – efficacyHR: The efficacy boundaries on the hazard ratio scale if estimateHazardRatio.
  - – futilityHR: The futility boundaries on the hazard ratio scale if estimateHazardRatio.
  - – efficacyP: The efficacy boundaries on the p-value scale.
  - – futilityP: The futility boundaries on the p-value scale.
  - – information: The cumulative information.
  - – HR: The average hazard ratio.
  - – efficacyStopping: Whether to allow efficacy stopping.
  - – futilityStopping: Whether to allow futility stopping.

- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, typeBetaSpending, parameterBetaSpending, allocationRatioPlanned, accrualTime, accuralIntensity, piecewiseSurvivalTime, stratumFraction, lambda1, lambda2, gamma1, gamma2, estimateHazardRatio, and spendingTime.

- byTreatmentCounts: A list containing the following counts by treatment group:

  - numberOfEvents1: The number of events by stage for the treatment group.
  - numberOfDropouts1: The number of dropouts by stage for the treatment group.
  - numberOfSubjects1: The number of subjects by stage for the treatment group.
  - numberOfEvents2: The number of events by stage for the control group.
  - numberOfDropouts2: The number of dropouts by stage for the control group.
  - numberOfSubjects2: The number of subjects by stage for the control group.
  - expectedNumberOfEvents1: The expected number of events for the treatment group.
  - expectedNumberOfDropouts1: The expected number of dropouts for the treatment group.
  - expectedNumberOfSubjects1: The expected number of subjects for the treatment group.
  - expectedNumberOfEvents2: The expected number of events for control group.
  - expectedNumberOfDropouts2: The expected number of dropouts for the control group.
  - expectedNumberOfSubjects2: The expected number of subjects for the control group.

Author(s)

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Examples

```
# Piecewise accrual, piecewise exponential survival, and 5% dropout by
# the end of 1 year.

lrpower(kMax = 2, informationRates = c(0.8, 1),
        alpha = 0.025, typeAlphaSpending = "sfOF",
        allocationRatioPlanned = 1, accrualTime = seq(0, 8),
        accrualIntensity = 26/9*seq(1, 9),
        piecewiseSurvivalTime = c(0, 6),
        lambda1 = c(0.0533, 0.0309),
        lambda2 = c(0.0533, 0.0533),
        gamma1 = -log(1-0.05)/12,
        gamma2 = -log(1-0.05)/12, accrualDuration = 22,
        followupTime = 18, fixedFollowup = FALSE)
```

---

lrpowerequiv   *Power for Equivalence in Hazard Ratio*

Description

Obtains the power for equivalence in hazard ratio.

Usage

```
lrpowerequiv(
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  hazardRatioLower = NA_real_,
  hazardRatioUpper = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  typeOfComputation = "direct",
  spendingTime = NA_real_,
  studyDuration = NA_real_
)
```

Arguments

kMax   The maximum number of stages.

informationRates

                The information rates. Defaults to (1:kMax) / kMax if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha   The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending

                The type of alpha spending. One of the following: "OF" for O'Brien-Fleming
                boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries,
                "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spend-
                ing function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang,
                Shi & DeCani spending function, "user" for user defined spending, and "none"
                for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

                The parameter value for the alpha spending. Corresponds to Delta for "WT",
                rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

                The user defined alpha spending. Cumulative alpha spent up to each stage.

hazardRatioLower

        The lower equivalence limit of hazard ratio.

hazardRatioUpper

        The upper equivalence limit of hazard ratio.

allocationRatioPlanned

        Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

        A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

        A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

        A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1   A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.

lambda2   A vector of hazard rates for the event in each analysis time interval by stratum for the control group.

gamma1   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.

gamma2   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration

        Duration of the enrollment period.

followupTime   Follow-up time for the last enrolled subject.

fixedFollowup   Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

typeOfComputation

        The type of computation, either "direct" for the direct approximation method, or "schoenfeld" for the Schoenfeld method. Defaults to "direct". Can use "Schoenfeld" under proportional hazards and conventional log-rank test.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

studyDuration   Study duration for fixed follow-up design. Defaults to missing, which is to be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and followupTime.

Value

An S3 class `lrpowerequiv` object with 4 components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The overall significance level.
  - `numberOfEvents`: The total number of events.
  - `numberOfDropouts`: The total number of dropouts.
  - `numbeOfSubjects`: The total number of subjects.
  - `studyDuration`: The total study duration.
  - `information`: The maximum information.
  - `expectedNumberOfEvents`: The expected number of events.
  - `expectedNumberOfDropouts`: The expected number of dropouts.
  - `expectedNumberOfSubjects`: The expected number of subjects.
  - `expectedStudyDuration`: The expected study duration.
  - `expectedInformation`: The expected information.
  - `kMax`: The number of stages.
  - `hazardRatioLower`: The lower equivalence limit of hazard ratio.
  - `hazardRatioUpper`: The upper equivalence limit of hazard ratio.
  - `accrualDuration`: The accrual duration.
  - `followupTime`: The follow-up time.
  - `fixedFollowup`: Whether a fixed follow-up design is used.

- `byStageResults`: A data frame containing the following variables:
  - `informationRates`: The information rates.
  - `efficacyBounds`: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - `rejectPerStage`: The probability for efficacy stopping.
  - `cumulativeRejection`: The cumulative probability for efficacy stopping.
  - `cumulativeAlphaSpent`: The cumulative alpha for each of the two one-sided tests.
  - `cumulativeAttainedAlphaH10`: The cumulative alpha attained under H10.
  - `cumulativeAttainedAlphaH20`: The cumulative alpha attained under H20.
  - `numberOfEvents`: The number of events.
  - `numberOfDropouts`: The number of dropouts.
  - `numberOfSubjects`: The number of subjects.
  - `analysisTime`: The average time since trial start.
  - `efficacyHRLower`: The efficacy boundaries on the hazard ratio scale for the one-sided null hypothesis at the lower equivalence limit.
  - `efficacyHRUpper`: The efficacy boundaries on the hazard ratio scale for the one-sided null hypothesis at the upper equivalence limit.
  - `efficacyP`: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - `information`: The cumulative information.
  - `HR`: The average hazard ratio.

- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, allocationRatioPlanned, accrualTime, accuralIntensity, piecewiseSurvivalTime, stratumFraction, lambda1, lambda2, gamma1, gamma2, typeOfComputation, and spendingTime.

- byTreatmentCounts: A list containing the following counts by treatment group:

    - numberOfEvents1: The number of events by stage for the treatment group.
    - numberOfDropouts1: The number of dropouts by stage for the treatment group.
    - numberOfSubjects1: The number of subjects by stage for the treatment group.
    - numberOfEvents2: The number of events by stage for the control group.
    - numberOfDropouts2: The number of dropouts by stage for the control group.
    - numberOfSubjects2: The number of subjects by stage for the control group.
    - expectedNumberOfEvents1: The expected number of events for the treatment group.
    - expectedNumberOfDropouts1: The expected number of dropouts for the treatment group.
    - expectedNumberOfSubjects1: The expected number of subjects for the treatment group.
    - expectedNumberOfEvents2: The expected number of events for control group.
    - expectedNumberOfDropouts2: The expected number of dropouts for the control group.
    - expectedNumberOfSubjects2: The expected number of subjects for the control group.

Author(s)

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See Also

[rmstat](#)

Examples

```
lrpowerequiv(kMax = 2, informationRates = c(0.5, 1),
             alpha = 0.05, typeAlphaSpending = "sfOF",
             hazardRatioLower = 0.71, hazardRatioUpper = 1.4,
             allocationRatioPlanned = 1, accrualTime = seq(0, 8),
             accrualIntensity = 100/9*seq(1, 9),
             piecewiseSurvivalTime = c(0, 6),
             lambda1 = c(0.0533, 0.0533),
             lambda2 = c(0.0533, 0.0533),
             gamma1 = -log(1-0.05)/12,
             gamma2 = -log(1-0.05)/12, accrualDuration = 22,
             followupTime = 18, fixedFollowup = FALSE)
```

---

lrsamplesize   *Log-Rank Test Sample Size*

Description

Obtains the needed accrual duration given power and follow-up time, the needed follow-up time given power and accrual duration, or the needed absolute accrual rates given power, accrual duration, follow-up time, and relative accrual rates in a two-group survival design.

Usage

```
lrsamplesize(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  hazardRatioH0 = 1,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  rho1 = 0,
  rho2 = 0,
  estimateHazardRatio = 1L,
  typeOfComputation = "direct",
  interval = as.numeric(c(0.001, 240)),
  spendingTime = NA_real_,
  rounding = 1L
)
```

Arguments

`beta`	Type II error. Defaults to 0.2.
`kMax`	The maximum number of stages.
`informationRates`	The information rates in terms of number of events for the conventional log-rank test and in terms of the actual information for weighted log-rank tests. Defaults to `(1:kMax) / kMax` if left unspecified.
`efficacyStopping`	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
`futilityStopping`	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
`criticalValues`	Upper boundaries on the z-test statistic scale for stopping for efficacy.
`alpha`	The significance level. Defaults to 0.025.
`typeAlphaSpending`	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
`parameterAlphaSpending`	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
`userAlphaSpending`	The user defined alpha spending. Cumulative alpha spent up to each stage.
`futilityBounds`	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to `rep(-6, kMax-1)` if left unspecified. The futility bounds are non-binding for the calculation of critical values.
`typeBetaSpending`	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
`parameterBetaSpending`	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
`userBetaSpending`	The user defined beta spending. Cumulative beta spent up to each stage.
`hazardRatioH0`	Hazard ratio under the null hypothesis for the active treatment versus control. Defaults to 1 for superiority test.

allocationRatioPlanned

        Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

        A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

        A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

        A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1   A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.

lambda2   A vector of hazard rates for the event in each analysis time interval by stratum for the control group.

gamma1   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.

gamma2   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration

        Duration of the enrollment period.

followupTime   Follow-up time for the last enrolled subject.

fixedFollowup   Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

rho1   The first parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

rho2   The second parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

estimateHazardRatio

        Whether to estimate the hazard ratio from weighted Cox regression model and report the stopping boundaries on the hazard ratio scale.

typeOfComputation

        The type of computation, either "direct" for the direct approximation method, or "schoenfeld" for the Schoenfeld method. Defaults to "direct". Can use "Schoenfeld" under proportional hazards and conventional log-rank test.

interval   The interval to search for the solution of accrualDuration, followupTime, or the proportionality constant of accrualIntensity. Defaults to `c(0.001, 240)`. Adjustment may be needed for non-monotone relationship with study power.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as `informationRates`.

rounding   Whether to round up sample size and events. Defaults to 1 for sample size
                  rounding.

Value

A list of two components:

- resultsUnderH1: An S3 class lrpower object under the alternative hypothesis.
- resultsUnderH0: An S3 class lrpower object under the null hypothesis.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

See Also

lrpower

Examples

```
# Piecewise accrual, piecewise exponential survival, and 5% dropout by
# the end of 1 year.

# Example 1: Obtains accrual duration given power and follow-up time

lrsamplesize(beta = 0.2, kMax = 2,
             informationRates = c(0.8, 1),
             alpha = 0.025, typeAlphaSpending = "sfOF",
             accrualTime = seq(0, 8),
             accrualIntensity = 26/9*seq(1, 9),
             piecewiseSurvivalTime = c(0, 6),
             lambda1 = c(0.0533, 0.0309),
             lambda2 = c(0.0533, 0.0533),
             gamma1 = -log(1-0.05)/12,
             gamma2 = -log(1-0.05)/12,
             accrualDuration = NA,
             followupTime = 18, fixedFollowup = FALSE)


# Example 2: Obtains follow-up time given power and accrual duration

lrsamplesize(beta = 0.2, kMax = 2,
             informationRates = c(0.8, 1),
             alpha = 0.025, typeAlphaSpending = "sfOF",
             accrualTime = seq(0, 8),
             accrualIntensity = 26/9*seq(1, 9),
             piecewiseSurvivalTime = c(0, 6),
             lambda1 = c(0.0533, 0.0309),
             lambda2 = c(0.0533, 0.0533),
             gamma1 = -log(1-0.05)/12,
             gamma2 = -log(1-0.05)/12,
             accrualDuration = 22,
```

```
                    followupTime = NA, fixedFollowup = FALSE)


  # Example 3: Obtains absolute accrual intensity given power,
  # accrual duration, follow-up time, and relative accrual intensity

  lrsamplesize(beta = 0.2, kMax = 2,
               informationRates = c(0.8, 1),
               alpha = 0.025, typeAlphaSpending = "sfOF",
               accrualTime = seq(0, 8),
               accrualIntensity = 26/9*seq(1, 9),
               piecewiseSurvivalTime = c(0, 6),
               lambda1 = c(0.0533, 0.0309),
               lambda2 = c(0.0533, 0.0533),
               gamma1 = -log(1-0.05)/12,
               gamma2 = -log(1-0.05)/12,
               accrualDuration = 22,
               followupTime = 18, fixedFollowup = FALSE)
```

---

lrsamplesizeequiv   *Sample Size for Equivalence in Hazard Ratio*

Description

Obtains the sample size for equivalence in hazard ratio.

Usage

```
lrsamplesizeequiv(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  hazardRatioLower = NA_real_,
  hazardRatioUpper = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
```

```
    gamma2 = 0L,
    accrualDuration = NA_real_,
    followupTime = NA_real_,
    fixedFollowup = 0L,
    typeOfComputation = "direct",
    interval = as.numeric(c(0.001, 240)),
    spendingTime = NA_real_,
    rounding = 1L
)
```

Arguments

beta	The type II error.
kMax	The maximum number of stages.
informationRates	The information rates. Defaults to (1:kMax) / kMax if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level for each of the two one-sided tests. Defaults to 0.05.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
hazardRatioLower	The lower equivalence limit of hazard ratio.
hazardRatioUpper	The upper equivalence limit of hazard ratio.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

> A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1   A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.

lambda2   A vector of hazard rates for the event in each analysis time interval by stratum for the control group.

gamma1   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.

gamma2   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration

> Duration of the enrollment period.

followupTime   Follow-up time for the last enrolled subject.

fixedFollowup   Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

typeOfComputation

> The type of computation, either "direct" for the direct approximation method, or "schoenfeld" for the Schoenfeld method. Defaults to "direct". Can use "Schoenfeld" under proportional hazards and conventional log-rank test.

interval   The interval to search for the solution of accrualDuration, followupDuration, or the proportionality constant of accrualIntensity. Defaults to c(0.001, 240).

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

rounding   Whether to round up sample size. Defaults to 1 for sample size rounding.

Value

An S3 class lrpowerequiv object

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

See Also

[lrpowerequiv](#)

Examples

```
lrsamplesizeequiv(kMax = 2, informationRates = c(0.5, 1),
                  alpha = 0.05, typeAlphaSpending = "sfOF",
                  hazardRatioLower = 0.71, hazardRatioUpper = 1.4,
                  allocationRatioPlanned = 1, accrualTime = seq(0, 8),
                  accrualIntensity = 26/9*seq(1, 9),
                  piecewiseSurvivalTime = c(0, 6),
```

```
                    lambda1 = c(0.0533, 0.0533),
                    lambda2 = c(0.0533, 0.0533),
                    gamma1 = -log(1-0.05)/12,
                    gamma2 = -log(1-0.05)/12, accrualDuration = NA,
                    followupTime = 18, fixedFollowup = FALSE)
```

---

lrschoenfeld   *Schoenfeld Method for Log-Rank Test Sample Size Calculation*

Description

Obtains the sample size and study duration by calibrating the number of events calculated using the
Schoenfeld formula under the proportional hazards assumption.

Usage

```
lrschoenfeld(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  hazardRatioH0 = 1,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  hazardRatio = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  interval = as.numeric(c(0.001, 240)),
  spendingTime = NA_real_,
  rounding = 1L,
```

```
  calibrate = 1L,
  maxNumberOfIterations = 10000L,
  maxNumberOfRawDatasetsPerStage = 0L,
  seed = NA_integer_
)
```

Arguments

beta	Type II error. Defaults to 0.2.
kMax	The maximum number of stages.
informationRates	
	The information rates in terms of number of events for the conventional log-rank test and in terms of the actual information for weighted log-rank tests. Defaults to (1:kMax) / kMax if left unspecified.
efficacyStopping	
	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	
	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	
	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	
	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	
	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.
typeBetaSpending	
	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	
	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

    The user defined beta spending. Cumulative beta spent up to each stage.

hazardRatioH0   Hazard ratio under the null hypothesis for the active treatment versus control. Defaults to 1 for superiority test.

allocationRatioPlanned

    Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

    A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

    A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

    A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

hazardRatio   Hazard ratio under the alternative hypothesis for the active treatment versus control.

lambda2   A vector of hazard rates for the event in each analysis time interval by stratum for the control group.

gamma1   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.

gamma2   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

followupTime   Follow-up time for the last enrolled subject.

fixedFollowup   Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

interval   The interval to search for the solution of followupTime. Defaults to `c(0.001, 240)`.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

rounding   Whether to round up sample size and events. Defaults to 1 for sample size rounding.

calibrate   Whether to use simulations to calibrate the number of events calculated using the Schoenfeld formula.

maxNumberOfIterations

    The number of simulation iterations. Defaults to 10000.

maxNumberOfRawDatasetsPerStage

    The number of raw datasets per stage to extract.

seed   The seed to reproduce the simulation results. The seed from the environment will be used if left unspecified.

Value

A list of two components:

- resultsUnderH1: An S3 class lrpower object under the alternative hypothesis.

- resultsUnderH0: An S3 class lrpower object under the null hypothesis.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
(lr1 <- lrschoenfeld(
  beta = 0.1, kMax = 2, alpha = 0.025,
  hazardRatioH0 = 1, allocationRatioPlanned = 1,
  accrualIntensity = 20, hazardRatio = 0.3,
  lambda2 = 1.9/12,
  gamma1 = -log(1-0.1)/24, gamma2 = -log(1-0.1)/24,
  fixedFollowup = 0, rounding = 1,
  calibrate = 0, maxNumberOfIterations = 1000,
  seed = 12345))

(lr2 <- lrschoenfeld(
  beta = 0.1, kMax = 2, alpha = 0.025,
  hazardRatioH0 = 1, allocationRatioPlanned = 1,
  accrualIntensity = 20, hazardRatio = 0.3,
  lambda2 = 1.9/12,
  gamma1 = -log(1-0.1)/24, gamma2 = -log(1-0.1)/24,
  fixedFollowup = 0, rounding = 1,
  calibrate = 1, maxNumberOfIterations = 1000,
  seed = 12345))
```

---

lrsim   *Log-Rank Test Simulation*

Description

Performs simulation for two-arm group sequential trials based on weighted log-rank test.

Usage

```
lrsim(
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  futilityBounds = NA_real_,
  hazardRatioH0 = 1,
```

```
    allocation1 = 1L,
    allocation2 = 1L,
    accrualTime = 0L,
    accrualIntensity = NA_real_,
    piecewiseSurvivalTime = 0L,
    stratumFraction = 1L,
    lambda1 = NA_real_,
    lambda2 = NA_real_,
    gamma1 = 0L,
    gamma2 = 0L,
    accrualDuration = NA_real_,
    followupTime = NA_real_,
    fixedFollowup = 0L,
    rho1 = 0,
    rho2 = 0,
    plannedEvents = NA_integer_,
    plannedTime = NA_real_,
    maxNumberOfIterations = 1000L,
    maxNumberOfRawDatasetsPerStage = 0L,
    seed = NA_integer_
)
```

Arguments

kMax   The maximum number of stages.

informationRates

                The information rates in terms of number of events for the conventional log-
                rank test and in terms of the actual information for weighted log-rank tests.
                Fixed prior to the trial. If left unspecified, it defaults to plannedEvents /
                plannedEvents[kMax] when plannedEvents is provided and to plannedTime
                / plannedTime[kMax] otherwise.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1,
                ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds
                are non-binding for the calculation of critical values.

hazardRatioH0   Hazard ratio under the null hypothesis for the active treatment versus control.
                Defaults to 1 for superiority test.

allocation1   Number of subjects in the active treatment group in a randomization block. De-
                faults to 1 for equal randomization.

allocation2   Number of subjects in the control group in a randomization block. Defaults to 1
                for equal randomization.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time
                intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual
                intervals: [0, 3) and [3, Inf).

accrualIntensity

                A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

        A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

        A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1   A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.

lambda2   A vector of hazard rates for the event in each analysis time interval by stratum for the control group.

gamma1   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.

gamma2   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration

        Duration of the enrollment period.

followupTime   Follow-up time for the last enrolled subject.

fixedFollowup   Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

rho1   The first parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

rho2   The second parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

plannedEvents   The planned cumulative total number of events at each stage.

plannedTime   The calendar times for the analyses. To use calendar time to plan the analyses, `plannedEvents` should be missing.

maxNumberOfIterations

        The number of simulation iterations. Defaults to 1000.

maxNumberOfRawDatasetsPerStage

        The number of raw datasets per stage to extract.

seed   The seed to reproduce the simulation results. The seed from the environment will be used if left unspecified.

Value

An S3 class `lrsim` object with 3 components:

- `overview`: A list containing the following information:
    - `rejectPerStage`: The efficacy stopping probability by stage.
    - `futilityPerStage`: The futility stopping probability by stage.
    - `cumulativeRejection`: Cumulative efficacy stopping probability by stage.
    - `cumulativeFutility`: The cumulative futility stopping probability by stage.

- **numberOfEvents**: The average number of events by stage.
- **numberOfDropouts**: The average number of dropouts by stage.
- **numberOfSubjects**: The average number of subjects by stage.
- **analysisTime**: The average analysis time by stage.
- **overallReject**: The overall rejection probability.
- **expectedNumberOfEvents**: The expected number of events for the overall study.
- **expectedNumberOfDropouts**: The expected number of dropouts for the overall study.
- **expectedNumberOfSubjects**: The expected number of subjects for the overall study.
- **expectedStudyDuration**: The expected study duration.
- **hazardRatioH0**: Hazard ratio under the null hypothesis for the active treatment versus control.
- **useEvents**: whether the analyses are planned based on the number of events or calendar time.
- **accrualDuration**: Duration of the enrollment period.
- **fixedFollowup**: Whether a fixed follow-up design is used.
- **rho1**: The first parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.
- **rho2**: The second parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.
- **kMax**: The maximum number of stages.

- **sumdata**: A data frame of summary data by iteration and stage:

  - **iterationNumber**: The iteration number.
  - **stopStage**: The stage at which the trial stops.
  - **eventsNotAchieved**: Whether the target number of events is not achieved for the iteration.
  - **stageNumber**: The stage number, covering all stages even if the trial stops at an interim look.
  - **analysisTime**: The time for the stage since trial start.
  - **accruals1**: The number of subjects enrolled at the stage for the treatment group.
  - **accruals2**: The number of subjects enrolled at the stage for the control group.
  - **totalAccruals**: The total number of subjects enrolled at the stage.
  - **events1**: The number of events at the stage for the treatment group.
  - **events2**: The number of events at the stage for the control group.
  - **totalEvents**: The total number of events at the stage.
  - **dropouts1**: The number of dropouts at the stage for the treatment group.
  - **dropouts2**: The number of dropouts at the stage for the control group.
  - **totalDropouts**: The total number of dropouts at the stage.
  - **uscore**: The numerator of the log-rank test statistic.
  - **vscore**: The variance of the log-rank test statistic.
  - **logRankStatistic**: The log-rank test Z-statistic.
  - **rejectPerStage**: Whether to reject the null hypothesis at the stage.
  - **futilityPerStage**: Whether to stop the trial for futility at the stage.

- rawdata (exists if maxNumberOfRawDatasetsPerStage is a positive integer): A data frame for subject-level data for selected replications, containing the following variables:

    - iterationNumber: The iteration number.
    - stopStage: The stage at which the trial stops.
    - analysisTime: The time for the stage since trial start.
    - subjectId: The subject ID.
    - arrivalTime: The enrollment time for the subject.
    - stratum: The stratum for the subject.
    - treatmentGroup: The treatment group (1 or 2) for the subject.
    - survivalTime: The underlying survival time for the subject.
    - dropoutTime: The underlying dropout time for the subject.
    - timeUnderObservation: The time under observation since randomization.
    - event: Whether the subject experienced the event.
    - dropoutEvent: Whether the subject dropped out.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: analyses based on number of events

sim1 = lrsim(kMax = 2, informationRates = c(0.5, 1),
             criticalValues = c(2.797, 1.977),
             accrualIntensity = 11,
             lambda1 = 0.018, lambda2 = 0.030,
             accrualDuration = 12,
             plannedEvents = c(60, 120),
             maxNumberOfIterations = 1000,
             maxNumberOfRawDatasetsPerStage = 1,
             seed = 314159)

# summary statistics
sim1

# summary for each simulated data set
head(sim1$sumdata)

# raw data for selected replication
head(sim1$rawdata)


# Example 2: analyses based on calendar time have similar power

sim2 = lrsim(kMax = 2, informationRates = c(0.5, 1),
             criticalValues = c(2.797, 1.977),
             accrualIntensity = 11,
             lambda1 = 0.018, lambda2 = 0.030,
```

```
                accrualDuration = 12,
                plannedTime = c(31.9, 113.2),
                maxNumberOfIterations = 1000,
                maxNumberOfRawDatasetsPerStage = 1,
                seed = 314159)

# summary statistics
sim2

# summary for each simulated data set
head(sim2$sumdata)
```

---

lrsim2e   *Log-Rank Test Simulation for Two Endpoints*

Description

Performs simulation for two-endpoint two-arm group sequential trials based on weighted log-rank test. The first kMaxe1 looks are driven by the total number of PFS events in two arms combined, and the subsequent looks are driven by the total number of OS events in two arms combined. Alternatively, the analyses can be planned to occur at specified calendar times.

Usage

```
lrsim2e(
  kMax = NA_integer_,
  kMaxe1 = NA_integer_,
  hazardRatioH0e1 = 1,
  hazardRatioH0e2 = 1,
  allocation1 = 1L,
  allocation2 = 1L,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  rho = 0,
  lambda1e1 = NA_real_,
  lambda2e1 = NA_real_,
  lambda1e2 = NA_real_,
  lambda2e2 = NA_real_,
  gamma1e1 = 0L,
  gamma2e1 = 0L,
  gamma1e2 = 0L,
  gamma2e2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
```

```
    rho1 = 0,
    rho2 = 0,
    plannedEvents = NA_integer_,
    plannedTime = NA_real_,
    maxNumberOfIterations = 1000L,
    maxNumberOfRawDatasetsPerStage = 0L,
    seed = NA_integer_
)
```

Arguments

kMax	The maximum number of stages.
kMaxe1	Number of stages with timing determined by PFS events. Ranges from 0 (none) to kMax.
hazardRatioH0e1	
	Hazard ratio under the null hypothesis for the active treatment vs control for endpoint 1 (PFS). Defaults to 1 for superiority test.
hazardRatioH0e2	
	Hazard ratio under the null hypothesis for the active treatment vs control for endpoint 2 (OS). Defaults to 1 for superiority test.
allocation1	Number of subjects in the treatment group in a randomization block. Defaults to 1 for equal randomization.
allocation2	Number of subjects in the control group in a randomization block. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).
accrualIntensity	
	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	
	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.
stratumFraction	
	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
rho	The correlation coefficient for the standard bivariate normal random variables used to generate time to disease progression and time to death using the inverse CDF method.
lambda1e1	A vector of hazard rates for the event in each analysis time interval by stratum for the treatment group and endpoint 1 (PFS).
lambda2e1	A vector of hazard rates for the event in each analysis time interval by stratum for the control group and endpoint 1 (PFS).
lambda1e2	A vector of hazard rates for the event in each analysis time interval by stratum for the treatment group and endpoint 2 (OS).
lambda2e2	A vector of hazard rates for the event in each analysis time interval by stratum for the control group and endpoint 2 (OS).

gamma1e1   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the treatment group and endpoint 1 (PFS).

gamma2e1   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group and endpoint 1 (PFS).

gamma1e2   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the treatment group and endpoint 2 (OS).

gamma2e2   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group and endpoint 2 (OS).

accrualDuration
                Duration of the enrollment period.

followupTime   Follow-up time for the last enrolled subject.

fixedFollowup   Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

rho1   The first parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

rho2   The second parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

plannedEvents   The planned cumulative total number of PFS events at Look 1 to Look kMaxe1 and the planned cumulative total number of OS events at Look kMaxe1+1 to Look kMax.

plannedTime   The calendar times for the analyses. To use calendar time to plan the analyses, plannedEvents should be missing.

maxNumberOfIterations
                The number of simulation iterations. Defaults to 1000.
maxNumberOfRawDatasetsPerStage
                The number of raw datasets per stage to extract.

seed   The seed to reproduce the simulation results. The seed from the environment will be used if left unspecified.

Value

A list with 2 components:

- sumdata: A data frame of summary data by iteration and stage:
    - iterationNumber: The iteration number.
    - eventsNotAchieved: Whether the target number of events is not achieved for the iteration.

- **stageNumber**: The stage number, covering all stages even if the trial stops at an interim look.
- **analysisTime**: The time for the stage since trial start.
- **accruals1**: The number of subjects enrolled at the stage for the treatment group.
- **accruals2**: The number of subjects enrolled at the stage for the control group.
- **totalAccruals**: The total number of subjects enrolled at the stage.
- **endpoint**: The endpoint (1 or 2) under consideration.
- **events1**: The number of events at the stage for the treatment group.
- **events2**: The number of events at the stage for the control group.
- **totalEvents**: The total number of events at the stage.
- **dropouts1**: The number of dropouts at the stage for the treatment group.
- **dropouts2**: The number of dropouts at the stage for the control group.
- **totalDropouts**: The total number of dropouts at the stage.
- **logRankStatistic**: The log-rank test Z-statistic for the endpoint.

- **rawdata** (exists if maxNumberOfRawDatasetsPerStage is a positive integer): A data frame for subject-level data for selected replications, containing the following variables:

  - **iterationNumber**: The iteration number.
  - **stageNumber**: The stage under consideration.
  - **analysisTime**: The time for the stage since trial start.
  - **subjectId**: The subject ID.
  - **arrivalTime**: The enrollment time for the subject.
  - **stratum**: The stratum for the subject.
  - **treatmentGroup**: The treatment group (1 or 2) for the subject.
  - **survivalTime1**: The underlying survival time for event endpoint 1 for the subject.
  - **dropoutTime1**: The underlying dropout time for event endpoint 1 for the subject.
  - **timeUnderObservation1**: The time under observation since randomization for event endpoint 1 for the subject.
  - **event1**: Whether the subject experienced event endpoint 1.
  - **dropoutEvent1**: Whether the subject dropped out for endpoint 1.
  - **survivalTime2**: The underlying survival time for event endpoint 2 for the subject.
  - **dropoutTime2**: The underlying dropout time for event endpoint 2 for the subject.
  - **timeUnderObservation2**: The time under observation since randomization for event endpoint 2 for the subject.
  - **event2**: Whether the subject experienced event endpoint 2.
  - **dropoutEvent2**: Whether the subject dropped out for endpoint 2.

Author(s)

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Examples

```
sim1 = lrsim2e(
  kMax = 3,
  kMaxe1 = 2,
  allocation1 = 2,
  allocation2 = 1,
  accrualTime = c(0, 8),
  accrualIntensity = c(10, 28),
  piecewiseSurvivalTime = 0,
  rho = 0,
  lambda1e1 = log(2)/12*0.60,
  lambda2e1 = log(2)/12,
  lambda1e2 = log(2)/30*0.65,
  lambda2e2 = log(2)/30,
  accrualDuration = 20.143,
  plannedEvents = c(186, 259, 183),
  maxNumberOfIterations = 1000,
  maxNumberOfRawDatasetsPerStage = 1,
  seed = 314159)

head(sim1$sumdata)
head(sim1$rawdata)
```

---

lrsim2e3a   *Log-Rank Test Simulation for Two Endpoints and Three Arms*

Description

Performs simulation for two-endpoint three-arm group sequential trials based on weighted log-rank test. The first kMaxe1 looks are driven by the total number of PFS events in Arm A and Arm C combined, and the subsequent looks are driven by the total number of OS events in Arm A and Arm C combined. Alternatively, the analyses can be planned to occur at specified calendar times.

Usage

```
lrsim2e3a(
  kMax = NA_integer_,
  kMaxe1 = NA_integer_,
  hazardRatioH013e1 = 1,
  hazardRatioH023e1 = 1,
  hazardRatioH012e1 = 1,
  hazardRatioH013e2 = 1,
  hazardRatioH023e2 = 1,
  hazardRatioH012e2 = 1,
  allocation1 = 1L,
  allocation2 = 1L,
  allocation3 = 1L,
```

```
    accrualTime = 0L,
    accrualIntensity = NA_real_,
    piecewiseSurvivalTime = 0L,
    stratumFraction = 1L,
    rho = 0,
    lambda1e1 = NA_real_,
    lambda2e1 = NA_real_,
    lambda3e1 = NA_real_,
    lambda1e2 = NA_real_,
    lambda2e2 = NA_real_,
    lambda3e2 = NA_real_,
    gamma1e1 = 0L,
    gamma2e1 = 0L,
    gamma3e1 = 0L,
    gamma1e2 = 0L,
    gamma2e2 = 0L,
    gamma3e2 = 0L,
    accrualDuration = NA_real_,
    followupTime = NA_real_,
    fixedFollowup = 0L,
    rho1 = 0,
    rho2 = 0,
    plannedEvents = NA_integer_,
    plannedTime = NA_real_,
    maxNumberOfIterations = 1000L,
    maxNumberOfRawDatasetsPerStage = 0L,
    seed = NA_integer_
)
```

Arguments

kMax   The maximum number of stages.

kMaxe1   Number of stages with timing determined by PFS events. Ranges from 0 (none) to kMax.

hazardRatioH013e1
                    Hazard ratio under the null hypothesis for arm 1 vs arm 3 for endpoint 1 (PFS). Defaults to 1 for superiority test.

hazardRatioH023e1
                    Hazard ratio under the null hypothesis for arm 2 vs arm 3 for endpoint 1 (PFS). Defaults to 1 for superiority test.

hazardRatioH012e1
                    Hazard ratio under the null hypothesis for arm 1 vs arm 2 for endpoint 1 (PFS). Defaults to 1 for superiority test.

hazardRatioH013e2
                    Hazard ratio under the null hypothesis for arm 1 vs arm 3 for endpoint 2 (OS). Defaults to 1 for superiority test.

hazardRatioH023e2

  Hazard ratio under the null hypothesis for arm 2 vs arm 3 for endpoint 2 (OS). Defaults to 1 for superiority test.

hazardRatioH012e2

  Hazard ratio under the null hypothesis for arm 1 vs arm 2 for endpoint 2 (OS). Defaults to 1 for superiority test.

allocation1   Number of subjects in Arm A in a randomization block. Defaults to 1 for equal randomization.

allocation2   Number of subjects in Arm B in a randomization block. Defaults to 1 for equal randomization.

allocation3   Number of subjects in Arm C in a randomization block. Defaults to 1 for equal randomization.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

  A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

  A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

  A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

rho   The correlation coefficient for the standard bivariate normal random variables used to generate time to disease progression and time to death using the inverse CDF method.

lambda1e1   A vector of hazard rates for the event in each analysis time interval by stratum for arm 1 and endpoint 1 (PFS).

lambda2e1   A vector of hazard rates for the event in each analysis time interval by stratum for arm 2 and endpoint 1 (PFS).

lambda3e1   A vector of hazard rates for the event in each analysis time interval by stratum for arm 3 and endpoint 1 (PFS).

lambda1e2   A vector of hazard rates for the event in each analysis time interval by stratum for arm 1 and endpoint 2 (OS).

lambda2e2   A vector of hazard rates for the event in each analysis time interval by stratum for arm 2 and endpoint 2 (OS).

lambda3e2   A vector of hazard rates for the event in each analysis time interval by stratum for arm 3 and endpoint 2 (OS).

gamma1e1   The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 1 and endpoint 1 (PFS).

gamma2e1   The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 2 and endpoint 1 (PFS).

gamma3e1	The hazard rate for exponential dropout. A vector of hazard rates for piece-wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 3 and endpoint 1 (PFS).
gamma1e2	The hazard rate for exponential dropout. A vector of hazard rates for piece-wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 1 and endpoint 2 (OS).
gamma2e2	The hazard rate for exponential dropout. A vector of hazard rates for piece-wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 2 and endpoint 2 (OS).
gamma3e2	The hazard rate for exponential dropout. A vector of hazard rates for piece-wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 3 and endpoint 2 (OS).
accrualDuration	
	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
rho1	The first parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.
rho2	The second parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.
plannedEvents	The planned cumulative total number of PFS events at Look 1 to Look kMaxe1 for Arms A and C combined and the planned cumulative total number of OS events at Look kMaxe1+1 to Look kMax for Arms A and C combined.
plannedTime	The calendar times for the analyses. To use calendar time to plan the analyses, plannedEvents should be missing.
maxNumberOfIterations	
	The number of simulation iterations. Defaults to 1000.
maxNumberOfRawDatasetsPerStage	
	The number of raw datasets per stage to extract.
seed	The seed to reproduce the simulation results. The seed from the environment will be used if left unspecified.

Value

A list with 2 components:

- sumdata: A data frame of summary data by iteration and stage:
  - iterationNumber: The iteration number.
  - eventsNotAchieved: Whether the target number of events is not achieved for the iteration.
  - stageNumber: The stage number, covering all stages even if the trial stops at an interim look.
  - analysisTime: The time for the stage since trial start.
  - accruals1: The number of subjects enrolled at the stage for the active treatment 1 group.

- – accruals2: The number of subjects enrolled at the stage for the active treatment 2 group.
- – accruals3: The number of subjects enrolled at the stage for the control group.
- – totalAccruals: The total number of subjects enrolled at the stage.
- – endpoint: The endpoint (1 or 2) under consideration.
- – events1: The number of events at the stage for the active treatment 1 group.
- – events2: The number of events at the stage for the active treatment 2 group.
- – events3: The number of events at the stage for the control group.
- – totalEvents: The total number of events at the stage.
- – dropouts1: The number of dropouts at the stage for the active treatment 1 group.
- – dropouts2: The number of dropouts at the stage for the active treatment 2 group.
- – dropouts3: The number of dropouts at the stage for the control group.
- – totalDropouts: The total number of dropouts at the stage.
- – logRankStatistic13: The log-rank test Z-statistic comparing the active treatment 1 to the control for the endpoint.
- – logRankStatistic23: The log-rank test Z-statistic comparing the active treatment 2 to the control for the endpoint.
- – logRankStatistic12: The log-rank test Z-statistic comparing the active treatment 1 to the active treatment 2 for the endpoint.

- rawdata (exists if maxNumberOfRawDatasetsPerStage is a positive integer): A data frame for subject-level data for selected replications, containing the following variables:

  - – iterationNumber: The iteration number.
  - – stageNumber: The stage under consideration.
  - – analysisTime: The time for the stage since trial start.
  - – subjectId: The subject ID.
  - – arrivalTime: The enrollment time for the subject.
  - – stratum: The stratum for the subject.
  - – treatmentGroup: The treatment group (1, 2, or 3) for the subject.
  - – survivalTime1: The underlying survival time for event endpoint 1 for the subject.
  - – dropoutTime1: The underlying dropout time for event endpoint 1 for the subject.
  - – timeUnderObservation1: The time under observation since randomization for event endpoint 1 for the subject.
  - – event1: Whether the subject experienced event endpoint 1.
  - – dropoutEvent1: Whether the subject dropped out for endpoint 1.
  - – survivalTime2: The underlying survival time for event endpoint 2 for the subject.
  - – dropoutTime2: The underlying dropout time for event endpoint 2 for the subject.
  - – timeUnderObservation2: The time under observation since randomization for event endpoint 2 for the subject.
  - – event2: Whether the subject experienced event endpoint 2.
  - – dropoutEvent2: Whether the subject dropped out for endpoint 2.

Author(s)

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Examples

```
sim1 = lrsim2e3a(
  kMax = 3,
  kMaxe1 = 2,
  allocation1 = 2,
  allocation2 = 2,
  allocation3 = 1,
  accrualTime = c(0, 8),
  accrualIntensity = c(10, 28),
  piecewiseSurvivalTime = 0,
  rho = 0,
  lambda1e1 = log(2)/12*0.60,
  lambda2e1 = log(2)/12*0.70,
  lambda3e1 = log(2)/12,
  lambda1e2 = log(2)/30*0.65,
  lambda2e2 = log(2)/30*0.75,
  lambda3e2 = log(2)/30,
  accrualDuration = 30.143,
  plannedEvents = c(186, 259, 183),
  maxNumberOfIterations = 500,
  maxNumberOfRawDatasetsPerStage = 1,
  seed = 314159)

head(sim1$sumdata)
head(sim1$rawdata)
```

---

lrsim3a   *Log-Rank Test Simulation for Three Arms*

Description

Performs simulation for three-arm group sequential trials based on weighted log-rank test. The looks are driven by the total number of events in Arm A and Arm C combined. Alternatively, the analyses can be planned to occur at specified calendar times.

Usage

```
lrsim3a(
  kMax = NA_integer_,
  hazardRatioH013 = 1,
  hazardRatioH023 = 1,
  hazardRatioH012 = 1,
  allocation1 = 1L,
  allocation2 = 1L,
  allocation3 = 1L,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
```

```
    piecewiseSurvivalTime = 0L,
    stratumFraction = 1L,
    lambda1 = NA_real_,
    lambda2 = NA_real_,
    lambda3 = NA_real_,
    gamma1 = 0L,
    gamma2 = 0L,
    gamma3 = 0L,
    accrualDuration = NA_real_,
    followupTime = NA_real_,
    fixedFollowup = 0L,
    rho1 = 0,
    rho2 = 0,
    plannedEvents = NA_integer_,
    plannedTime = NA_real_,
    maxNumberOfIterations = 1000L,
    maxNumberOfRawDatasetsPerStage = 0L,
    seed = NA_integer_
)
```

Arguments

kMax   The maximum number of stages.

hazardRatioH013

                Hazard ratio under the null hypothesis for arm 1 versus arm 3. Defaults to 1 for
                superiority test.

hazardRatioH023

                Hazard ratio under the null hypothesis for arm 2 versus arm 3. Defaults to 1 for
                superiority test.

hazardRatioH012

                Hazard ratio under the null hypothesis for arm 1 versus arm 2. Defaults to 1 for
                superiority test.

allocation1   Number of subjects in Arm A in a randomization block. Defaults to 1 for equal
                randomization.

allocation2   Number of subjects in Arm B in a randomization block. Defaults to 1 for equal
                randomization.

allocation3   Number of subjects in Arm C in a randomization block. Defaults to 1 for equal
                randomization.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time
                intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual
                intervals: [0, 3) and [3, Inf).

accrualIntensity

                A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

                A vector that specifies the starting time of piecewise exponential survival time
                intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event
                intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction
    A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1   A vector of hazard rates for the event in each analysis time interval by stratum for arm 1.

lambda2   A vector of hazard rates for the event in each analysis time interval by stratum for arm 2.

lambda3   A vector of hazard rates for the event in each analysis time interval by stratum for arm 3.

gamma1   The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 1.

gamma2   The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 2.

gamma3   The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 3.

accrualDuration
    Duration of the enrollment period.

followupTime   Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

rho1   The first parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

rho2   The second parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

plannedEvents The planned cumulative total number of events at Look 1 to Look kMax for Arms A and C combined.

plannedTime   The calendar times for the analyses. To use calendar time to plan the analyses, plannedEvents should be missing.

maxNumberOfIterations
    The number of simulation iterations. Defaults to 1000.

maxNumberOfRawDatasetsPerStage
    The number of raw datasets per stage to extract.

seed   The seed to reproduce the simulation results. The seed from the environment will be used if left unspecified.

Value

A list with 2 components:

- sumdata: A data frame of summary data by iteration and stage:
  - iterationNumber: The iteration number.
  - eventsNotAchieved: Whether the target number of events is not achieved for the iteration.

- – stageNumber: The stage number, covering all stages even if the trial stops at an interim look.
- – analysisTime: The time for the stage since trial start.
- – accruals1: The number of subjects enrolled at the stage for the active treatment 1 group.
- – accruals2: The number of subjects enrolled at the stage for the active treatment 2 group.
- – accruals3: The number of subjects enrolled at the stage for the control group.
- – totalAccruals: The total number of subjects enrolled at the stage.
- – events1: The number of events at the stage for the active treatment 1 group.
- – events2: The number of events at the stage for the active treatment 2 group.
- – events3: The number of events at the stage for the control group.
- – totalEvents: The total number of events at the stage.
- – dropouts1: The number of dropouts at the stage for the active treatment 1 group.
- – dropouts2: The number of dropouts at the stage for the active treatment 2 group.
- – dropouts3: The number of dropouts at the stage for the control group.
- – totalDropouts: The total number of dropouts at the stage.
- – logRankStatistic13: The log-rank test Z-statistic comparing the active treatment 1 to the control.
- – logRankStatistic23: The log-rank test Z-statistic comparing the active treatment 2 to the control.
- – logRankStatistic12: The log-rank test Z-statistic comparing the active treatment 1 to the active treatment 2.

- rawdata (exists if maxNumberOfRawDatasetsPerStage is a positive integer): A data frame for subject-level data for selected replications, containing the following variables:

  - – iterationNumber: The iteration number.
  - – stageNumber: The stage under consideration.
  - – analysisTime: The time for the stage since trial start.
  - – subjectId: The subject ID.
  - – arrivalTime: The enrollment time for the subject.
  - – stratum: The stratum for the subject.
  - – treatmentGroup: The treatment group (1, 2, or 3) for the subject.
  - – survivalTime: The underlying survival time for the subject.
  - – dropoutTime: The underlying dropout time for the subject.
  - – timeUnderObservation: The time under observation since randomization for the subject.
  - – event: Whether the subject experienced the event.
  - – dropoutEvent: Whether the subject dropped out.

Author(s)

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Examples

```
sim1 = lrsim3a(
  kMax = 3,
  allocation1 = 2,
  allocation2 = 2,
  allocation3 = 1,
  accrualTime = c(0, 8),
  accrualIntensity = c(10, 28),
  piecewiseSurvivalTime = 0,
  lambda1 = log(2)/12*0.60,
  lambda2 = log(2)/12*0.70,
  lambda3 = log(2)/12,
  accrualDuration = 30.143,
  plannedEvents = c(186, 259, 295),
  maxNumberOfIterations = 1000,
  maxNumberOfRawDatasetsPerStage = 1,
  seed = 314159)

head(sim1$sumdata)
head(sim1$rawdata)
```

---

lrstat *Number of Subjects Having an Event and Log-Rank Statistics*

Description

Obtains the number of subjects accrued, number of events, number of dropouts, and number of subjects reaching the maximum follow-up in each group, mean and variance of weighted log-rank score statistic, estimated hazard ratio from weighted Cox regression and variance of log hazard ratio estimate at given calendar times.

Usage

```
lrstat(
  time = NA_real_,
  hazardRatioH0 = 1,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
```

```
    fixedFollowup = 0L,
    rho1 = 0,
    rho2 = 0,
    predictTarget = 2L
)
```

Arguments

time	A vector of calendar times at which to calculate the number of events and the mean and variance of log-rank test score statistic.
hazardRatioH0	Hazard ratio under the null hypothesis for the active treatment versus control. Defaults to 1 for superiority test.
allocationRatioPlanned	
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).
accrualIntensity	
	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	
	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.
stratumFraction	
	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
lambda1	A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.
lambda2	A vector of hazard rates for the event in each analysis time interval by stratum for the control group.
gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.
gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.
accrualDuration	
	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
rho1	The first parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.
rho2	The second parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

predictTarget   The target of prediction. Set predictTarget = 1 to predict the number of events only. Set predictTarget = 2 (default) to predict the number of events and log-rank score statistic mean and variance. Set predictTarget = 3 to predict the number of events, log-rank score statistic mean and variance, and hazard ratio and variance of log hazard ratio.

Value

A data frame containing the following variables if predictTarget = 1:

- time: The analysis time since trial start.
- subjects: The number of enrolled subjects.
- nevents: The total number of events.
- nevents1: The number of events in the active treatment group.
- nevents2: The number of events in the control group.
- ndropouts: The total number of dropouts.
- ndropouts1: The number of dropouts in the active treatment group.
- ndropouts2: The number of dropouts in the control group.
- nfmax: The total number of subjects reaching maximum follow-up.
- nfmax1: The number of subjects reaching maximum follow-up in the active treatment group.
- nfmax2: The number of subjects reaching maximum follow-up in the control group.

If predictTarget = 2, the following variables will also be included:

- uscore: The numerator of the log-rank test statistic.
- vscore: The variance of the log-rank score test statistic.
- logRankZ: The log-rank test statistic on the Z-scale.
- hazardRatioH0: The hazard ratio under the null hypothesis.

Furthermore, if predictTarget = 3, the following additional variables will also be included:

- HR: The average hazard ratio from weighted Cox regression.
- vlogHR: The variance of log hazard ratio.
- zlogHR: The Z-statistic for log hazard ratio.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Piecewise accrual, piecewise exponential survivals, and 5% dropout by
# the end of 1 year.

lrstat(time = c(22, 40), allocationRatioPlanned = 1,
       accrualTime = seq(0, 8),
       accrualIntensity = 26/9*seq(1, 9),
```

```
        piecewiseSurvivalTime = c(0, 6),
        lambda1 = c(0.0533, 0.0309),
        lambda2 = c(0.0533, 0.0533),
        gamma1 = -log(1-0.05)/12,
        gamma2 = -log(1-0.05)/12,
        accrualDuration = 22,
        followupTime = 18, fixedFollowup = FALSE)
```

---

lrtest   *Log-Rank Test of Survival Curve Difference*

Description

Obtains the log-rank test using the Fleming-Harrington family of weights.

Usage

```
lrtest(
  data,
  rep = "",
  stratum = "",
  treat = "treat",
  time = "time",
  event = "event",
  rho1 = 0,
  rho2 = 0
)
```

Arguments

data	The input data frame that contains the following variables:
	• rep: The replication for by-group processing.
	• stratum: The stratum.
	• treat: The treatment.
	• time: The possibly right-censored survival time.
	• event: The event indicator.
rep	The name of the replication variable in the input data.
stratum	The name of the stratum variable in the input data.
treat	The name of the treatment variable in the input data.
time	The name of the time variable in the input data.
event	The name of the event variable in the input data.
rho1	The first parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.
rho2	The second parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

Value

A data frame with the following variables:

- uscore: The numerator of the log-rank test statistic.

- vscore: The variance of the log-rank score test statistic.

- logRankZ: The Z-statistic value.

- logRankPValue: The one-sided p-value.

- rho1: The first parameter of the Fleming-Harrington weights.

- rho2: The second parameter of the Fleming-Harrington weights.

- rep: The replication.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
df <- lrtest(data = rawdata, rep = "iterationNumber",
             stratum = "stratum", treat = "treatmentGroup",
             time = "timeUnderObservation", event = "event",
             rho1 = 0.5, rho2 = 0)
head(df)
```

---

mnOddsRatioCI	*Miettinen-Nurminen Score Confidence Interval for Two-Sample Odds Ratio*

Description

Obtains the Miettinen-Nurminen score confidence interval for two-sample odds ratio possibly with stratification.

Usage

```
mnOddsRatioCI(
  n1 = NA_real_,
  y1 = NA_real_,
  n2 = NA_real_,
  y2 = NA_real_,
  cilevel = 0.95
)
```

Arguments

n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.
cilevel	The confidence interval level.

Details

The Mantel-Haenszel sample size weights are used for stratified samples.

Value

A list with two components:

- data A data frame containing the input sample size and number of responses for each treatment group. It has the following variables:
  - n1: The sample size for the active treatment group.
  - y1: The number of responses for the active treatment group.
  - n2: The sample size for the control group.
  - y2: The number of responses for the control group.
- estimates: A data frame containing the point estimate and confidence interval for odds ratio. It has the following variables:
  - scale: The scale of treatment effect.
  - estimate: The point estimate.
  - lower: The lower limit of the confidence interval.
  - upper: The upper limit of the confidence interval.
  - cilevel: The confidence interval level.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
mnOddsRatioCI(n1 = c(10,10), y1 = c(4,3), n2 = c(20,10), y2 = c(2,0))
```

---

mnRateDiffCI	*Miettinen-Nurminen Score Confidence Interval for Two-Sample Rate Difference*

Description

Obtains the Miettinen-Nurminen score confidence interval for two-sample rate difference possibly with stratification.

Usage

```
mnRateDiffCI(
  t1 = NA_real_,
  y1 = NA_real_,
  t2 = NA_real_,
  y2 = NA_real_,
  cilevel = 0.95
)
```

Arguments

t1	The exposure for the active treatment group.
y1	The number of events for the active treatment group.
t2	The exposure for the control group.
y2	The number of events for the control group.
cilevel	The confidence interval level.

Details

The Mantel-Haenszel weights are used for stratified samples.

Value

A list with two components:

- data A data frame containing the input exposure and number of events for each treatment group. It has the following variables:
    - t1: The exposure for the active treatment group.
    - y1: The number of events for the active treatment group.
    - t2: The exposure for the control group.
    - y2: The number of events for the control group.
- estimates: A data frame containing the point estimate and confidence interval for rate difference. It has the following variables:
    - scale: The scale of treatment effect.
    - estimate: The point estimate.

 – lower: The lower limit of the confidence interval.

 – upper: The upper limit of the confidence interval.

 – cilevel: The confidence interval level.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
mnRateDiffCI(t1 = c(10,10), y1 = c(4,3), t2 = c(20,10), y2 = c(2,0))
```

---

mnRateRatioCI	*Miettinen-Nurminen Score Confidence Interval for Two-Sample Rate Ratio*

Description

Obtains the Miettinen-Nurminen score confidence interval for two-sample rate ratio possibly with stratification.

Usage

```
mnRateRatioCI(t1, y1, t2, y2, cilevel = 0.95)
```

Arguments

t1	The exposure for the active treatment group.
y1	The number of events for the active treatment group.
t2	The exposure for the control group.
y2	The number of events for the control group.
cilevel	The confidence interval level.

Details

The Mantel-Haenszel weights are used for stratified samples.

Value

A list with two components:

 • data A data frame containing the input exposure and number of events for each treatment group. It has the following variables:

 – t1: The exposure for the active treatment group.
 – y1: The number of events for the active treatment group.
 – t2: The exposure for the control group.

> – y2: The number of events for the control group.

- estimates: A data frame containing the point estimate and confidence interval for rate ratio. It has the following variables:

  – scale: The scale of treatment effect.
  – estimate: The point estimate.
  – lower: The lower limit of the confidence interval.
  – upper: The upper limit of the confidence interval.
  – cilevel: The confidence interval level.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
mnRateRatioCI(t1 = c(10,10), y1 = c(4,3), t2 = c(20,10), y2 = c(2,0))
```

---

mnRiskDiffCI	*Miettinen-Nurminen Score Confidence Interval for Two-Sample Risk Difference*

Description

Obtains the Miettinen-Nurminen score confidence interval for two-sample risk difference possibly with stratification.

Usage

```
mnRiskDiffCI(
  n1 = NA_real_,
  y1 = NA_real_,
  n2 = NA_real_,
  y2 = NA_real_,
  cilevel = 0.95
)
```

Arguments

n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.
cilevel	The confidence interval level.

Details

The Mantel-Haenszel sample size weights are used for stratified samples.

Value

A list with two components:

- data A data frame containing the input sample size and number of responses for each treatment group. It has the following variables:
    - n1: The sample size for the active treatment group.
    - y1: The number of responses for the active treatment group.
    - n2: The sample size for the control group.
    - y2: The number of responses for the control group.
- estimates: A data frame containing the point estimate and confidence interval for risk difference. It has the following variables:
    - scale: The scale of treatment effect.
    - estimate: The point estimate.
    - lower: The lower limit of the confidence interval.
    - upper: The upper limit of the confidence interval.
    - cilevel: The confidence interval level.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
mnRiskDiffCI(n1 = c(10,10), y1 = c(4,3), n2 = c(20,10), y2 = c(2,0))
```

---

mnRiskRatioCI   *Miettinen-Nurminen Score Confidence Interval for Two-Sample Risk Ratio*

Description

Obtains the Miettinen-Nurminen score confidence interval for two-sample risk ratio possibly with stratification.

Usage

```
mnRiskRatioCI(
  n1 = NA_real_,
  y1 = NA_real_,
  n2 = NA_real_,
  y2 = NA_real_,
  cilevel = 0.95
)
```

Arguments

n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.
cilevel	The confidence interval level.

Details

The Mantel-Haenszel sample size weights are used for stratified samples.

Value

A list with two components:

- data A data frame containing the input sample size and number of responses for each treatment group. It has the following variables:

  - n1: The sample size for the active treatment group.
  - y1: The number of responses for the active treatment group.
  - n2: The sample size for the control group.
  - y2: The number of responses for the control group.

- estimates: A data frame containing the point estimate and confidence interval for risk ratio. It has the following variables:

  - scale: The scale of treatment effect.
  - estimate: The point estimate.
  - lower: The lower limit of the confidence interval.
  - upper: The upper limit of the confidence interval.
  - cilevel: The confidence interval level.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
mnRiskRatioCI(n1 = c(10,10), y1 = c(4,3), n2 = c(20,10), y2 = c(2,0))
```

---

mTPI2Table   *mTPI-2 Decision Table*

Description

Obtains the decision table for the modified toxicity probability interval-2 (mTPI-2) design.

Usage

```
mTPI2Table(
  nMax = NA_integer_,
  pT = 0.3,
  epsilon1 = 0.05,
  epsilon2 = 0.05,
  a = 1,
  b = 1,
  pExcessTox = 0.95
)
```

Arguments

nMax	The maximum number of subjects in a dose cohort.
pT	The target toxicity probability. Defaults to 0.3.
epsilon1	The lower equivalence margin from the target. Defaults to 0.05.
epsilon2	The upper equivalence margin from the target. Defaults to 0.05.
a	The prior toxicity parameter for the beta prior.
b	The prior non-toxicity parameter for the beta prior.
pExcessTox	The threshold for excessive toxicity, i.e., if Prob(p > pT | Data) > pExcessTox, then the current and all higher doses will be excluded and never be used again in the remainder of the trial to avoid any other subjects receiving treatment at those doses. Defaults to 0.95.

Value

An S3 class mTPI2Table object with the following components:

- settings: The input settings data frame with the following variables:
  - nMax: The maximum number of subjects in a dose cohort.
  - pT: The target toxicity probability.
  - epsilon1: The lower equivalence margin from the target.
  - epsilon2: The upper equivalence margin from the target.
  - a: The prior toxicity parameter for the beta prior.
  - b: The prior non-toxicity parameter for the beta prior.
  - pExcessTox: The threshold for excessive toxicity.

- subintervals: The subintervals of equal length in the mTPI-2 design. It includes the following variables:

    – lower: The lower bound of the subinterval.
    – upper: The upper bound of the subinterval.
    – decision: The dosing decision for the subinterval.

- decisionDataFrame: The decision data frame for the mTPI-2 design. It includes the following variables:

    – n: The sample size.
    – y: The number of toxicities.
    – decision: The dosing decision.

- decisionMatrix: The decision matrix corresponding to the decision data frame.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
mTPI2Table(nMax = 18, pT = 0.3, epsilon1 = 0.05, epsilon2 = 0.05)
```

---

natrisk   *Number of Subjects at Risk*

Description

Obtains the number of subjects at risk at given analysis times for each treatment group.

Usage

```
natrisk(
  time = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  minFollowupTime = NA_real_,
  maxFollowupTime = NA_real_
)
```

Arguments

`time`	A vector of analysis times at which to calculate the number of patients at risk.
`allocationRatioPlanned`	
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
`accrualTime`	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).
`accrualIntensity`	
	A vector of accrual intensities. One for each accrual time interval.
`piecewiseSurvivalTime`	
	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.
`lambda1`	A vector of hazard rates for the event for the active treatment group. One for each analysis time interval.
`lambda2`	A vector of hazard rates for the event for the control group. One for each analysis time interval.
`gamma1`	The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the active treatment group.
`gamma2`	The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the control group.
`accrualDuration`	
	Duration of the enrollment period.
`minFollowupTime`	
	Follow-up time for the last enrolled subject.
`maxFollowupTime`	
	Follow-up time for the first enrolled subject. For fixed follow-up, `maxFollowupTime = minFollowupTime`. For variable follow-up, `maxFollowupTime = accrualDuration + minFollowupTime`.

Value

A matrix of the number of patients at risk at the specified analysis times (row) for each treatment group (column).

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Piecewise accrual, piecewise exponential survivals, and 5% dropout by
# the end of 1 year.

natrisk(time = c(9, 24), allocationRatioPlanned = 1,
```

```
        accrualTime = c(0, 3), accrualIntensity = c(10, 20),
        piecewiseSurvivalTime = c(0, 6),
        lambda1 = c(0.0533, 0.0309), lambda2 = c(0.0533, 0.0533),
        gamma1 = -log(1-0.05)/12, gamma2 = -log(1-0.05)/12,
        accrualDuration = 12, minFollowupTime = 18,
        maxFollowupTime = 30)
```

---

nbpower   *Power for Negative Binomial Rate Ratio*

Description

Estimates the power for negative binomial rate ratio test.

Usage

```
nbpower(
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  rateRatioH0 = 1,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  kappa1 = NA_real_,
  kappa2 = NA_real_,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  spendingTime = NA_real_,
  studyDuration = NA_real_,
  nullVariance = 0L
)
```

Arguments

kMax   The maximum number of stages.

informationRates
                     The information rates. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping
                     Indicators of whether efficacy stopping is allowed at each stage. Defaults to true
                     if left unspecified.

futilityStopping
                     Indicators of whether futility stopping is allowed at each stage. Defaults to true
                     if left unspecified.

criticalValues   Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha   The significance level. Defaults to 0.025.

typeAlphaSpending
                     The type of alpha spending. One of the following: "OF" for O'Brien-Fleming
                     boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries,
                     "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spend-
                     ing function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang,
                     Shi & DeCani spending function, "user" for user defined spending, and "none"
                     for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending
                     The parameter value for the alpha spending. Corresponds to Delta for "WT",
                     rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending
                     The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds   Lower boundaries on the z-test statistic scale for stopping for futility at stages 1,
                     ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds
                     are non-binding for the calculation of critical values.

typeBetaSpending
                     The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming
                     type spending function, "sfP" for Pocock type spending function, "sfKD" for
                     Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending
                     function, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending
                     The parameter value for the beta spending. Corresponds to rho for "sfKD", and
                     gamma for "sfHSD".

rateRatioH0   Rate ratio under the null hypothesis.

allocationRatioPlanned
                     Allocation ratio for the active treatment versus control. Defaults to 1 for equal
                     randomization.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time
                     intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual
                     intervals: [0, 3) and [3, Inf).

accrualIntensity
                     A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

kappa1 The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the active treatment group by stratum.

kappa2 The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the control group by stratum.

lambda1 The rate parameter of the negative binomial distribution for the active treatment group by stratum.

lambda2 The rate parameter of the negative binomial distribution for the control group by stratum.

gamma1 The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.

gamma2 The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

studyDuration Study duration for fixed follow-up design. Defaults to missing, which is to be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and followupTime.

nullVariance Whether to calculate the variance for log rate ratio under the null hypothesis.

Value

An S3 class nbpower object with 4 components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - numberOfEvents: The total number of events.
  - numberOfDropouts: The total number of dropouts.
  - numbeOfSubjects: The total number of subjects.
  - exposure: The total exposure.

- – studyDuration: The total study duration.
- – information: The maximum information.
- – expectedNumberOfEvents: The expected number of events.
- – expectedNumberOfDropouts: The expected number of dropouts.
- – expectedNumberOfSubjects: The expected number of subjects.
- – expectedExposure: The expected exposure.
- – expectedStudyDuration: The expected study duration.
- – expectedInformation: The expected information.
- – accrualDuration: The accrual duration.
- – followupTime: The follow-up duration.
- – fixedFollowup: Whether a fixed follow-up design is used.
- – kMax: The number of stages.
- – rateRatioH0: The rate ratio under the null hypothesis.
- – rateRatio: The rate ratio.

- byStageResults: A data frame containing the following variables:

  - – informationRates: The information rates.
  - – efficacyBounds: The efficacy boundaries on the Z-scale.
  - – futilityBounds: The futility boundaries on the Z-scale.
  - – rejectPerStage: The probability for efficacy stopping.
  - – futilityPerStage: The probability for futility stopping.
  - – cumulativeRejection: The cumulative probability for efficacy stopping.
  - – cumulativeFutility: The cumulative probability for futility stopping.
  - – cumulativeAlphaSpent: The cumulative alpha spent.
  - – numberOfEvents: The number of events.
  - – numberOfDropouts: The number of dropouts.
  - – numberOfSubjects: The number of subjects.
  - – exposure: The exposure.
  - – analysisTime: The average time since trial start.
  - – efficacyRateRatio: The efficacy boundaries on the rate ratio scale.
  - – futilityRateRatio: The futility boundaries on the rate ratio scale.
  - – efficacyP: The efficacy boundaries on the p-value scale.
  - – futilityP: The futility boundaries on the p-value scale.
  - – information: The cumulative information.
  - – efficacyStopping: Whether to allow efficacy stopping.
  - – futilityStopping: Whether to allow futility stopping.

- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, typeBetaSpending, parameterBetaSpending, allocationRatioPlanned, accrualTime, accuralIntensity, piecewiseSurvivalTime, kappa1, kappa2, lambda1, lambda2, gamma1, gamma2, spendingTime, and nullVariance.

- byTreatmentCounts: A list containing the following counts by treatment group:

  - – numberOfEvents1: The number of events by stage for the treatment group.
  - – numberOfDropouts1: The number of dropouts by stage for the treatment group.

- numberOfSubjects1: The number of subjects by stage for the treatment group.
- exposure1: The exposure by stage for the treatment group.
- numberOfEvents2: The number of events by stage for the control group.
- numberOfDropouts2: The number of dropouts by stage for the control group.
- numberOfSubjects2: The number of subjects by stage for the control group.
- exposure2: The exposure by stage for the control group.
- expectedNumberOfEvents1: The expected number of events for the treatment group.
- expectedNumberOfDropouts1: The expected number of dropouts for the treatment group.
- expectedNumberOfSubjects1: The expected number of subjects for the treatment group.
- expectedExposure1: The expected exposure for the treatment group.
- expectedNumberOfEvents2: The expected number of events for control group.
- expectedNumberOfDropouts2: The expected number of dropouts for the control group.
- expectedNumberOfSubjects2: The expected number of subjects for the control group.
- expectedExposure2: The expected exposure for the control group.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

See Also

nbstat

Examples

```
# Example 1: Variable follow-up design

nbpower(kMax = 2, informationRates = c(0.5, 1),
        alpha = 0.025, typeAlphaSpending = "sfOF",
        accrualIntensity = 1956/1.25,
        stratumFraction = c(0.2, 0.8),
        kappa1 = 5, kappa2 = 5,
        lambda1 = c(0.7*0.125, 0.75*0.25),
        lambda2 = c(0.125, 0.25),
        gamma1 = 0, gamma2 = 0,
        accrualDuration = 1.25,
        followupTime = 2.75, fixedFollowup = FALSE,
        nullVariance = 1)

# Example 2: Fixed follow-up design

nbpower(kMax = 2, informationRates = c(0.5, 1),
        alpha = 0.025, typeAlphaSpending = "sfOF",
        accrualIntensity = 220/1.5,
        kappa1 = 3, kappa2 = 3,
        lambda1 = 0.5*8.4, lambda2 = 8.4,
        gamma1 = 0, gamma2 = 0,
        accrualDuration = 1.5,
        followupTime = 0.5, fixedFollowup = TRUE)
```

Description

Estimates the power, stopping probabilities, and expected sample size in a one-group negative binomial design.

Usage

```
nbpower1s(
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  lambdaH0 = NA_real_,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  kappa = NA_real_,
  lambda = NA_real_,
  gamma = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  spendingTime = NA_real_,
  studyDuration = NA_real_
)
```

Arguments

kMax   The maximum number of stages.

informationRates

                The information rates. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

                Indicators of whether efficacy stopping is allowed at each stage. Defaults to true
                if left unspecified.

futilityStopping

    Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha   The significance level. Defaults to 0.025.

typeAlphaSpending

    The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

    The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

    The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

    The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

    The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

lambdaH0   The rate parameter of the negative binomial distribution under the null hypothesis.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

    A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

    A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

    A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

kappa   The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) of the negative binomial distribution by stratum.

lambda   The rate parameter of the negative binomial distribution under the alternative hypothesis by stratum.

gamma   The hazard rate for exponential dropout or a vector of hazard rates for piecewise exponential dropout by stratum. Defaults to 0 for no dropout.

accrualDuration
               Duration of the enrollment period.

followupTime   Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

studyDuration Study duration for fixed follow-up design. Defaults to missing, which is to be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and followupTime.

Value

An S3 class nbpower1s object with 3 components:

- overallResults: A data frame containing the following variables:
    - overallReject: The overall rejection probability.
    - alpha: The overall significance level.
    - numberOfEvents: The total number of events.
    - numberOfDropouts: The total number of dropouts.
    - numbeOfSubjects: The total number of subjects.
    - exposure: The total exposure.
    - studyDuration: The total study duration.
    - information: The maximum information.
    - expectedNumberOfEvents: The expected number of events.
    - expectedNumberOfDropouts: The expected number of dropouts.
    - expectedNumberOfSubjects: The expected number of subjects.
    - expectedExposure: The expected exposure.
    - expectedStudyDuration: The expected study duration.
    - expectedInformation: The expected information.
    - accrualDuration: The accrual duration.
    - followupTime: The follow-up duration.
    - fixedFollowup: Whether a fixed follow-up design is used.
    - kMax: The number of stages.
    - lambdaH0: The rate parameter of the negative binomial distribution under the null hypothesis.
    - lambda: The overall rate parameter of the negative binomial distribution under the alternative hypothesis.

- byStageResults: A data frame containing the following variables:
    - informationRates: The information rates.
    - efficacyBounds: The efficacy boundaries on the Z-scale.

- – futilityBounds: The futility boundaries on the Z-scale.
    - – rejectPerStage: The probability for efficacy stopping.
    - – futilityPerStage: The probability for futility stopping.
    - – cumulativeRejection: The cumulative probability for efficacy stopping.
    - – cumulativeFutility: The cumulative probability for futility stopping.
    - – cumulativeAlphaSpent: The cumulative alpha spent.
    - – numberOfEvents: The number of events.
    - – numberOfDropouts: The number of dropouts.
    - – numberOfSubjects: The number of subjects.
    - – exposure: The exposure.
    - – analysisTime: The average time since trial start.
    - – efficacyRate: The efficacy boundaries on the rate scale.
    - – futilityRate: The futility boundaries on the rate scale.
    - – efficacyP: The efficacy boundaries on the p-value scale.
    - – futilityP: The futility boundaries on the p-value scale.
    - – information: The cumulative information.
    - – efficacyStopping: Whether to allow efficacy stopping.
    - – futilityStopping: Whether to allow futility stopping.
- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, typeBetaSpending, parameterBetaSpending, accrualTime, accuralIntensity, piecewiseSurvivalTime, stratumFraction, kappa, lambda, gamma, and spendingTime.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

See Also

nbstat

Examples

```
# Example 1: Variable follow-up design

nbpower1s(kMax = 2, informationRates = c(0.5, 1),
          alpha = 0.025, typeAlphaSpending = "sfOF",
          lambdaH0 = 0.125, accrualIntensity = 500,
          stratumFraction = c(0.2, 0.8),
          kappa = c(3, 5), lambda = c(0.0875, 0.085),
          gamma = 0, accrualDuration = 1.25,
          followupTime = 2.75, fixedFollowup = FALSE)

# Example 2: Fixed follow-up design

nbpower1s(kMax = 2, informationRates = c(0.5, 1),
          alpha = 0.025, typeAlphaSpending = "sfOF",
          lambdaH0 = 8.4, accrualIntensity = 40,
```

```
                  kappa = 3, lambda = 0.5*8.4,
                  gamma = 0, accrualDuration = 1.5,
                  followupTime = 0.5, fixedFollowup = TRUE)
```

---

nbpowerequiv   *Power for Equivalence in Negative Binomial Rate Ratio*

Description

Obtains the power for equivalence in negative binomial rate ratio.

Usage

```
nbpowerequiv(
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  rateRatioLower = NA_real_,
  rateRatioUpper = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  kappa1 = NA_real_,
  kappa2 = NA_real_,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  spendingTime = NA_real_,
  studyDuration = NA_real_
)
```

Arguments

kMax   The maximum number of stages.

informationRates

                The information rates. Defaults to (1:kMax) / kMax if left unspecified.

criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level for each of the two one-sided tests. Defaults to 0.05.
typeAlphaSpending	
	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	
	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	
	The user defined alpha spending. Cumulative alpha spent up to each stage.
rateRatioLower	The lower equivalence limit of rate ratio.
rateRatioUpper	The upper equivalence limit of rate ratio.
allocationRatioPlanned	
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).
accrualIntensity	
	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	
	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.
stratumFraction	
	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
kappa1	The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the active treatment group by stratum.
kappa2	The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the control group by stratum.
lambda1	The rate parameter of the negative binomial distribution for the active treatment group by stratum.
lambda2	The rate parameter of the negative binomial distribution for the control group by stratum.
gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.
gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration
             Duration of the enrollment period.

followupTime   Follow-up time for the last enrolled subject.

fixedFollowup   Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

studyDuration   Study duration for fixed follow-up design. Defaults to missing, which is to be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and followupTime.

Value

An S3 class nbpowerequiv object with 4 components:

- overallResults: A data frame containing the following variables:
    - overallReject: The overall rejection probability.
    - alpha: The overall significance level.
    - numberOfEvents: The total number of events.
    - numbeOfSubjects: The total number of subjects.
    - exposure: The total exposure.
    - studyDuration: The total study duration.
    - information: The maximum information.
    - expectedNumberOfEvents: The expected number of events.
    - expectedNumberOfSubjects: The expected number of subjects.
    - expectedExposure: The expected exposure.
    - expectedStudyDuration: The expected study duration.
    - expectedInformation: The expected information.
    - kMax: The number of stages.
    - rateRatioLower: The lower equivalence limit of rate ratio.
    - rateRatioUpper: The upper equivalence limit of rate ratio.
    - rateRatio: The rate ratio.
    - accrualDuration: The accrual duration.
    - followupTime: The follow-up duration.
    - fixedFollowup: Whether a fixed follow-up design is used.
- byStageResults: A data frame containing the following variables:
    - informationRates: The information rates.
    - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
    - rejectPerStage: The probability for efficacy stopping.
    - cumulativeRejection: The cumulative probability for efficacy stopping.
    - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
    - cumulativeAttainedAlphaH10: The cumulative alpha attained under H10.

- cumulativeAttainedAlphaH20: The cumulative alpha attained under H20.

- numberOfEvents: The number of events.

- numberOfDropouts: The number of dropouts.

- numberOfSubjects: The number of subjects.

- exposure: The exposure.

- analysisTime: The average time since trial start.

- efficacyRateRatioLower: The efficacy boundaries on the rate ratio scale for the one-sided null hypothesis at the lower equivalence limit.

- efficacyRateRatioUpper: The efficacy boundaries on the rate ratio scale for the one-sided null hypothesis at the upper equivalence limit.

- efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.

- information: The cumulative information.

- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, allocationRatioPlanned, accrualTime, accuralIntensity, piecewiseSurvivalTime, stratumFraction, kappa1, kappa2, lambda1, lambda2, gamma1, gamma2, spendingTime.

- byTreatmentCounts: A list containing the following counts by treatment group:

  - numberOfEvents1: The number of events by stage for the treatment group.

  - numberOfDropouts1: The number of dropouts by stage for the treatment group.

  - numberOfSubjects1: The number of subjects by stage for the treatment group.

  - exposure1: The exposure by stage for the treatment group.

  - numberOfEvents2: The number of events by stage for the control group.

  - numberOfDropouts2: The number of dropouts by stage for the control group.

  - numberOfSubjects2: The number of subjects by stage for the control group.

  - exposure2: The exposure by stage for the control group.

  - expectedNumberOfEvents1: The expected number of events for the treatment group.

  - expectedNumberOfDropouts1: The expected number of dropouts for the treatment group.

  - expectedNumberOfSubjects1: The expected number of subjects for the treatment group.

  - expectedExposure1: The expected exposure for the treatment group.

  - expectedNumberOfEvents2: The expected number of events for control group.

  - expectedNumberOfDropouts2: The expected number of dropouts for the control group.

  - expectedNumberOfSubjects2: The expected number of subjects for the control group.

  - expectedExposure2: The expected exposure for the control group.

Author(s)

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See Also

[nbstat](#)

Examples

```
# Example 1: Variable follow-up design
nbpowerequiv(kMax = 2, informationRates = c(0.5, 1),
             alpha = 0.05, typeAlphaSpending = "sfOF",
             rateRatioLower = 2/3, rateRatioUpper = 3/2,
             accrualIntensity = 1956/1.25,
             kappa1 = 5, kappa2 = 5,
             lambda1 = 0.125, lambda2 = 0.125,
             gamma1 = 0, gamma2 = 0,
             accrualDuration = 1.25,
             followupTime = 2.75, fixedFollowup = FALSE)

# Example 2: Fixed follow-up design
nbpowerequiv(kMax = 2, informationRates = c(0.5, 1),
             alpha = 0.05, typeAlphaSpending = "sfOF",
             rateRatioLower = 0.5, rateRatioUpper = 2,
             accrualIntensity = 220/1.5,
             stratumFraction = c(0.2, 0.8),
             kappa1 = 3, kappa2 = 3,
             lambda1 = c(8.4, 10.2),
             lambda2 = c(8.0, 11.5),
             gamma1 = 0, gamma2 = 0,
             accrualDuration = 1.5,
             followupTime = 0.5, fixedFollowup = TRUE)
```

---

nbsamplesize   *Sample Size for Negative Binomial Rate Ratio*

Description

Obtains the needed accrual duration given power and follow-up time, the needed follow-up time given power and accrual duration, or the needed absolute accrual rates given power, accrual duration, follow-up duration, and relative accrual rates in a two-group negative binomial design.

Usage

```
nbsamplesize(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
```

```
    futilityBounds = NA_real_,
    typeBetaSpending = "none",
    parameterBetaSpending = NA_real_,
    userBetaSpending = NA_real_,
    rateRatioH0 = 1,
    allocationRatioPlanned = 1,
    accrualTime = 0L,
    accrualIntensity = NA_real_,
    piecewiseSurvivalTime = 0L,
    stratumFraction = 1L,
    kappa1 = NA_real_,
    kappa2 = NA_real_,
    lambda1 = NA_real_,
    lambda2 = NA_real_,
    gamma1 = 0L,
    gamma2 = 0L,
    accrualDuration = NA_real_,
    followupTime = NA_real_,
    fixedFollowup = 0L,
    interval = as.numeric(c(0.001, 240)),
    spendingTime = NA_real_,
    rounding = 1L,
    nullVariance = 0L
)
```

Arguments

beta   Type II error. Defaults to 0.2.

kMax   The maximum number of stages.

informationRates

                The information rates. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

                Indicators of whether efficacy stopping is allowed at each stage. Defaults to true
                if left unspecified.

futilityStopping

                Indicators of whether futility stopping is allowed at each stage. Defaults to true
                if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha   The significance level. Defaults to 0.025.

typeAlphaSpending

                The type of alpha spending. One of the following: "OF" for O'Brien-Fleming
                boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries,
                "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spend-
                ing function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang,
                Shi & DeCani spending function, "user" for user defined spending, and "none"
                for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

> The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

> The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds   Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

> The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

> The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

> The user defined beta spending. Cumulative beta spent up to each stage.

rateRatioH0   Rate ratio under the null hypothesis.

allocationRatioPlanned

> Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

> A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

> A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

> A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

kappa1   The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the active treatment group by stratum.

kappa2   The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the control group by stratum.

lambda1   The rate parameter of the negative binomial distribution for the active treatment group by stratum.

lambda2   The rate parameter of the negative binomial distribution for the control group by stratum.

gamma1   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.

gamma2   The hazard rate for exponential dropout, a vector of hazard rates for piece-wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration

     Duration of the enrollment period.

followupTime   Follow-up time for the last enrolled subject.

fixedFollowup   Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

interval   The interval to search for the solution of accrualDuration, followupDuration, or the proportionality constant of accrualIntensity. Defaults to c(0.001, 240).

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

rounding   Whether to round up sample size. Defaults to 1 for sample size rounding.

nullVariance   Whether to calculate the variance for log rate ratio under the null hypothesis.

Value

A list of two components:

- resultsUnderH1: An S3 class nbpower object under the alternative hypothesis.
- resultsUnderH0: An S3 class nbpower object under the null hypothesis.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

See Also

[nbpower](#)

Examples

```
# Example 1: Obtains follow-up duration given power, accrual intensity,
# and accrual duration for variable follow-up

nbsamplesize(beta = 0.2, kMax = 2,
             informationRates = c(0.5, 1),
             alpha = 0.025, typeAlphaSpending = "sfOF",
             accrualIntensity = 1956/1.25,
             kappa1 = 5, kappa2 = 5,
             lambda1 = 0.0875, lambda2 = 0.125,
             gamma1 = 0, gamma2 = 0,
             accrualDuration = 1.25,
             followupTime = NA, fixedFollowup = FALSE)

# Example 2: Obtains accrual intensity given power, accrual duration, and
# follow-up duration for variable follow-up

nbsamplesize(beta = 0.2, kMax = 2,
             informationRates = c(0.5, 1),
```

```
                  alpha = 0.025, typeAlphaSpending = "sfOF",
                  accrualIntensity = 100,
                  kappa1 = 5, kappa2 = 5,
                  lambda1 = 0.0875, lambda2 = 0.125,
                  gamma1 = 0, gamma2 = 0,
                  accrualDuration = 1.25,
                  followupTime = 2.25, fixedFollowup = FALSE)


# Example 3: Obtains accrual duration given power, accrual intensity, and
# follow-up duration for fixed follow-up

nbsamplesize(beta = 0.2, kMax = 2,
             informationRates = c(0.5, 1),
             alpha = 0.025, typeAlphaSpending = "sfOF",
             accrualIntensity = 1667,
             stratumFraction = c(0.2, 0.8),
             kappa1 = 5, kappa2 = 5,
             lambda1 = c(0.7*0.125, 0.75*0.25),
             lambda2 = c(0.125, 0.25),
             gamma1 = 0, gamma2 = 0,
             accrualDuration = NA,
             followupTime = 0.5, fixedFollowup = TRUE)
```

---

nbsamplesize1s   *Sample Size for One-Sample Negative Binomial Rate*

Description

Obtains the needed accrual duration given power and follow-up time, the needed follow-up time given power and accrual duration, or the needed absolute accrual rates given power, accrual duration, follow-up duration, and relative accrual rates in a one-group negative binomial design.

Usage

```
nbsamplesize1s(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
```

```
    parameterBetaSpending = NA_real_,
    userBetaSpending = NA_real_,
    lambdaH0 = NA_real_,
    accrualTime = 0L,
    accrualIntensity = NA_real_,
    piecewiseSurvivalTime = 0L,
    stratumFraction = 1L,
    kappa = NA_real_,
    lambda = NA_real_,
    gamma = 0L,
    accrualDuration = NA_real_,
    followupTime = NA_real_,
    fixedFollowup = 0L,
    interval = as.numeric(c(0.001, 240)),
    spendingTime = NA_real_,
    rounding = 1L
)
```

Arguments

beta	Type II error. Defaults to 0.2.
kMax	The maximum number of stages.
informationRates	
	The information rates. Defaults to (1:kMax) / kMax if left unspecified.
efficacyStopping	
	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	
	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	
	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	
	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	
	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

        The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

        The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

        The user defined beta spending. Cumulative beta spent up to each stage.

lambdaH0   The rate parameter of the negative binomial distribution under the null hypothesis.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

        A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

        A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

        A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

kappa   The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) of the negative binomial distribution by stratum.

lambda   The rate parameter of the negative binomial distribution under the alternative hypothesis by stratum.

gamma   The hazard rate for exponential dropout or a vector of hazard rates for piecewise exponential dropout by stratum. Defaults to 0 for no dropout.

accrualDuration

        Duration of the enrollment period.

followupTime   Follow-up time for the last enrolled subject.

fixedFollowup   Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

interval   The interval to search for the solution of accrualDuration, followupDuration, or the proportionality constant of accrualIntensity. Defaults to `c(0.001, 240)`.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as `informationRates`.

rounding   Whether to round up sample size. Defaults to 1 for sample size rounding.

Value

A list of two components:

- resultsUnderH1: An S3 class nbpower1s object under the alternative hypothesis.
- resultsUnderH0: An S3 class nbpower1s object under the null hypothesis.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

See Also

nbpower1s

Examples

```
# Example 1: Obtains follow-up duration given power, accrual intensity,
# and accrual duration for variable follow-up

nbsamplesize1s(beta = 0.2, kMax = 2,
               informationRates = c(0.5, 1),
               alpha = 0.025, typeAlphaSpending = "sfOF",
               lambdaH0 = 0.125, accrualIntensity = 500,
               stratumFraction = c(0.2, 0.8),
               kappa = c(3, 5), lambda = c(0.0875, 0.085),
               gamma = 0, accrualDuration = 1.25,
               followupTime = NA, fixedFollowup = FALSE)

# Example 2: Obtains accrual intensity given power, accrual duration, and
# follow-up duration for variable follow-up

nbsamplesize1s(beta = 0.2, kMax = 2,
               informationRates = c(0.5, 1),
               alpha = 0.025, typeAlphaSpending = "sfOF",
               lambdaH0 = 0.125, accrualIntensity = 100,
               kappa = 5, lambda = 0.0875,
               gamma = 0, accrualDuration = 1.25,
               followupTime = 2.25, fixedFollowup = FALSE)


# Example 3: Obtains accrual duration given power, accrual intensity, and
# follow-up duration for fixed follow-up

nbsamplesize1s(beta = 0.2, kMax = 2,
               informationRates = c(0.5, 1),
               alpha = 0.025, typeAlphaSpending = "sfOF",
               lambdaH0 = 8.4, accrualIntensity = 40,
               kappa = 3, lambda = 4.2,
               gamma = 0, accrualDuration = NA,
               followupTime = 0.5, fixedFollowup = TRUE)
```

---

nbsamplesizeequiv   *Sample Size for Equivalence in Negative Binomial Rate Ratio*

Description

Obtains the sample size for equivalence in negative binomial rate ratio.

Usage

```
nbsamplesizeequiv(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  rateRatioLower = NA_real_,
  rateRatioUpper = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  kappa1 = NA_real_,
  kappa2 = NA_real_,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  interval = as.numeric(c(0.001, 240)),
  spendingTime = NA_real_,
  rounding = 1L
)
```

Arguments

beta   The type II error.

kMax   The maximum number of stages.

informationRates
                The information rates. Defaults to (1:kMax) / kMax if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha   The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending
                The type of alpha spending. One of the following: "OF" for O'Brien-Fleming
                boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries,

"sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

rateRatioLower   The lower equivalence limit of rate ratio.

rateRatioUpper   The upper equivalence limit of rate ratio.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

kappa1   The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the active treatment group by stratum.

kappa2   The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the control group by stratum.

lambda1   The rate parameter of the negative binomial distribution for the active treatment group by stratum.

lambda2   The rate parameter of the negative binomial distribution for the control group by stratum.

gamma1   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.

gamma2   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration

Duration of the enrollment period.

followupTime   Follow-up time for the last enrolled subject.

fixedFollowup   Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

interval	The interval to search for the solution of accrualDuration, followupDuration, or the proportionality constant of accrualIntensity. Defaults to `c(0.001, 240)`.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as `informationRates`.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.

Value

An S3 class nbpowerequiv object

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

See Also

[nbpowerequiv](#)

Examples

```
# Example 1: Variable follow-up design and solve for follow-up time
nbsamplesizeequiv(beta = 0.1, kMax = 2, informationRates = c(0.5, 1),
                  alpha = 0.05, typeAlphaSpending = "sfOF",
                  rateRatioLower = 2/3, rateRatioUpper = 3/2,
                  accrualIntensity = 1956/1.25,
                  stratumFraction = c(0.2, 0.8),
                  kappa1 = c(3, 5),
                  kappa2 = c(2, 3),
                  lambda1 = c(0.125, 0.165),
                  lambda2 = c(0.135, 0.175),
                  gamma1 = -log(1-0.05),
                  gamma2 = -log(1-0.10),
                  accrualDuration = 1.25,
                  followupTime = NA, fixedFollowup = FALSE)

# Example 2: Fixed follow-up design and solve for accrual duration
nbsamplesizeequiv(beta = 0.2, kMax = 2, informationRates = c(0.5, 1),
                  alpha = 0.05, typeAlphaSpending = "sfOF",
                  rateRatioLower = 0.5, rateRatioUpper = 2,
                  accrualIntensity = 220/1.5,
                  kappa1 = 3, kappa2 = 3,
                  lambda1 = 8.4, lambda2 = 8.4,
                  gamma1 = 0, gamma2 = 0,
                  accrualDuration = NA,
                  followupTime = 0.5, fixedFollowup = TRUE)
```

---

nbstat   *Negative Binomial Rate Ratio*

Description

Obtains the number of subjects accrued, number of events, number of dropouts, number of subjects reaching the maximum follow-up, total exposure, and variance for log rate in each group, rate ratio, variance, and Wald test statistic of log rate ratio at given calendar times.

Usage

```
nbstat(
  time = NA_real_,
  rateRatioH0 = 1,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  kappa1 = NA_real_,
  kappa2 = NA_real_,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  nullVariance = 0L
)
```

Arguments

time
:   A vector of calendar times for data cut.

rateRatioH0
:   Rate ratio under the null hypothesis.

allocationRatioPlanned
:   Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime
:   A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity
:   A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime
:   A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction	
	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
kappa1	The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the active treatment group by stratum.
kappa2	The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the control group by stratum.
lambda1	The rate parameter of the negative binomial distribution for the active treatment group by stratum.
lambda2	The rate parameter of the negative binomial distribution for the control group by stratum.
gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.
gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.
accrualDuration	
	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
nullVariance	Whether to calculate the variance for log rate ratio under the null hypothesis.

Details

The probability mass function for a negative binomial distribution with dispersion parameter κ_i and rate parameter λ_i is given by

$$P(Y_{ij} = y) = \frac{\Gamma(y + 1/\kappa_i)}{\Gamma(1/\kappa_i)y!} \left(\frac{1}{1 + \kappa_i \lambda_i t_{ij}}\right)^{1/\kappa_i} \left(\frac{\kappa_i \lambda_i t_{ij}}{1 + \kappa_i \lambda_i t_{ij}}\right)^y,$$

where Y_{ij} is the event count for subject j in treatment group i, and t_{ij} is the exposure time for the subject. If $\kappa_i = 0$, the negative binomial distribution reduces to the Poisson distribution.

For treatment group i, let $\beta_i = \log(\lambda_i)$. The log-likelihood for $\{(\kappa_i, \beta_i) : i = 1, 2\}$ can be written as

$$l = \sum_{i=1}^{2} \sum_{j=1}^{n_i} \{\log \Gamma(y_{ij} + 1/\kappa_i) - \log \Gamma(1/\kappa_i) + y_{ij}(\log(\kappa_i) + \beta_i) - (y_{ij} + 1/\kappa_i) \log(1 + \kappa_i \exp(\beta_i) t_{ij})\}.$$

It follows that

$$\frac{\partial l}{\partial \beta_i} = \sum_{j=1}^{n_i} \left\{ y_{ij} - (y_{ij} + 1/\kappa_i) \frac{\kappa_i \exp(\beta_i) t_{ij}}{1 + \kappa_i \exp(\beta_i) t_{ij}} \right\},$$

and

$$-\frac{\partial^2 l}{\partial \beta_i^2} = \sum_{j=1}^{n_i} (y_{ij} + 1/\kappa_i) \frac{\kappa_i \lambda_i t_{ij}}{(1 + \kappa_i \lambda_i t_{ij})^2}.$$

The Fisher information for β_i is

$$E\left(-\frac{\partial^2 l}{\partial \beta_i^2}\right) = n_i E\left(\frac{\lambda_i t_{ij}}{1 + \kappa_i \lambda_i t_{ij}}\right).$$

In addition, we can show that

$$E\left(-\frac{\partial^2 l}{\partial \beta_i \partial \kappa_i}\right) = 0.$$

Therefore, the variance of $\hat{\beta}_i$ is

$$Var(\hat{\beta}_i) = \frac{1}{n_i}\left\{E\left(\frac{\lambda_i t_{ij}}{1 + \kappa_i \lambda_i t_{ij}}\right)\right\}^{-1}.$$

To evaluate the integral, we need to obtain the distribution of the exposure time,

$$t_{ij} = \min(\tau - W_{ij}, C_{ij}, T_{fmax}),$$

where τ denotes the calendar time since trial start, W_{ij} denotes the enrollment time for subject j in treatment group i, C_{ij} denotes the time to dropout after enrollment for subject j in treatment group i, and T_{fmax} denotes the maximum follow-up time for all subjects. Therefore,

$$P(t_{ij} \geq t) = P(W_{ij} \leq \tau - t)P(C_{ij} \geq t)I(t \leq T_{fmax}).$$

Let H denote the distribution function of the enrollment time, and G_i denote the survival function of the dropout time for treatment group i. By the change of variables, we have

$$E\left(\frac{\lambda_i t_{ij}}{1 + \kappa_i \lambda_i t_{ij}}\right) = \int_0^{\tau \wedge T_{fmax}} \frac{\lambda_i}{(1 + \kappa_i \lambda_i t)^2} H(\tau - t)G_i(t)dt.$$

A numerical integration algorithm for a univariate function can be used to evaluate the above integral.

For the restricted maximum likelihood (reml) estimate of (β_1, β_2) subject to the constraint that $\beta_1 - \beta_2 = \Delta$, we express the log-likelihood in terms of $(\beta_2, \Delta, \kappa_1, \kappa_2)$, and takes the derivative of the log-likelihood function with respect to β_2. The resulting score equation has asymptotic limit

$$E\left(\frac{\partial l}{\partial \beta_2}\right) = s_1 + s_2,$$

where

$$s_1 = nrE\left\{\lambda_1 t_{1j} - \left(\lambda_1 t_{1j} + \frac{1}{\kappa_1}\right)\frac{\kappa_1 e^{\tilde{\beta}_2 + \Delta} t_{1j}}{1 + \kappa_1 e^{\tilde{\beta}_2 + \Delta} t_{1j}}\right\},$$

and

$$s_2 = n(1 - r)E\left\{\lambda_2 t_{2j} - \left(\lambda_2 t_{2j} + \frac{1}{\kappa_2}\right)\frac{\kappa_2 e^{\tilde{\beta}_2} t_{2j}}{1 + \kappa_2 e^{\tilde{\beta}_2} t_{2j}}\right\}.$$

Here r is the randomization probability for the active treatment group. The asymptotic limit of the reml of β_2 is the solution $\tilde{\beta}_2$ to $E\left(\frac{\partial l}{\partial \beta_2}\right) = 0$.

Value

A list with two components:

- resultsUnderH1: A data frame containing the following variables:
    - time: The analysis time since trial start.
    - subjects: The number of enrolled subjects.
    - nevents: The total number of events.
    - nevents1: The number of events in the active treatment group.
    - nevents2: The number of events in the control group.
    - ndropouts: The total number of dropouts.
    - ndropouts1: The number of dropouts in the active treatment group.
    - ndropouts2: The number of dropouts in the control group.
    - nfmax: The total number of subjects reaching maximum follow-up.
    - nfmax1: The number of subjects reaching maximum follow-up in the active treatment group.
    - nfmax2: The number of subjects reaching maximum follow-up in the control group.
    - exposure: The total exposure time.
    - exposure1: The exposure time for the active treatment group.
    - exposure2: The exposure time for the control group.
    - rateRatio: The rate ratio of the active treatment group versus the control group.
    - vlogRate1: The variance for the log rate parameter for the active treatment group.
    - vlogRate2: The variance for the log rate parameter for the control group.
    - vlogRR: The variance of log rate ratio.
    - information: The information of log rate ratio.
    - zlogRR: The Z-statistic for log rate ratio.
- resultsUnderH0 when nullVariance = TRUE: A data frame with the following variables:
    - time: The analysis time since trial start.
    - lambda1H0: The restricted maximum likelihood estimate of the event rate for the active treatment group.
    - lambda2H0: The restricted maximum likelihood estimate of the event rate for the control group.
    - rateRatioH0: The rate ratio under H0.
    - vlogRate1H0: The variance for the log rate parameter for the active treatment group under H0.
    - vlogRate2H0: The variance for the log rate parameter for the control group under H0.
    - vlogRRH0: The variance of log rate ratio under H0.
    - informationH0: The information of log rate ratio under H0.
    - zlogRRH0: The Z-statistic for log rate ratio with variance evaluated under H0.
    - varianceRatio: The ratio of the variance under H0 versus the variance under H1.
    - lambda1: The true event rate for the active treatment group.
    - lambda2: The true event rate for the control group.
    - rateRatio: The true rate ratio.

- resultsUnderH0 when nullVariance = FALSE: A data frame with the following variables:
    - time: The analysis time since trial start.
    - rateRatioH0: The rate ratio under H0.
    - varianceRatio: Equal to 1.
    - lambda1: The true event rate for the active treatment group.
    - lambda2: The true event rate for the control group.
    - rateRatio: The true rate ratio.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: Variable follow-up design

nbstat(time = c(1, 1.25, 2, 3, 4),
       accrualIntensity = 1956/1.25,
       kappa1 = 5,
       kappa2 = 5,
       lambda1 = 0.7*0.125,
       lambda2 = 0.125,
       gamma1 = 0,
       gamma2 = 0,
       accrualDuration = 1.25,
       followupTime = 2.75)

# Example 2: Fixed follow-up design

nbstat(time = c(0.5, 1, 1.5, 2),
       accrualIntensity = 220/1.5,
       stratumFraction = c(0.2, 0.8),
       kappa1 = 3,
       kappa2 = 3,
       lambda1 = c(0.5*8.4, 0.6*10.5),
       lambda2 = c(8.4, 10.5),
       gamma1 = 0,
       gamma2 = 0,
       accrualDuration = 1.5,
       followupTime = 0.5,
       fixedFollowup = 1,
       nullVariance = 1)
```

---

nevent   *Number of Subjects Having an Event*

Description

Obtains the number of subjects having an event by given analysis times for each treatment group.

Usage

```
nevent(
  time = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  minFollowupTime = NA_real_,
  maxFollowupTime = NA_real_
)
```

Arguments

time   A vector of analysis times at which to calculate the number of patients having
                            an event.

allocationRatioPlanned

                            Allocation ratio for the active treatment versus control. Defaults to 1 for equal
                            randomization.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time
                            intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual
                            intervals: [0, 3) and [3, Inf).

accrualIntensity

                            A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

                            A vector that specifies the starting time of piecewise exponential survival time
                            intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event
                            intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

lambda1   A vector of hazard rates for the event for the active treatment group. One for
                            each analysis time interval.

lambda2   A vector of hazard rates for the event for the control group. One for each analysis
                            time interval.

gamma1   The hazard rate for exponential dropout, or a vector of hazard rates for piecewise
                            exponential dropout for the active treatment group.

gamma2   The hazard rate for exponential dropout, or a vector of hazard rates for piecewise
                            exponential dropout for the control group.

accrualDuration

                            Duration of the enrollment period.

minFollowupTime

>   Follow-up time for the last enrolled subject.

maxFollowupTime

>   Follow-up time for the first enrolled subject. For fixed follow-up, maxFollowupTime = minFollowupTime. For variable follow-up, maxFollowupTime = accrualDuration + minFollowupTime.

Value

A matrix of the number of patients having an event at the specified analysis times (row) for each treatment group (column).

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Piecewise accrual, piecewise exponential survivals, and 5% dropout by
# the end of 1 year.

nevent(time = c(9, 24), allocationRatioPlanned = 1,
       accrualTime = c(0, 3), accrualIntensity = c(10, 20),
       piecewiseSurvivalTime = c(0, 6),
       lambda1 = c(0.0533, 0.0309), lambda2 = c(0.0533, 0.0533),
       gamma1 = -log(1-0.05)/12, gamma2 = -log(1-0.05)/12,
       accrualDuration = 12, minFollowupTime = 18,
       maxFollowupTime = 30)
```

---

nevent2 *Number of Subjects Having an Event by Calendar Time*

Description

Obtains the number of subjects having an event by given calendar times for each treatment group.

Usage

```
nevent2(
  time = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
```

```
  gamma2 = 0L,
  accrualDuration = NA_real_,
  minFollowupTime = NA_real_,
  maxFollowupTime = NA_real_
)
```

Arguments

`time`	A vector of calendar times at which to calculate the number of patients having an event.
`allocationRatioPlanned`	
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
`accrualTime`	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).
`accrualIntensity`	
	A vector of accrual intensities. One for each accrual time interval.
`piecewiseSurvivalTime`	
	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.
`lambda1`	A vector of hazard rates for the event for the active treatment group. One for each analysis time interval.
`lambda2`	A vector of hazard rates for the event for the control group. One for each analysis time interval.
`gamma1`	The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the active treatment group.
`gamma2`	The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the control group.
`accrualDuration`	
	Duration of the enrollment period.
`minFollowupTime`	
	Follow-up time for the last enrolled subject.
`maxFollowupTime`	
	Follow-up time for the first enrolled subject. For fixed follow-up, `maxFollowupTime` = `minFollowupTime`. For variable follow-up, `maxFollowupTime` = `accrualDuration` + `minFollowupTime`.

Value

A matrix of the number of patients having an event at the specified calendar times (row) for each treatment group (column).

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Piecewise accrual, piecewise exponential survivals, and 5% dropout by
# the end of 1 year.
nevent2(time = c(9, 24), allocationRatioPlanned = 1,
        accrualTime = c(0, 3), accrualIntensity = c(10, 20),
        piecewiseSurvivalTime = c(0, 6),
        lambda1 = c(0.0533, 0.0309), lambda2 = c(0.0533, 0.0533),
        gamma1 = -log(1-0.05)/12, gamma2 = -log(1-0.05)/12,
        accrualDuration = 12, minFollowupTime = 18,
        maxFollowupTime = 30)
```

---

patrisk   *Probability of Being at Risk*

Description

Obtains the probability of being at risk at given analysis times.

Usage

```
patrisk(
  time = NA_real_,
  piecewiseSurvivalTime = 0L,
  lambda = NA_real_,
  gamma = 0L
)
```

Arguments

time   A vector of analysis times at which to calculate the probability of being at risk.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

lambda   A vector of hazard rates for the event. One for each analysis time interval.

gamma   The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout.

Value

A vector of probabilities of being at risk at the specified analysis times after enrollment for a patient in a treatment group with specified piecewise exponential survival and dropout distributions.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Piecewise exponential survival with hazard 0.0533 in the first 6
# months, and hazard 0.0309 thereafter, and 5% dropout by the end of
# 1 year.

patrisk(time = c(3, 9), piecewiseSurvivalTime = c(0, 6),
        lambda = c(0.0533, 0.0309), gamma = -log(1-0.05)/12)
```

---

pevent | *Probability of Having an Event*

Description

Obtains the probability of having an event at given analysis times.

Usage

```
pevent(
  time = NA_real_,
  piecewiseSurvivalTime = 0L,
  lambda = NA_real_,
  gamma = 0L
)
```

Arguments

time   A vector of analysis times at which to calculate the probability of having an event.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

lambda   A vector of hazard rates for the event. One for each analysis time interval.

gamma   The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout.

Value

A vector of probabilities of having an event at the specified analysis times after enrollment for a patient in a treatment group with specified piecewise exponential survival and dropout distributions.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Piecewise exponential survival with hazard 0.0533 in the first 6
# months, and hazard 0.0309 thereafter, and 5% dropout by the end of
# 1 year.

pevent(time = c(3, 9), piecewiseSurvivalTime = c(0, 6),
       lambda = c(0.0533, 0.0309), gamma = -log(1-0.05)/12)
```

---

phregr	*Proportional Hazards Regression Models*

Description

Obtains the hazard ratio estimates from the proportional hazards regression model with right censored or counting process data.

Usage

```
phregr(
  data,
  rep = "",
  stratum = "",
  time = "time",
  time2 = "",
  event = "event",
  covariates = "",
  weight = "",
  offset = "",
  id = "",
  ties = "efron",
  robust = FALSE,
  est_basehaz = TRUE,
  est_resid = TRUE,
  firth = FALSE,
  plci = FALSE,
  alpha = 0.05
)
```

Arguments

data   The input data frame that contains the following variables:

- rep: The replication for by-group processing.
- stratum: The stratum.
- time: The follow-up time for right censored data, or the left end of each interval for counting process data.

- time2: The right end of each interval for counting process data. Intervals are assumed to be open on the left and closed on the right, and event indicates whether an event occurred at the right end of each interval.
- event: The event indicator, 1=event, 0=no event.
- covariates: The values of baseline covariates (and time-dependent covariates in each interval for counting process data).
- weight: The weight for each observation.
- offset: The offset for each observation.
- id: The optional subject ID for counting process data with time-dependent covariates.

rep	The name(s) of the replication variable(s) in the input data.
stratum	The name(s) of the stratum variable(s) in the input data.
time	The name of the time variable or the left end of each interval for counting process data in the input data.
time2	The name of the right end of each interval for counting process data in the input data.
event	The name of the event variable in the input data.
covariates	The vector of names of baseline and time-dependent covariates in the input data.
weight	The name of the weight variable in the input data.
offset	The name of the offset variable in the input data.
id	The name of the id variable in the input data.
ties	The method for handling ties, either "breslow" or "efron" (default).
robust	Whether a robust sandwich variance estimate should be computed. In the presence of the id variable, the score residuals will be aggregated for each id when computing the robust sandwich variance estimate.
est_basehaz	Whether to estimate the baseline hazards. Defaults to TRUE.
est_resid	Whether to estimate the martingale residuals. Defaults to TRUE.
firth	Whether to use Firth's penalized likelihood method. Defaults to FALSE.
plci	Whether to obtain profile likelihood confidence interval.
alpha	The two-sided significance level.

Value

A list with the following components:

- sumstat: The data frame of summary statistics of model fit with the following variables:
  - n: The number of observations.
  - nevents: The number of events.
  - loglik0: The (penalized) log-likelihood under null.
  - loglik1: The maximum (penalized) log-likelihood.
  - scoretest: The score test statistic.
  - niter: The number of Newton-Raphson iterations.

- – `ties`: The method for handling ties, either "breslow" or "efron".
- – `p`: The number of columns of the Cox model design matrix.
- – `robust`: Whether to use the robust variance estimate.
- – `firth`: Whether to use Firth's penalized likelihood method.
- – `loglik0_unpenalized`: The unpenalized log-likelihood under null.
- – `loglik1_unpenalized`: The maximum unpenalized log-likelihood.
- – `rep`: The replication.

- `parest`: The data frame of parameter estimates with the following variables:

  - – `param`: The name of the covariate for the parameter estimate.
  - – `beta`: The log hazard ratio estimate.
  - – `sebeta`: The standard error of log hazard ratio estimate.
  - – `z`: The Wald test statistic for log hazard ratio.
  - – `expbeta`: The hazard ratio estimate.
  - – `vbeta`: The covariance matrix for parameter estimates.
  - – `lower`: The lower limit of confidence interval.
  - – `upper`: The upper limit of confidence interval.
  - – `p`: The p-value from the chi-square test.
  - – `method`: The method to compute the confidence interval and p-value.
  - – `sebeta_naive`: The naive standard error of log hazard ratio estimate if robust variance is requested.
  - – `vbeta_naive`: The naive covariance matrix for parameter estimates if robust variance is requested.
  - – `rep`: The replication.

- `basehaz`: The data frame of baseline hazards with the following variables (if est_basehaz is TRUE):

  - – `time`: The observed event time.
  - – `nrisk`: The number of patients at risk at the time point.
  - – `nevent`: The number of events at the time point.
  - – `haz`: The baseline hazard at the time point.
  - – `varhaz`: The variance of the baseline hazard at the time point assuming the parameter beta is known.
  - – `gradhaz`: The gradient of the baseline hazard with respect to beta at the time point (in the presence of covariates).
  - – `stratum`: The stratum.
  - – `rep`: The replication.

- `residuals`: The martingale residuals.
- `p`: The number of parameters.
- `param`: The parameter names.
- `beta`: The parameter estimate.
- `vbeta`: The covariance matrix for parameter estimates.
- `vbeta_naive`: The naive covariance matrix for parameter estimates.

- `terms`: The terms object.
- `xlevels`: A record of the levels of the factors used in fitting.
- `data`: The input data.
- `rep`: The name(s) of the replication variable(s).
- `stratum`: The name(s) of the stratum variable(s).
- `time`: The name of the time varaible.
- `time2`: The name of the time2 variable.
- `event`: The name of the event variable.
- `covariates`: The names of baseline covariates.
- `weight`: The name of the weight variable.
- `offset`: The name of the offset variable.
- `id`: The name of the id variable.
- `ties`: The method for handling ties.
- `robust`: Whether a robust sandwich variance estimate should be computed.
- `est_basehaz`: Whether to estimate the baseline hazards.
- `est_resid`: Whether to estimate the martingale residuals.
- `firth`: Whether to use Firth's penalized likelihood method.
- `plci`: Whether to obtain profile likelihood confidence interval.
- `alpha`: The two-sided significance level.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Per K. Anderson and Richard D. Gill. Cox's regression model for counting processes, a large sample study. Annals of Statistics 1982; 10:1100-1120.

Terry M. Therneau and Patricia M. Grambsch. Modeling Survival Data: Extending the Cox Model. Springer-Verlag, 2000.

Examples

```
library(dplyr)

# Example 1 with right-censored data
(fit1 <- phregr(
  data = rawdata %>% mutate(treat = 1*(treatmentGroup == 1)),
  rep = "iterationNumber", stratum = "stratum",
  time = "timeUnderObservation", event = "event",
  covariates = "treat", est_basehaz = FALSE, est_resid = FALSE))

# Example 2 with counting process data and robust variance estimate
(fit2 <- phregr(
```

```
data = heart %>% mutate(rx = as.numeric(transplant) - 1),
time = "start", time2 = "stop", event = "event",
covariates = c("rx", "age"), id = "id",
robust = TRUE, est_basehaz = TRUE, est_resid = TRUE))
```

---

ptpwexp	*Distribution Function of Truncated Piecewise Exponential Distribution*

Description

Obtains the probability of a truncated piecewise exponential distribution.

Usage

```
ptpwexp(
  q,
  piecewiseSurvivalTime = 0,
  lambda = 0.0578,
  lowerBound = 0,
  lower.tail = TRUE,
  log.p = FALSE
)
```

Arguments

q   The vector of quantiles.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

lambda   A vector of hazard rates for the event. One for each analysis time interval.

lowerBound   The left truncation time point for the survival time. Defaults to 0 for no truncation.

lower.tail   Logical; if TRUE (default), probabilities are P(X <= x), otherwise, P(X > x).

log.p   Logical; if TRUE, probabilities p are given as log(p).

Value

The probability p such that P(X > q | X > lowerBound) = 1 - p.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
ptpwexp(q = c(8, 18), piecewiseSurvivalTime = c(0, 6, 9, 15),
        lambda = c(0.025, 0.04, 0.015, 0.007))
```

---

pwexpcuts   *Piecewise Exponential Approximation to a Survival Distribution*

Description

Obtains the piecewise exponential distribution that approximates a survival distribution.

Usage

```
pwexpcuts(S, ...)
```

Arguments

S   The survival function of a univariate survival time.

...   Additional arguments to be passed to S.

Value

A list with three components:

- piecewiseSurvivalTime: A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf).

- lambda: A vector of hazard rates for the event. One for each analysis time interval.

- loglik: The sequence of the asymptotic limit of the piecewise exponential log-likelihood for an increasing number of change points.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: Piecewise exponential
pwexpcuts(ptpwexp, piecewiseSurvivalTime = c(0, 3.4, 5.5),
          lambda = c(0.0168, 0.0833, 0.0431), lowerBound = 0,
          lower.tail = FALSE)

# Example 2: Weibull
pwexpcuts(pweibull, shape = 1.37, scale = 1/0.818, lower.tail = FALSE)
```

pwexploglik	*Profile Log-Likelihood Function for the Change Points in Piecewise Exponential Approximation*

Description

Obtains the profile log-likelihood function for the change points in the piecewise exponential approximation to a survival function.

Usage

```
pwexploglik(tau, S, ...)
```

Arguments

tau	The numeric vector of change points.
S	The survival function of a univariate survival time.
...	Additional arguments to be passed to S.

Value

A list with the following three components:

- piecewiseSurvivalTime: A vector that specifies the starting time of piecewise exponential survival time intervals.
- lambda: A vector of hazard rates for the event. One for each analysis time interval.
- loglik: The value of the profile log-likelihood.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
pwexploglik(tau = c(0.5, 1.2, 2.8), pweibull,
            shape = 1.37, scale = 1/0.818, lower.tail = FALSE)
```

---

qrcpp   *QR Decomposition of a Matrix*

Description

Computes the QR decomposition of a matrix.

Usage

```
qrcpp(X, tol = 1e-12)
```

Arguments

X	A numeric matrix whose QR decomposition is to be computed.
tol	The tolerance for detecting linear dependencies in the columns of X.

Details

This function performs Householder QR with column pivoting: Given an m-by-n matrix A with $m \geq n$, the following algorithm computes $r = \text{rank}(A)$ and the factorization $Q^T A P$ equal to

$$\begin{array}{ccc} | & R_{11} & R_{12} & | & r \\ | & 0 & 0 & | & m-r \\ & r & n-r & \end{array}$$

with $Q = H_1 \cdots H_r$ and $P = P_1 \cdots P_r$. The upper triangular part of A is overwritten by the upper triangular part of R and components $(j+1) : m$ of the jth Householder vector are stored in $A((j+1) : m, j)$. The permutation P is encoded in an integer vector `pivot`.

Value

A list with the following components:

- `qr`: A matrix with the same dimensions as X. The upper triangle contains the R of the decomposition and the lower triangle contains Householder vectors (stored in compact form).
- `rank`: The rank of X as computed by the decomposition.
- `pivot`: The column permutation for the pivoting strategy used during the decomposition.
- `Q`: The complete m-by-m orthogonal matrix Q.
- `R`: The complete m-by-n upper triangular matrix R.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Gene N. Golub and Charles F. Van Loan. Matrix Computations, second edition. Baltimore, Maryland: The John Hopkins University Press, 1989, p.235.

Examples

```
hilbert <- function(n) { i <- 1:n; 1 / outer(i - 1, i, `+`) }
h9 <- hilbert(9)
qrcpp(h9)
```

---

qtpwexp   *Quantile Function of Truncated Piecewise Exponential Distribution*

Description

Obtains the quantile of a truncated piecewise exponential distribution.

Usage

```
qtpwexp(
  p,
  piecewiseSurvivalTime = 0,
  lambda = 0.0578,
  lowerBound = 0,
  lower.tail = TRUE,
  log.p = FALSE
)
```

Arguments

p	The vector of probabilities.
piecewiseSurvivalTime	
	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.
lambda	A vector of hazard rates for the event. One for each analysis time interval.
lowerBound	The left truncation time point for the survival time. Defaults to 0 for no truncation.
lower.tail	Logical; if TRUE (default), probabilities are P(X <= x), otherwise, P(X > x).
log.p	Logical; if TRUE, probabilities p are given as log(p).

Value

The quantile q such that P(X > q | X > lowerBound) = 1 - p.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
qtpwexp(p = c(0.205, 0.317), piecewiseSurvivalTime = c(0, 6, 9, 15),
        lambda = c(0.025, 0.04, 0.015, 0.007))
```

---

rawdata   *A simulated time-to-event data set with 10 replications*

Description

A simulated data set with stratification and delayed treatment effect:

iterationNumber The iteration number

arrivalTime The enrollment time for the subject

stratum The stratum for the subject

treatmentGroup The treatment group for the subject

timeUnderObservation The time under observation since randomization

event Whether the subject experienced the event

dropoutEvent Whether the subject dropped out

Usage

```
rawdata
```

Format

An object of class data.frame with 4910 rows and 7 columns.

---

remlOddsRatio   *REML Estimates of Individual Proportions With Specified Odds Ratio*

Description

Obtains the restricted maximum likelihood estimates of individual proportions with specified odds ratio.

Usage

```
remlOddsRatio(
  oddsRatioH0 = 1,
  n1 = NA_real_,
  y1 = NA_real_,
  n2 = NA_real_,
  y2 = NA_real_
)
```

Arguments

oddsRatioH0	The specified odds ratio.
n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.

Value

A vector of the restricted maximum likelihood estimates of the response probabilities for the two treatment groups.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
remlOddsRatio(oddsRatioH0 = 1.25, n1 = 10, y1 = 4, n2 = 20, y2 = 2)
```

---

remlRateDiff	*REML Estimates of Individual Rates With Specified Rate Difference*

Description

Obtains the restricted maximum likelihood estimates of individual proportions with specified rate difference.

Usage

```
remlRateDiff(
  rateDiffH0 = 0,
  t1 = NA_real_,
  y1 = NA_real_,
  t2 = NA_real_,
  y2 = NA_real_
)
```

Arguments

rateDiffH0	The specified rate difference.
t1	The exposure for the active treatment group.
y1	The number of events for the active treatment group.
t2	The exposure for the control group.
y2	The number of events for the control group.

Value

A vector of the restricted maximum likelihood estimates of the incidence rates for the two treatment groups.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
remlRateDiff(rateDiffH0 = 0.1, t1 = 10, y1 = 4, t2 = 20, y2 = 2)
```

---

remlRateRatio   *REML Estimates of Individual Rates With Specified Rate Ratio*

Description

Obtains the restricted maximum likelihood estimates of individual proportions with specified rate ratio.

Usage

```
remlRateRatio(
  rateRatioH0 = 1,
  t1 = NA_real_,
  y1 = NA_real_,
  t2 = NA_real_,
  y2 = NA_real_
)
```

Arguments

rateRatioH0	The specified rate ratio.
t1	The exposure for the active treatment group.
y1	The number of events for the active treatment group.
t2	The exposure for the control group.
y2	The number of events for the control group.

Value

A vector of the restricted maximum likelihood estimates of the incidence rates for the two treatment groups.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
remlRateRatio(rateRatioH0 = 1.1, t1 = 10, y1 = 4, t2 = 20, y2 = 2)
```

---

remlRiskDiff	*REML Estimates of Individual Proportions With Specified Risk differ-ence*

Description

Obtains the restricted maximum likelihood estimates of individual proportions with specified risk difference.

Usage

```
remlRiskDiff(
  riskDiffH0 = 0,
  n1 = NA_real_,
  y1 = NA_real_,
  n2 = NA_real_,
  y2 = NA_real_
)
```

Arguments

riskDiffH0	The specified risk difference.
n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.

Value

A vector of the restricted maximum likelihood estimates of the response probabilities for the two treatment groups.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
remlRiskDiff(riskDiffH0 = 0.1, n1 = 10, y1 = 4, n2 = 20, y2 = 0)
```

---

remlRiskRatio   *REML Estimates of Individual Proportions With Specified Risk Ratio*

Description

Obtains the restricted maximum likelihood estimates of individual proportions with specified risk ratio.

Usage

```
remlRiskRatio(
  riskRatioH0 = 1,
  n1 = NA_real_,
  y1 = NA_real_,
  n2 = NA_real_,
  y2 = NA_real_
)
```

Arguments

riskRatioH0	The specified risk ratio.
n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.

Value

A vector of the restricted maximum likelihood estimates of the response probabilities for the two treatment groups.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
remlRiskRatio(riskRatioH0 = 1.2, n1 = 10, y1 = 4, n2 = 20, y2 = 2)
```

---

repeatedPValue   *Repeated p-Values for Group Sequential Design*

Description

Obtains the repeated p-values for a group sequential design.

Usage

```
repeatedPValue(
  kMax,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA,
  maxInformation = 1,
  p,
  information,
  spendingTime = NULL
)
```

Arguments

kMax   The maximum number of stages.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

maxInformation   The target maximum information. Defaults to 1, in which case, information represents informationRates.

p   The raw p-values at look 1 to look k. It can be a matrix with k columns for k <= kMax.

information   The observed information by look. It can be a matrix with k columns.

spendingTime   The error spending time at each analysis, must be increasing and less than or equal to 1. Defaults to NULL, in which case, it is the same as informationRates derived from information and maxInformation. It can be a matrix with k columns.

Value

The repeated p-values at look 1 to look k.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Example 1: informationRates different from spendingTime
repeatedPValue(kMax = 3, typeAlphaSpending = "sfOF",
               maxInformation = 800,
               p = c(0.2, 0.15, 0.1),
               information = c(529, 700, 800),
               spendingTime = c(0.6271186, 0.8305085, 1))

# Example 2: Maurer & Bretz (2013), current look is not the last look
repeatedPValue(kMax = 3, typeAlphaSpending = "sfOF",
               p = matrix(c(0.0062, 0.017,
                            0.009, 0.13,
                            0.0002, 0.0035,
                            0.002, 0.06),
                          nrow=4, ncol=2),
               information = c(1/3, 2/3))
```

---

residuals_phregr   *Residuals for Proportional Hazards Regression Models*

Description

Obtains the martingale, deviance, score, or Schoenfeld residuals for a proportional hazards regression model.

Usage

```
residuals_phregr(
  fit_phregr,
  type = c("martingale", "deviance", "score", "schoenfeld", "dfbeta", "dfbetas",
    "scaledsch"),
  collapse = FALSE,
  weighted = (type %in% c("dfbeta", "dfbetas"))
)
```

Arguments

fit_phregr	The output from the phregr call.
type	The type of residuals desired, with options including "martingale", "deviance", "score", "schoenfeld", "dfbeta", "dfbetas", and "scaledsch".
collapse	Whether to collapse the residuals by id. This is not applicable for Schoenfeld type residuals.
weighted	Whether to compute weighted residuals.

Details

For score and Schoenfeld type residuals, the proportional hazards model must include at least one covariate. The algorithms for `deviance`, `dfbeta`, `dfbetas`, and `scaledsch` residuals follow the `residuals.coxph` function in the `survival` package.

Value

For martingale and deviance residuals, the result is a vector with one element corresponding to each subject (without `collapse`). For score residuals, the result is a matrix where each row represents a subject and each column corresponds to a variable. The row order aligns with the input data used in the original fit. For Schoenfeld residuals, the result is a matrix with one row for each event and one column per variable. These rows are sorted by time within strata, with the attributes `stratum` and `time` included.

Score residuals represent each individual's contribution to the score vector. Two commonly used transformations of this are `dfbeta`, which represents the approximate change in the coefficient vector if the observation is excluded, and `dfbetas`, which gives the approximate change in the coefficients scaled by the standard error of the coefficients.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Terry M. Therneau, Patricia M. Grambsch, and Thomas M. Fleming. Martingale based residuals for survival models. Biometrika 1990; 77:147-160.

Patricia M. Grambsch and Terry M. Therneau. Proportional hazards tests and diagnostics based on weighted residuals. Biometrika 1994; 81:515-26.

Examples

```
library(dplyr)

# Example 1 with right-censored data
fit1 <- phregr(data = rawdata %>% filter(iterationNumber == 1) %>%
                 mutate(treat = 1*(treatmentGroup == 1)),
               stratum = "stratum",
               time = "timeUnderObservation", event = "event",
               covariates = "treat")

ressco <- residuals_phregr(fit1, type = "score")

# Example 2 with counting process data
fit2 <- phregr(data = heart %>% mutate(rx = as.numeric(transplant) - 1),
               time = "start", time2 = "stop", event = "event",
               covariates = c("rx", "age"), id = "id", robust = TRUE)

resssch <- residuals_phregr(fit2, type = "scaledsch")
```

---

riskDiffExactCI   *Exact Unconditional Confidence Interval for Risk Difference*

Description

Obtains the exact unconditional confidence interval for risk difference based on the standardized score statistic.

Usage

```
riskDiffExactCI(
  n1 = NA_integer_,
  y1 = NA_integer_,
  n2 = NA_integer_,
  y2 = NA_integer_,
  cilevel = 0.95
)
```

Arguments

n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.
cilevel	The confidence interval level.

Value

A data frame containing the following variables:

- scale: The scale of treatment effect.
- estimate: The point estimate.
- lower: The lower limit of the confidence interval.
- upper: The upper limit of the confidence interval.
- cilevel: The confidence interval level.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
riskDiffExactCI(n1 = 30, y1 = 2, n2 = 30, y2 = 1, cilevel = 0.95)
```

---

riskDiffExactPValue   *P-Value for Exact Unconditional Test of Risk Difference*

Description

Obtains the p-value for exact unconditional test of risk difference.

Usage

```
riskDiffExactPValue(
  riskDiffH0 = 0,
  directionUpper = 1L,
  n1 = NA_integer_,
  y1 = NA_integer_,
  n2 = NA_integer_,
  y2 = NA_integer_
)
```

Arguments

riskDiffH0	The risk difference under the null hypothesis. Defaults to 0.
directionUpper	Whether larger values represent better responses.
n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.

Value

A data frame containing the following variables:

- riskDiffH0: The risk difference under the null hypothesis.
- directionUpper: Whether larger values represent better responses.
- riskDiff: The observed risk difference.
- zstat: The observed value of the Z test statistic.
- pvalue: The one-sided p-value for the unconditional exact test.
- pi2star: The value of pi2 that yields the p-value.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
riskDiffExactPValue(riskDiffH0 = 0, directionUpper = 1,
                    n1 = 68, y1 = 2, n2 = 65, y2 = 1)
```

---

riskRatioExactCI   *Exact Unconditional Confidence Interval for Risk Ratio*

Description

Obtains the exact unconditional confidence interval for risk ratio based on the standardized score statistic.

Usage

```
riskRatioExactCI(
  n1 = NA_integer_,
  y1 = NA_integer_,
  n2 = NA_integer_,
  y2 = NA_integer_,
  cilevel = 0.95
)
```

Arguments

n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.
cilevel	The confidence interval level.

Value

A data frame containing the following variables:

- scale: The scale of treatment effect.
- estimate: The point estimate.
- lower: The lower limit of the confidence interval.
- upper: The upper limit of the confidence interval.
- cilevel: The confidence interval level.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
riskRatioExactCI(n1 = 30, y1 = 2, n2 = 30, y2 = 1, cilevel = 0.95)
```

riskRatioExactPValue   *P-Value for Exact Unconditional Test of Risk Ratio*

Description

Obtains the p-value for exact unconditional test of risk ratio.

Usage

```
riskRatioExactPValue(
  riskRatioH0 = 1,
  directionUpper = 1L,
  n1 = NA_integer_,
  y1 = NA_integer_,
  n2 = NA_integer_,
  y2 = NA_integer_
)
```

Arguments

riskRatioH0	The risk ratio under the null hypothesis. Defaults to 1.
directionUpper	Whether larger values represent better responses.
n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.

Value

A data frame containing the following variables:

- riskRatioH0: The risk ratio under the null hypothesis.
- directionUpper: Whether larger values represent better responses.
- riskRatio: The observed risk ratio.
- zstat: The observed value of the Z test statistic.
- pvalue: The one-sided p-value for the unconditional exact test.
- pi2star: The value of pi2 that yields the p-value.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
riskRatioExactPValue(riskRatioH0 = 1, directionUpper = 1,
                     n1 = 68, y1 = 2, n2 = 65, y2 = 1)
```

Estimate of Restricted Mean Survival Time Difference

Description

Obtains the estimate of restricted mean survival time difference between two treatment groups.

Usage

```
rmdiff(
  data,
  rep = "",
  stratum = "",
  treat = "treat",
  time = "time",
  event = "event",
  milestone = NA_real_,
  rmstDiffH0 = 0,
  conflev = 0.95,
  biascorrection = 0L
)
```

Arguments

data	The input data frame that contains the following variables:

- rep: The replication for by-group processing.
- stratum: The stratum.
- treat: The treatment.
- time: The possibly right-censored survival time.
- event: The event indicator.

rep	The name of the replication variable in the input data.
stratum	The name of the stratum variable in the input data.
treat	The name of the treatment variable in the input data.
time	The name of the time variable in the input data.
event	The name of the event variable in the input data.
milestone	The milestone time at which to calculate the restricted mean survival time.
rmstDiffH0	The difference in restricted mean survival times under the null hypothesis. Defaults to 0 for superiority test.
conflev	The level of the two-sided confidence interval for the difference in restricted mean survival times. Defaults to 0.95.
biascorrection	Whether to apply bias correction for the variance estimate of individual restricted mean survival times. Defaults to no bias correction.

Value

A data frame with the following variables:

- rep: The replication number.
- milestone: The milestone time relative to randomization.
- rmstDiffH0: The difference in restricted mean survival times under the null hypothesis.
- rmst1: The estimated restricted mean survival time for the treatment group.
- rmst2: The estimated restricted mean survival time for the control group.
- rmstDiff: The estimated difference in restricted mean survival times.
- vrmst1: The variance for rmst1.
- vrmst2: The variance for rmst2.
- vrmstDiff: The variance for rmstDiff.
- rmstDiffZ: The Z-statistic value.
- rmstDiffPValue: The one-sided p-value.
- lower: The lower bound of confidence interval.
- upper: The upper bound of confidence interval.
- conflev: The level of confidence interval.
- biascorrection: Whether to apply bias correction for the variance estimate of individual restricted mean survival times.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
df <- rmdiff(data = rawdata, rep = "iterationNumber",
             stratum = "stratum", treat = "treatmentGroup",
             time = "timeUnderObservation", event = "event",
             milestone = 12)
head(df)
```

---

rmest   *Estimate of Restricted Mean Survival Time*

Description

Obtains the estimate of restricted means survival time for each stratum.

Usage

```
rmest(
  data,
  rep = "",
  stratum = "",
  time = "time",
  event = "event",
  milestone = NA_real_,
  conflev = 0.95,
  biascorrection = 0L
)
```

Arguments

data	The input data frame that contains the following variables:

- rep: The replication for by-group processing.
- stratum: The stratum.
- time: The possibly right-censored survival time.
- event: The event indicator.

rep	The name of the replication variable in the input data.
stratum	The name of the stratum variable in the input data.
time	The name of the time variable in the input data.
event	The name of the event variable in the input data.
milestone	The milestone time at which to calculate the restricted mean survival time.
conflev	The level of the two-sided confidence interval for the survival probabilities. Defaults to 0.95.
biascorrection	Whether to apply bias correction for the variance estimate. Defaults to no bias correction.

Value

A data frame with the following variables:

- rep: The replication.
- stratum: The stratum variable.
- size: The number of subjects in the stratum.
- milestone: The milestone time relative to randomization.
- rmst: The estimate of restricted mean survival time.
- stderr: The standard error of the estimated rmst.
- lower: The lower bound of confidence interval if requested.
- upper: The upper bound of confidence interval if requested.
- conflev: The level of confidence interval if requested.
- biascorrection: Whether to apply bias correction for the variance estimate.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
rmest(data = aml, stratum = "x",
      time = "time", event = "status", milestone = 24)
```

---

rmpower   *Power for Difference in Restricted Mean Survival Times*

Description

Estimates the power for testing the difference in restricted mean survival times in a two-sample survival design.

Usage

```
rmpower(
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  milestone = NA_real_,
  rmstDiffH0 = 0,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  spendingTime = NA_real_,
```

```
  studyDuration = NA_real_
)
```

Arguments

kMax   The maximum number of stages.

informationRates
                  The information rates. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping
                  Indicators of whether efficacy stopping is allowed at each stage. Defaults to true
                  if left unspecified.

futilityStopping
                  Indicators of whether futility stopping is allowed at each stage. Defaults to true
                  if left unspecified.

criticalValues   Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha   The significance level. Defaults to 0.025.

typeAlphaSpending
                  The type of alpha spending. One of the following: "OF" for O'Brien-Fleming
                  boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries,
                  "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spend-
                  ing function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang,
                  Shi & DeCani spending function, "user" for user defined spending, and "none"
                  for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending
                  The parameter value for the alpha spending. Corresponds to Delta for "WT",
                  rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending
                  The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds   Lower boundaries on the z-test statistic scale for stopping for futility at stages 1,
                  ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds
                  are non-binding for the calculation of critical values.

typeBetaSpending
                  The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming
                  type spending function, "sfP" for Pocock type spending function, "sfKD" for
                  Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending
                  function, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending
                  The parameter value for the beta spending. Corresponds to rho for "sfKD", and
                  gamma for "sfHSD".

milestone   The milestone time at which to calculate the restricted mean survival time.

rmstDiffH0   The difference in restricted mean survival times under the null hypothesis. De-
                  faults to 0 for superiority test.

allocationRatioPlanned
                  Allocation ratio for the active treatment versus control. Defaults to 1 for equal
                  randomization.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

                     A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

                     A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

                     A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1   A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.

lambda2   A vector of hazard rates for the event in each analysis time interval by stratum for the control group.

gamma1   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.

gamma2   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration

                     Duration of the enrollment period.

followupTime   Follow-up time for the last enrolled subject.

fixedFollowup   Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as `informationRates`.

studyDuration   Study duration for fixed follow-up design. Defaults to missing, which is to be replaced with the sum of `accrualDuration` and `followupTime`. If provided, the value is allowed to be less than the sum of `accrualDuration` and `followupTime`.

Value

An S3 class rmpower object with 4 components:

- overallResults: A data frame containing the following variables:
    - overallReject: The overall rejection probability.
    - alpha: The overall significance level.
    - numberOfEvents: The total number of events.
    - numbeOfSubjects: The total number of subjects.
    - studyDuration: The total study duration.
    - information: The maximum information.
    - expectedNumberOfEvents: The expected number of events.

- – expectedNumberOfSubjects: The expected number of subjects.
- – expectedStudyDuration: The expected study duration.
- – expectedInformation: The expected information.
- – accrualDuration: The accrual duration.
- – followupTime: The follow-up duration.
- – fixedFollowup: Whether a fixed follow-up design is used.
- – kMax: The number of stages.
- – milestone: The milestone time relative to randomization.
- – rmstDiffH0: The difference in restricted mean survival times under the null hypothesis.
- – rmst1: The restricted mean survival time for the treatment group.
- – rmst2: The restricted mean survival time for the control group.
- – rmstDiff: The difference in restricted mean survival times, equal to rmst1 – rmst2.

- byStageResults: A data frame containing the following variables:
  - – informationRates: The information rates.
  - – efficacyBounds: The efficacy boundaries on the Z-scale.
  - – futilityBounds: The futility boundaries on the Z-scale.
  - – rejectPerStage: The probability for efficacy stopping.
  - – futilityPerStage: The probability for futility stopping.
  - – cumulativeRejection: The cumulative probability for efficacy stopping.
  - – cumulativeFutility: The cumulative probability for futility stopping.
  - – cumulativeAlphaSpent: The cumulative alpha spent.
  - – numberOfEvents: The number of events.
  - – numberOfDropouts: The number of dropouts.
  - – numberOfSubjects: The number of subjects.
  - – numberOfMilestone: The number of subjects reaching milestone.
  - – analysisTime: The average time since trial start.
  - – efficacyRmstDiff: The efficacy boundaries on the restricted mean survival time difference scale.
  - – futilityRmstDiff: The futility boundaries on the restricted mean survival time difference scale.
  - – efficacyP: The efficacy boundaries on the p-value scale.
  - – futilityP: The futility boundaries on the p-value scale.
  - – information: The cumulative information.
  - – efficacyStopping: Whether to allow efficacy stopping.
  - – futilityStopping: Whether to allow futility stopping.

- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, typeBetaSpending, parameterBetaSpending, allocationRatioPlanned, accrualTime, accuralIntensity, piecewiseSurvivalTime, stratumFraction, lambda1, lambda2, gamma1, gamma2, and spendingTime.

- byTreatmentCounts: A list containing the following counts by treatment group:
  - – numberOfEvents1: The number of events by stage for the treatment group.
  - – numberOfDropouts1: The number of dropouts by stage for the treatment group.

- – numberOfSubjects1: The number of subjects by stage for the treatment group.
- – numberOfMilestone1: The number of subjects reaching milestone by stage for the active treatment group.
- – numberOfEvents2: The number of events by stage for the control group.
- – numberOfDropouts2: The number of dropouts by stage for the control group.
- – numberOfSubjects2: The number of subjects by stage for the control group.
- – numberOfMilestone2: The number of subjects reaching milestone by stage for the control group.
- – expectedNumberOfEvents1: The expected number of events for the treatment group.
- – expectedNumberOfDropouts1: The expected number of dropouts for the active treatment group.
- – expectedNumberOfSubjects1: The expected number of subjects for the active treatment group.
- – expectedNumberOfMilestone1: The expected number of subjects reaching milestone for the active treatment group.
- – expectedNumberOfEvents2: The expected number of events for control group.
- – expectedNumberOfDropouts2: The expected number of dropouts for the control group.
- – expectedNumberOfSubjects2: The expected number of subjects for the control group.
- – expectedNumberOfMilestone2: The expected number of subjects reaching milestone for the control group.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Piecewise accrual, piecewise exponential survival, and 5% dropout by
# the end of 1 year.

rmpower(kMax = 2, informationRates = c(0.8, 1),
        alpha = 0.025, typeAlphaSpending = "sfOF",
        milestone = 18,
        allocationRatioPlanned = 1, accrualTime = seq(0, 8),
        accrualIntensity = 100/9*seq(1, 9),
        piecewiseSurvivalTime = c(0, 6),
        stratumFraction = c(0.2, 0.8),
        lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
        lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
        gamma1 = -log(1-0.05)/12,
        gamma2 = -log(1-0.05)/12, accrualDuration = 22,
        followupTime = 18, fixedFollowup = FALSE)
```

---

rmpower1s   *Power for One-Sample Restricted Mean Survival Time*

Description

Estimates the power, stopping probabilities, and expected sample size in a one-group survival design.

Usage

```
rmpower1s(
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  milestone = NA_real_,
  rmstH0 = NA_real_,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda = NA_real_,
  gamma = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  spendingTime = NA_real_,
  studyDuration = NA_real_
)
```

Arguments

kMax   The maximum number of stages.

informationRates

        The information rates. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

        Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

    Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues   Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha   The significance level. Defaults to 0.025.

typeAlphaSpending

    The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

    The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

    The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds   Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

    The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

    The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

milestone   The milestone time at which to calculate the restricted mean survival time.

rmstH0   The restricted mean survival time under the null hypothesis.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

    A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

    A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

    A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda   A vector of hazard rates for the event in each analysis time interval by stratum under the alternative hypothesis.

gamma   The hazard rate for exponential dropout or a vector of hazard rates for piecewise exponential dropout. Defaults to 0 for no dropout.

accrualDuration
               Duration of the enrollment period.

followupTime   Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

studyDuration Study duration for fixed follow-up design. Defaults to missing, which is to be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and followupTime.

Value

An S3 class rmpower1s object with 3 components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - numberOfEvents: The total number of events.
  - numbeOfSubjects: The total number of subjects.
  - numberOfMilestone: The total number of subjects reaching milestone.
  - studyDuration: The total study duration.
  - information: The maximum information.
  - expectedNumberOfEvents: The expected number of events.
  - expectedNumberOfSubjects: The expected number of subjects.
  - expectedNumberOfMilestone: The expected number of subjects reaching milestone.
  - expectedStudyDuration: The expected study duration.
  - expectedInformation: The expected information.
  - accrualDuration: The accrual duration.
  - followupTime: The follow-up duration.
  - fixedFollowup: Whether a fixed follow-up design is used.
  - kMax: The number of stages.
  - milestone: The milestone time to calculate the restricted mean survival time.
  - rmstH0: The restricted mean survival time under the null hypothesis.
  - rmst: The restricted mean survival time under the alternative hypothesis.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.

- – cumulativeAlphaSpent: The cumulative alpha spent.
- – numberOfEvents: The number of events.
- – numberOfDropouts: The number of dropouts.
- – numberOfSubjects: The number of subjects.
- – numberOfMilestone: The number of subjects reaching milestone.
- – analysisTime: The average time since trial start.
- – efficacyRmst: The efficacy boundaries on the restricted mean survival time.
- – futilityRmst: The futility boundaries on the restricted mean survival time.
- – efficacyP: The efficacy boundaries on the p-value scale.
- – futilityP: The futility boundaries on the p-value scale.
- – information: The cumulative information.
- – efficacyStopping: Whether to allow efficacy stopping.
- – futilityStopping: Whether to allow futility stopping.
- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, typeBetaSpending, parameterBetaSpending, accrualTime, accuralIntensity, piecewiseSurvivalTime, stratumFraction, lambda, gamma, and spendingTime.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

See Also

rmstat

Examples

```
rmpower1s(kMax = 2, informationRates = c(0.8, 1),
          alpha = 0.025, typeAlphaSpending = "sfOF",
          milestone = 18, rmstH0 = 10,
          accrualTime = seq(0, 8),
          accrualIntensity = 26/9*seq(1, 9),
          piecewiseSurvivalTime = c(0, 6),
          stratumFraction = c(0.2, 0.8),
          lambda = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
          gamma = -log(1-0.05)/12, accrualDuration = 22,
          followupTime = 18, fixedFollowup = FALSE)
```

---

rmpowerequiv *Power for Equivalence in Restricted Mean Survival Time Difference*

Description

Obtains the power for equivalence in restricted mean survival time difference.

Usage

```
rmpowerequiv(
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  milestone = NA_real_,
  rmstDiffLower = NA_real_,
  rmstDiffUpper = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  spendingTime = NA_real_,
  studyDuration = NA_real_
)
```

Arguments

kMax   The maximum number of stages.

informationRates

The information rates. Defaults to (1:kMax) / kMax if left unspecified.

criticalValues   Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha   The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

milestone   The milestone time at which to calculate the restricted mean survival time.

rmstDiffLower   The lower equivalence limit of restricted mean survival time difference.

rmstDiffUpper   The upper equivalence limit of restricted mean survival time difference.

allocationRatioPlanned

    Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

    A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

    A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

    A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1   A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.

lambda2   A vector of hazard rates for the event in each analysis time interval by stratum for the control group.

gamma1   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.

gamma2   The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration

    Duration of the enrollment period.

followupTime   Follow-up time for the last enrolled subject.

fixedFollowup   Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

studyDuration   Study duration for fixed follow-up design. Defaults to missing, which is to be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and followupTime.

Value

An S3 class rmpowerequiv object with 4 components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.

- – alpha: The overall significance level.
    - – numberOfEvents: The total number of events.
    - – numberOfSubjects: The total number of subjects.
    - – studyDuration: The total study duration.
    - – information: The maximum information.
    - – expectedNumberOfEvents: The expected number of events.
    - – expectedNumberOfSubjects: The expected number of subjects.
    - – expectedStudyDuration: The expected study duration.
    - – expectedInformation: The expected information.
    - – kMax: The number of stages.
    - – milestone: The milestone time relative to randomization.
    - – rmstDiffLower: The lower equivalence limit of restricted mean survival time difference.
    - – rmstDiffUpper: The upper equivalence limit of restricted mean survival time difference.
    - – rmst1: The restricted mean survival time for the treatment group.
    - – rmst2: The restricted mean survival time for the control group.
    - – rmstDiff: The restricted mean survival time difference.
    - – accrualDuration: The accrual duration.
    - – followupTime: The follow-up duration.
    - – fixedFollowup: Whether a fixed follow-up design is used.

- byStageResults: A data frame containing the following variables:

    - – informationRates: The information rates.
    - – efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
    - – rejectPerStage: The probability for efficacy stopping.
    - – cumulativeRejection: The cumulative probability for efficacy stopping.
    - – cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
    - – cumulativeAttainedAlphaH10: The cumulative alpha attained under H10.
    - – cumulativeAttainedAlphaH20: The cumulative alpha attained under H20.
    - – numberOfEvents: The number of events.
    - – numberOfDropouts: The number of dropouts.
    - – numberOfSubjects: The number of subjects.
    - – numberOfMilestone: The number of subjects reaching milestone.
    - – analysisTime: The average time since trial start.
    - – efficacyRmstDiffLower: The efficacy boundaries on the restricted mean survival time difference scale for the one-sided null hypothesis at the lower equivalence limit.
    - – efficacyRmstDiffUpper: The efficacy boundaries on the restricted mean survival time difference scale for the one-sided null hypothesis at the upper equivalence limit.
    - – efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
    - – information: The cumulative information.

- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, allocationRatioPlanned, accrualTime, accuralIntensity, piecewiseSurvivalTime, stratumFraction, lambda1, lambda2, gamma1, gamma2, and spendingTime.

- byTreatmentCounts: A list containing the following counts by treatment group:
    - numberOfEvents1: The number of events by stage for the treatment group.
    - numberOfDropouts1: The number of dropouts by stage for the treatment group.
    - numberOfSubjects1: The number of subjects by stage for the treatment group.
    - numberOfMilestone1: The number of subjects reaching milestone by stage for the active treatment group.
    - numberOfEvents2: The number of events by stage for the control group.
    - numberOfDropouts2: The number of dropouts by stage for the control group.
    - numberOfSubjects2: The number of subjects by stage for the control group.
    - numberOfMilestone2: The number of subjects reaching milestone by stage for the control group.
    - expectedNumberOfEvents1: The expected number of events for the treatment group.
    - expectedNumberOfDropouts1: The expected number of dropouts for the active treatment group.
    - expectedNumberOfSubjects1: The expected number of subjects for the active treatment group.
    - expectedNumberOfMilestone1: The expected number of subjects reaching milestone for the active treatment group.
    - expectedNumberOfEvents2: The expected number of events for control group.
    - expectedNumberOfDropouts2: The expected number of dropouts for the control group.
    - expectedNumberOfSubjects2: The expected number of subjects for the control group.
    - expectedNumberOfMilestone2: The expected number of subjects reaching milestone for the control group.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

See Also

rmstat

Examples

```
rmpowerequiv(kMax = 2, informationRates = c(0.5, 1),
             alpha = 0.05, typeAlphaSpending = "sfOF",
             milestone = 18,
             rmstDiffLower = -2, rmstDiffUpper = 2,
             allocationRatioPlanned = 1, accrualTime = seq(0, 8),
             accrualIntensity = 100/9*seq(1, 9),
             piecewiseSurvivalTime = c(0, 6),
             stratumFraction = c(0.2, 0.8),
             lambda1 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
             lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
             gamma1 = -log(1-0.05)/12,
             gamma2 = -log(1-0.05)/12, accrualDuration = 22,
             followupTime = 18, fixedFollowup = FALSE)
```

---

rmsamplesize   *Sample Size for Difference in Restricted Mean Survival Times*

Description

Obtains the needed accrual duration given power, accrual intensity, and follow-up time, the needed
follow-up time given power, accrual intensity, and accrual duration, or the needed absolute accrual
intensity given power, relative accrual intensity, accrual duration, and follow-up time in a two-group
survival design.

Usage

```
rmsamplesize(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  milestone = NA_real_,
  rmstDiffH0 = 0,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  interval = as.numeric(c(0.001, 240)),
  spendingTime = NA_real_,
  rounding = 1L
)
```

Arguments

beta	Type II error. Defaults to 0.2.
kMax	The maximum number of stages.
informationRates	
	The information rates. Defaults to (1:kMax) / kMax if left unspecified.
efficacyStopping	
	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	
	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	
	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	
	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	
	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.
typeBetaSpending	
	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	
	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
userBetaSpending	
	The user defined beta spending. Cumulative beta spent up to each stage.
milestone	The milestone time at which to calculate the restricted mean survival time.
rmstDiffH0	The difference in restricted mean survival times under the null hypothesis. Defaults to 0 for superiority test.
allocationRatioPlanned	
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time
                   intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual
                   intervals: [0, 3) and [3, Inf).

accrualIntensity
                   A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime
                   A vector that specifies the starting time of piecewise exponential survival time
                   intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event
                   intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction
                   A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1   A vector of hazard rates for the event in each analysis time interval by stratum
                   for the active treatment group.

lambda2   A vector of hazard rates for the event in each analysis time interval by stratum
                   for the control group.

gamma1   The hazard rate for exponential dropout, a vector of hazard rates for piece-
                   wise exponential dropout applicable for all strata, or a vector of hazard rates
                   for dropout in each analysis time interval by stratum for the active treatment
                   group.

gamma2   The hazard rate for exponential dropout, a vector of hazard rates for piece-
                   wise exponential dropout applicable for all strata, or a vector of hazard rates
                   for dropout in each analysis time interval by stratum for the control group.

accrualDuration
                   Duration of the enrollment period.

followupTime   Follow-up time for the last enrolled subject.

fixedFollowup   Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

interval   The interval to search for the solution of accrualDuration, followupTime, or the
                   proportionality constant of accrualIntensity. Defaults to `c(0.001, 240)`.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to
                   missing, in which case, it is the same as `informationRates`.

rounding   Whether to round up sample size. Defaults to 1 for sample size rounding.

Value

A list of two components:

- resultsUnderH1: An S3 class rmpower object under the alternative hypothesis.

- resultsUnderH0: An S3 class rmpower object under the null hypothesis.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

See Also

rmpower

Examples

```
# Example 1: Obtains follow-up time given power, accrual intensity,
# and accrual duration for variable follow-up. Of note, the power
# reaches the maximum when the follow-up time equals milestone.

rmsamplesize(beta = 0.2, kMax = 2, informationRates = c(0.8, 1),
             alpha = 0.025, typeAlphaSpending = "sfOF",
             milestone = 18,
             allocationRatioPlanned = 1, accrualTime = seq(0, 8),
             accrualIntensity = 100/9*seq(1, 9),
             piecewiseSurvivalTime = c(0, 6),
             stratumFraction = c(0.2, 0.8),
             lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
             lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
             gamma1 = -log(1-0.05)/12,
             gamma2 = -log(1-0.05)/12, accrualDuration = 22,
             followupTime = NA, fixedFollowup = FALSE)

# Example 2: Obtains accrual intensity given power, accrual duration, and
# follow-up time for variable follow-up

rmsamplesize(beta = 0.2, kMax = 2, informationRates = c(0.8, 1),
             alpha = 0.025, typeAlphaSpending = "sfOF",
             milestone = 18,
             allocationRatioPlanned = 1, accrualTime = seq(0, 8),
             accrualIntensity = 100/9*seq(1, 9),
             piecewiseSurvivalTime = c(0, 6),
             stratumFraction = c(0.2, 0.8),
             lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
             lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
             gamma1 = -log(1-0.05)/12,
             gamma2 = -log(1-0.05)/12, accrualDuration = 22,
             followupTime = 18, fixedFollowup = FALSE)


# Example 3: Obtains accrual duration given power, accrual intensity, and
# follow-up time for fixed follow-up

rmsamplesize(beta = 0.2, kMax = 2, informationRates = c(0.8, 1),
             alpha = 0.025, typeAlphaSpending = "sfOF",
             milestone = 18,
             allocationRatioPlanned = 1, accrualTime = seq(0, 8),
             accrualIntensity = 100/9*seq(1, 9),
             piecewiseSurvivalTime = c(0, 6),
             stratumFraction = c(0.2, 0.8),
             lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
             lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
             gamma1 = -log(1-0.05)/12,
             gamma2 = -log(1-0.05)/12, accrualDuration = NA,
             followupTime = 18, fixedFollowup = TRUE)
```

---

rmsamplesize1s   *Sample Size for One-Sample Restricted Mean Survival Time*

Description

Obtains the needed accrual duration given power and follow-up time, the needed follow-up time given power and accrual duration, or the needed absolute accrual rates given power, accrual duration, follow-up duration, and relative accrual rates in a one-group survival design.

Usage

```
rmsamplesize1s(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  milestone = NA_real_,
  rmstH0 = NA_real_,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda = NA_real_,
  gamma = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  interval = as.numeric(c(0.001, 240)),
  spendingTime = NA_real_,
  rounding = 1L
)
```

Arguments

beta	Type II error. Defaults to 0.2.
kMax	The maximum number of stages.

informationRates

The information rates. Defaults to `(1:kMax) / kMax` if left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues   Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha   The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds   Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to `rep(-6, kMax-1)` if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

milestone   The milestone time at which to calculate the restricted survival time.

rmstH0   The restricted mean survival time under the null hypothesis.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda   A vector of hazard rates for the event in each analysis time interval by stratum under the alternative hypothesis.

gamma   The hazard rate for exponential dropout or a vector of hazard rates for piecewise exponential dropout. Defaults to 0 for no dropout.

accrualDuration

Duration of the enrollment period.

followupTime   Follow-up time for the last enrolled subject.

fixedFollowup   Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

interval   The interval to search for the solution of accrualDuration, followupDuration, or the proportionality constant of accrualIntensity. Defaults to c(0.001, 240).

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

rounding   Whether to round up sample size. Defaults to 1 for sample size rounding.

Value

A list of two components:

- resultsUnderH1: An S3 class rmpower1s object under the alternative hypothesis.
- resultsUnderH0: An S3 class rmpower1s object under the null hypothesis.

Author(s)

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See Also

[rmpower1s](#)

Examples

```
# Example 1: Obtains follow-up duration given power, accrual intensity,
# and accrual duration for variable follow-up

rmsamplesize1s(beta = 0.2, kMax = 2,
               informationRates = c(0.8, 1),
               alpha = 0.025, typeAlphaSpending = "sfOF",
               milestone = 18, rmstH0 = 10,
               accrualTime = seq(0, 8),
               accrualIntensity = 26/9*seq(1, 9),
               piecewiseSurvivalTime = c(0, 6),
               stratumFraction = c(0.2, 0.8),
               lambda = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
               gamma = -log(1-0.05)/12, accrualDuration = 22,
               followupTime = NA, fixedFollowup = FALSE)

# Example 2: Obtains accrual intensity given power, accrual duration, and
```

```
# follow-up duration for variable follow-up

rmsamplesize1s(beta = 0.2, kMax = 2,
               informationRates = c(0.8, 1),
               alpha = 0.025, typeAlphaSpending = "sfOF",
               milestone = 18, rmstH0 = 10,
               accrualTime = seq(0, 8),
               accrualIntensity = 26/9*seq(1, 9),
               piecewiseSurvivalTime = c(0, 6),
               stratumFraction = c(0.2, 0.8),
               lambda = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
               gamma = -log(1-0.05)/12, accrualDuration = 22,
               followupTime = 18, fixedFollowup = FALSE)


# Example 3: Obtains accrual duration given power, accrual intensity, and
# follow-up duration for fixed follow-up

rmsamplesize1s(beta = 0.2, kMax = 2,
               informationRates = c(0.8, 1),
               alpha = 0.025, typeAlphaSpending = "sfOF",
               milestone = 18, rmstH0 = 10,
               accrualTime = seq(0, 8),
               accrualIntensity = 26/9*seq(1, 9),
               piecewiseSurvivalTime = c(0, 6),
               stratumFraction = c(0.2, 0.8),
               lambda = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
               gamma = -log(1-0.05)/12, accrualDuration = NA,
               followupTime = 18, fixedFollowup = TRUE)
```

---

rmsamplesizeequiv	*Sample Size for Equivalence in Restricted Mean Survival Time Difference*

Description

Obtains the sample size for equivalence in restricted mean survival time difference.

Usage

```
rmsamplesizeequiv(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
```

```
  milestone = NA_real_,
  rmstDiffLower = NA_real_,
  rmstDiffUpper = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  interval = as.numeric(c(0.001, 240)),
  spendingTime = NA_real_,
  rounding = 1L
)
```

Arguments

beta	The type II error.
kMax	The maximum number of stages.
informationRates	
	The information rates. Defaults to (1:kMax) / kMax if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level for each of the two one-sided tests. Defaults to 0.05.
typeAlphaSpending	
	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	
	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	
	The user defined alpha spending. Cumulative alpha spent up to each stage.
milestone	The milestone time at which to calculate the restricted mean survival time.
rmstDiffLower	The lower equivalence limit of restricted mean survival time difference.
rmstDiffUpper	The upper equivalence limit of restricted mean survival time difference.
allocationRatioPlanned	
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time
                    intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual
                    intervals: [0, 3) and [3, Inf).

accrualIntensity
                    A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime
                    A vector that specifies the starting time of piecewise exponential survival time
                    intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event
                    intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction
                    A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1   A vector of hazard rates for the event in each analysis time interval by stratum
                    for the active treatment group.

lambda2   A vector of hazard rates for the event in each analysis time interval by stratum
                    for the control group.

gamma1   The hazard rate for exponential dropout, a vector of hazard rates for piece-
                    wise exponential dropout applicable for all strata, or a vector of hazard rates
                    for dropout in each analysis time interval by stratum for the active treatment
                    group.

gamma2   The hazard rate for exponential dropout, a vector of hazard rates for piece-
                    wise exponential dropout applicable for all strata, or a vector of hazard rates
                    for dropout in each analysis time interval by stratum for the control group.

accrualDuration
                    Duration of the enrollment period.

followupTime   Follow-up time for the last enrolled subject.

fixedFollowup   Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

interval   The interval to search for the solution of accrualDuration, followupDuration, or
                    the proportionality constant of accrualIntensity. Defaults to `c(0.001, 240)`.

spendingTime   A vector of length kMax for the error spending time at each analysis. Defaults to
                    missing, in which case, it is the same as `informationRates`.

rounding   Whether to round up sample size. Defaults to 1 for sample size rounding.

Value

An S3 class `rmpowerequiv` object

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

See Also

rmpowerequiv

Examples

```
rmsamplesizeequiv(beta = 0.1, kMax = 2, informationRates = c(0.5, 1),
                  alpha = 0.05, typeAlphaSpending = "sfOF",
                  milestone = 18,
                  rmstDiffLower = -2, rmstDiffUpper = 2,
                  allocationRatioPlanned = 1, accrualTime = seq(0, 8),
                  accrualIntensity = 26/9*seq(1, 9),
                  piecewiseSurvivalTime = c(0, 6),
                  stratumFraction = c(0.2, 0.8),
                  lambda1 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
                  lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
                  gamma1 = -log(1-0.05)/12,
                  gamma2 = -log(1-0.05)/12, accrualDuration = NA,
                  followupTime = 18, fixedFollowup = FALSE)
```

---

rmst   *Restricted Mean Survival Time*

Description

Obtains the restricted mean survival time over an interval.

Usage

```
rmst(t1 = 0, t2 = NA_real_, piecewiseSurvivalTime = 0L, lambda = NA_real_)
```

Arguments

t1	Lower bound of the analysis time interval.
t2	Upper bound of the analysis time interval.
piecewiseSurvivalTime	
	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.
lambda	A vector of hazard rates for the event. One for each analysis time interval.

Value

The integral of the survival function from t1 to t2

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
rmst(t1 = 0, t2 = 7, piecewiseSurvivalTime = c(0, 6),
     lambda = c(0.0533, 0.0309))
```

rmstat   *Stratified Difference in Restricted Mean Survival Times*

Description

Obtains the stratified restricted mean survival times and difference in restricted mean survival times at given calendar times.

Usage

```
rmstat(
  time = NA_real_,
  milestone = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L
)
```

Arguments

time   A vector of calendar times for data cut.

milestone   The milestone time at which to calculate the restricted mean survival time.

allocationRatioPlanned

        Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime   A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

        A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

        A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

        A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1   A vector of hazard rates for the event in each analysis time interval by stratum
               for the active treatment group.

lambda2   A vector of hazard rates for the event in each analysis time interval by stratum
               for the control group.

gamma1   The hazard rate for exponential dropout, a vector of hazard rates for piece-
               wise exponential dropout applicable for all strata, or a vector of hazard rates
               for dropout in each analysis time interval by stratum for the active treatment
               group.

gamma2   The hazard rate for exponential dropout, a vector of hazard rates for piece-
               wise exponential dropout applicable for all strata, or a vector of hazard rates
               for dropout in each analysis time interval by stratum for the control group.

accrualDuration
               Duration of the enrollment period.

followupTime   Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

Value

A data frame containing the following variables:

- `time`: The calendar time since trial start.
- `subjects`: The number of enrolled subjects.
- `nevents`: The total number of events.
- `nevents1`: The number of events in the active treatment group.
- `nevents2`: The number of events in the control group.
- `ndropouts`: The total number of dropouts.
- `ndropouts1`: The number of dropouts in the active treatment group.
- `ndropouts2`: The number of dropouts in the control group.
- `milestone`: The milestone time relative to randomization.
- `nmilestone`: The total number of subjects reaching milestone.
- `nmilestone1`: The number of subjects reaching milestone in the active treatment group.
- `nmiletone2`: The number of subjects reaching milestone in the control group.
- `rmst1`: The restricted mean survival time for the treatment group.
- `rmst2`: The restricted mean survival time for the control group.
- `rmstDiff`: The difference in restricted mean survival times, i.e., rmst1 – rmst2.
- `vrmst1`: The variance for `rmst1`.
- `vrmst2`: The variance for `rmst2`.
- `vrmstDiff`: The variance for `rmstDiff`.
- `information`: The information for `rmstDiff`, equal to 1/`vrmstDiff`.
- `rmstDiffZ`: The Z-statistic value, i.e., rmstDiff/sqrt(vrmstDiff).

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
# Piecewise accrual, piecewise exponential survivals, and 5% dropout by
# the end of 1 year.

rmstat(time = c(22, 40),
       milestone = 18,
       allocationRatioPlanned = 1,
       accrualTime = seq(0, 8),
       accrualIntensity = 26/9*seq(1, 9),
       piecewiseSurvivalTime = c(0, 6),
       stratumFraction = c(0.2, 0.8),
       lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
       lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
       gamma1 = -log(1-0.05)/12,
       gamma2 = -log(1-0.05)/12,
       accrualDuration = 22,
       followupTime = 18, fixedFollowup = FALSE)
```

rtpwexp	*Random Number Generation Function of Truncated Piecewise Exponential Distribution*

Description

Obtains random samples from a truncated piecewise exponential distribution.

Usage

```
rtpwexp(n, piecewiseSurvivalTime = 0, lambda = 0.0578, lowerBound = 0)
```

Arguments

n	The number of observations.
piecewiseSurvivalTime	
	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.
lambda	A vector of hazard rates for the event. One for each analysis time interval.
lowerBound	The left truncation time point for the survival time. Defaults to 0 for no truncation.

Value

The random numbers from truncated piecewise exponential distribution.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
rtpwexp(n = 10, piecewiseSurvivalTime = c(0, 6, 9, 15),
        lambda = c(0.025, 0.04, 0.015, 0.007))
```

---

runShinyApp_lrstat   *Run Shiny App*

Description

Runs the log-rank test power and sample size calculation Shiny app.

Usage

```
runShinyApp_lrstat()
```

Value

No return value, called for side effects.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

---

sexagg   *Urinary tract infection data from the logistf package*

Description

This data set deals with urinary tract infection in sexually active college women, along with covariate information on age an contraceptive use. The variables are all binary and coded in 1 (condition is present) and 0 (condition is absent).

Usage

```
sexagg
```

Format

An object of class data.frame with 36 rows and 9 columns.

Details

case urinary tract infection, the study outcome variable

age >= 24 years

dia use of diaphragm

oc use of oral contraceptive

vic use of condom

vicl use of lubricated condom

vis use of spermicide

---

shilong   *The randomized clinical trial SHIVA data in long format from the ipcwswitch package*

Description

The original SHIdat data set contains an anonymized excerpt of data from the SHIVA01 trial. This was the first randomized clinical trial that aimed at comparing molecularly targeted therapy based on tumor profiling (MTA) versus conventional therapy (CT) for advanced cancer. Patients were randomly assigned to receive the active or control treatment and may switch to the other arm or subsequent anti-cancer therapy upon disease progression. The restructured data is in the long format.

id The patient's identifier

tstart The start of the time interval

tstop The end of the time interval

event Whether the patient died at the end of the interval

agerand The patient's age (in years) at randomization

sex.f The patients' gender, either Male or Female

tt_Lnum The number of previous lines of treatment

rmh_alea.c The Royal Marsden Hospital score segregated into two categories

pathway.f The molecular pathway altered (the hormone receptors pathway, the PI3K/ AKT/mTOR pathway, and the RAF/MEK pathway)

bras.f The patient's randomized arm, either MTA or CT

ps The ECOG performance status

ttc The presence of concomitant treatments

tran The use of platelet transfusions

dpd The relative day of a potential progression

dco The relative day of treatment switching

ady The relative day of the latest news

dcut The relative day of administrative cutoff

pd Whether the patient had disease progression

co Whether the patient switched treatment

Usage

```
shilong
```

Format

An object of class data.frame with 602 rows and 19 columns.

---

simon2stage   *Simon's Two-Stage Design*

Description

Obtains Simon's two-stage minimax, admissible, and optimal designs.

Usage

```
simon2stage(
  alpha = NA_real_,
  beta = NA_real_,
  piH0 = NA_real_,
  pi = NA_real_,
  n_max = 110L
)
```

Arguments

alpha	Type I error rate (one-sided).
beta	Type II error rate (1-power).
piH0	Response probability under the null hypothesis.
pi	Response probability under the alternative hypothesis.
n_max	Upper limit for sample size, defaults to 110.

Value

A data frame containing the following variables:

- piH0: Response probability under the null hypothesis.
- pi: Response probability under the alternative hypothesis.
- alpha: The specified one-sided significance level.
- beta: The specified type II error.
- n: Total sample size.
- n1: Stage 1 sample size.
- r1: Futility boundary for stage 1.
- r: Futility boundary for stage 2.

- `EN0`: Expected sample size under the null hypothesis.
- `attainedAlpha`: Attained type 1 error.
- `power`: Attained power.
- `PET0`: Probability of early stopping under the null hypothesis.
- `w_lower`: Lower bound of the interval for `w`.
- `w_upper`: Upper bound of the interval for `w`.
- `design`: Description of the design, e.g., minimax, admissible, or optimal.

Here `w` is the weight in the objective function: `w*n + (1-w)*EN0`.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
simon2stage(0.05, 0.2, 0.1, 0.3)
```

---

simonBayesAnalysis   *Analysis of Simon's Bayesian Basket Trials*

Description

Obtains the prior and posterior probabilities for Simon's Bayesian basket discovery trials.

Usage

```
simonBayesAnalysis(
  nstrata = NA_integer_,
  r = NA_real_,
  n = NA_real_,
  lambda = NA_real_,
  gamma = NA_real_,
  phi = NA_real_,
  plo = NA_real_
)
```

Arguments

nstrata	The number of strata.
r	The vector of number of responders across strata.
n	The vector of number of subjects across strata.
lambda	The prior probability that the drug activity is homogeneous across strata.
gamma	The prior probability that the drug is active in a stratum.
phi	The response probability for an active drug.
plo	The response probability for an inactive drug.

Value

A list containing the following five components:

- case: The matrix with each row corresponding to a combination of drug activity over strata represented by the columns.
- prior_case: The vector of joint prior probabilities for the stratum-specific response rates.
- prior_stratum: The vector of marginal prior probabilities for the stratum-specific response rates.
- post_case: The vector of joint posterior probabilities for the stratum-specific response rates.
- post_stratum: The vector of marginal posterior probabilities for the stratum-specific response rates.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
a = simonBayesAnalysis(
  nstrata = 10,
  r = c(8,0,1,1,6,2,0,0,3,3),
  n = c(19,10,26,8,14,7,8,5,4,14),
  lambda = 0.5, gamma = 0.33,
  phi = 0.35, plo = 0.15)

a$post_stratum
```

---

simonBayesSim   *Simulation of Simon's Bayesian Basket Trials*

Description

Obtains the simulated raw and summary data for Simon's Bayesian basket discovery trials.

Usage

```
simonBayesSim(
  p = NA_real_,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  stratumFraction = 1L,
  lambda = NA_real_,
  gamma = NA_real_,
  phi = NA_real_,
  plo = NA_real_,
  T = NA_real_,
```

```
  maxSubjects = NA_integer_,
  plannedSubjects = NA_integer_,
  maxNumberOfIterations = 1000L,
  maxNumberOfRawDatasets = 1L,
  seed = NA_integer_
)
```

Arguments

p	The vector of true response probabilities across strata.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).
accrualIntensity	
	A vector of accrual intensities. One for each accrual time interval.
stratumFraction	
	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
lambda	The prior probability that the drug activity is homogeneous across strata.
gamma	The prior probability that the drug is active in a stratum.
phi	The response probability for an active drug.
plo	The response probability for an inactive drug.
T	The threshold for a conclusive posterior probability to stop enrollment.
maxSubjects	The maximum total sample size.
plannedSubjects	
	The planned cumulative number of subjects at each stage.
maxNumberOfIterations	
	The number of simulation iterations. Defaults to 1000.
maxNumberOfRawDatasets	
	The number of raw datasets to extract.
seed	The seed to reproduce the simulation results. The seed from the environment will be used if left unspecified,

Value

A list containing the following four components:

- rawdata: A data frame for subject-level data, containing the following variables:
    - iterationNumber: The iteration number.
    - stageNumber: The stage number.
    - subjectId: The subject ID.
    - arrivalTime: The enrollment time for the subject.
    - stratum: The stratum for the subject.
    - y: Whether the subject was a responder (1) or nonresponder (0).
- sumdata1: A data frame for simulation and stratum-level summary data, containing the following variables:

- – `iterationNumber`: The iteration number.
- – `stageNumber`: The stage number.
- – `stratum`: The stratum number.
- – `active`: Whether the drug is active in the stratum.
- – `n`: The number of subjects in the stratum.
- – `r`: The number of responders in the stratum.
- – `posterior`: The posterior probability that the drug is active in the stratum.
- – `open`: Whether the stratum is still open for enrollment.
- – `positive`: Whether the stratum has been determined to be a positive stratum.
- – `negative`: Whether the stratum has been determined to be a negative stratum.
- `sumdata2`: A data frame for the simulation level summary data, containing the following variables:
  - – `iterationNumber`: The iteration number.
  - – `numberOfStrata`: The total number of strata.
  - – `n_active_strata`: The number of active strata.
  - – `true_positive`: The number of true positive strata.
  - – `false_negative`: The number of false negative strata.
  - – `false_positive`: The number of false positive strata.
  - – `true_negative`: The number of true negative strata.
  - – `n_indet_strata`: The number of indeterminate strata.
  - – `numberOfSubjects`: The number of subjects.
- `overview`: A data frame for the summary across simulations, containing the following variables:
  - – `numberOfStrata`: The total number of strata.
  - – `n_active_strata`: The average number of active strata.
  - – `true_positive`: The average number of true positive strata.
  - – `false_negative`: The average number of false negative strata.
  - – `false_positive`: The average number of false positive strata.
  - – `true_negative`: The average number of true negative strata.
  - – `n_indet_strata`: The average number of indeterminate strata.
  - – `numberOfSubjects`: The average number of subjects.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
sim1 = simonBayesSim(
  p = c(0.25, 0.25, 0.05),
  accrualIntensity = 5,
  stratumFraction = c(1/3, 1/3, 1/3),
  lambda = 0.33, gamma = 0.5,
  phi = 0.25, plo = 0.05,
  T = 0.8, maxSubjects = 50,
```

```
  plannedSubjects = seq(5, 50, 5),
  maxNumberOfIterations = 1000,
  maxNumberOfRawDatasets = 1,
  seed = 314159)

sim1$overview
```

---

six | *The repeated measures data from the "Six Cities" study of the health effects of air pollution (Ware et al. 1984).*

Description

The data analyzed are the 16 selected cases in Lipsitz et al. (1994). The binary response is the wheezing status of 16 children at ages 9, 10, 11, and 12 years. A value of 1 of wheezing status indicates the occurrence of wheezing. The explanatory variables city of residence, age, and maternal smoking status at the particular age.

Usage

```
six
```

Format

An object of class tbl_df (inherits from tbl, data.frame) with 64 rows and 6 columns.

Details

case case id

city city of residence

age age of the child

smoke maternal smoking status

wheeze wheezing status

---

survfit_phregr   *Survival Curve for Proportional Hazards Regression Models*

Description

Obtains the predicted survivor function for a proportional hazards regression model.

Usage

```
survfit_phregr(
  fit_phregr,
  newdata,
  sefit = TRUE,
  conftype = "log-log",
  conflev = 0.95
)
```

Arguments

fit_phregr	The output from the phregr call.
newdata	A data frame with the same variable names as those that appear in the phregr call. For right-censored data, one curve is produced per row to represent a cohort whose covariates correspond to the values in newdata. For counting-process data, one curve is produced per id in newdata to present the survival curve along the path of time-dependent covariates at the observed event times in the data used to fit phregr.
sefit	Whether to compute the standard error of the survival estimates.
conftype	The type of the confidence interval. One of "none", "plain", "log", "log-log" (the default), or "arcsin". The arcsin option bases the intervals on asin(sqrt(surv)).
conflev	The level of the two-sided confidence interval for the survival probabilities. Defaults to 0.95.

Details

If newdata is not provided and there is no covariate, survival curves based on the basehaz data frame will be produced.

Value

A data frame with the following variables:

- id: The id of the subject for counting-process data with time-dependent covariates.
- time: The observed times in the data used to fit phregr.
- nrisk: The number of patients at risk at the time point in the data used to fit phregr.
- nevent: The number of patients having event at the time point in the data used to fit phregr.

- cumhaz: The cumulative hazard at the time point.
- surv: The estimated survival probability at the time point.
- sesurv: The standard error of the estimated survival probability.
- lower: The lower confidence limit for survival probability.
- upper: The upper confidence limit for survival probability.
- conflev: The level of the two-sided confidence interval.
- conftype: The type of the confidence interval.
- covariates: The values of covariates based on newdata.
- stratum: The stratum of the subject.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Terry M. Therneau and Patricia M. Grambsch. Modeling Survival Data: Extending the Cox Model. Springer-Verlag, 2000.

Examples

```
library(dplyr)

# Example 1 with right-censored data
fit1 <- phregr(data = rawdata %>% filter(iterationNumber == 1) %>%
                 mutate(treat = 1*(treatmentGroup == 1)),
               stratum = "stratum",
               time = "timeUnderObservation", event = "event",
               covariates = "treat")

surv1 <- survfit_phregr(fit1,
                        newdata = data.frame(
                          stratum = as.integer(c(1,1,2,2)),
                          treat = c(1,0,1,0)))

# Example 2 with counting process data and robust variance estimate
fit2 <- phregr(data = heart %>% mutate(rx = as.numeric(transplant) - 1),
               time = "start", time2 = "stop", event = "event",
               covariates = c("rx", "age"), id = "id", robust = TRUE)

surv2 <- survfit_phregr(fit2,
                        newdata = data.frame(
                          id = c(4,4,11,11),
                          age = c(-7.737,-7.737,-0.019,-0.019),
                          start = c(0,36,0,26),
                          stop = c(36,39,26,153),
                          rx = c(0,1,0,1)))
```

---

survQuantile	*Brookmeyer-Crowley Confidence Interval for Quantiles of Right-Censored Time-to-Event Data*

Description

Obtains the Brookmeyer-Crowley confidence interval for quantiles of right-censored time-to-event data.

Usage

```
survQuantile(
  time = NA_real_,
  event = NA_real_,
  cilevel = 0.95,
  transform = "loglog",
  probs = c(0.25, 0.5, 0.75)
)
```

Arguments

time	The vector of possibly right-censored survival times.
event	The vector of event indicators.
cilevel	The confidence interval level. Defaults to 0.95.
transform	The transformation of the survival function to use to construct the confidence interval. Options include "linear", "loglog", "log", "asinsqrt", and "logit". Defaults to "loglog".
probs	The vector of probabilities to calculate the quantiles. Defaults to c(0.25, 0.5, 0.75).

Value

A data frame containing the estimated quantile and confidence interval corresponding to each specified probability. It includes the following variables:

- prob: The probability to calculate the quantile.
- quantile: The estimated quantile.
- lower: The lower limit of the confidence interval.
- upper: The upper limit of the confidence interval.
- cilevel: The confidence interval level.
- transform: The transformation of the survival function to use to construct the confidence interval.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
survQuantile(
  time = c(33.7, 3.9, 10.5, 5.4, 19.5, 23.8, 7.9, 16.9, 16.6,
           33.7, 17.1, 7.9, 10.5, 38),
  event = c(0, 1, 1, 1, 1, 0, 1, 0, 0, 0, 0, 0, 1, 1),
  probs = c(0.25, 0.5, 0.75))
```

---

svdcpp	*Singular Value Decomposition of a Matrix*

Description

Computes the singular-value decomposition of a rectangular matrix.

Usage

```
svdcpp(X, outtransform = 1L, decreasing = 1L)
```

Arguments

X	A numeric matrix whose SVD decomposition is to be computed.
outtransform	Whether the orthogonal matrices composing of the left and right singular vectors are to be computed.
decreasing	Whether the singular values should be sorted in decreasing order and the corresponding singular vectors rearranged accordingly.

Details

Given $A \in R^{m \times n}(m \geq n)$, the following algorithm overwrites A with $U^T A V = D$, where $U \in R^{m \times m}$ is orthogonal, $V \in R^{n \times n}$ is orthogonal, and $D \in R^{m \times n}$ is diagonal.

Value

A list with the following components:

- d: A vector containing the singular values of X.
- U: A matrix whose columns contain the left singular vectors of X.
- V: A matrix whose columns contain the right singular vectors of X.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

References

Gene N. Golub and Charles F. Van Loan. Matrix Computations, second edition. Baltimore, Maryland: The John Hopkins University Press, 1989, p.434.

Examples

```
A <- matrix(c(1,0,0,0, 1,2,0,0, 0,1,3,0, 0,0,1,4), 4, 4)
svdcpp(A)
```

---

tobin   *Tobin's tobit data from the survival package*

Description

Data from Tobin's original paper.

durable Durable goods purchase

age Age in years

quant Liquidity ratio (x 1000)

Usage

```
tobin
```

Format

An object of class data.frame with 20 rows and 3 columns.

---

updateGraph   *Update Graph for Graphical Approaches*

Description

Updates the weights and transition matrix for graphical approaches.

Usage

```
updateGraph(w, G, I, j)
```

Arguments

w	The current vector of weights for elementary hypotheses.
G	The current transition matrix.
I	The set of indices for yet to be rejected hypotheses.
j	The hypothesis to remove from index set I.

Value

A list containing the new vector of weights, the new transition matrix for the graph, and the new set of indices of yet to be rejected hypotheses.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
updateGraph(w = c(0.5, 0.5, 0, 0),
            G = matrix(c(0, 0.5, 0.5, 0,  0.5, 0, 0, 0.5,
                         0, 1, 0, 0,  1, 0, 0, 0),
                       nrow=4, ncol=4, byrow=TRUE),
            I = c(1, 2, 3, 4),
            j = 1)
```

---

zstatOddsRatio *Miettinen-Nurminen Score Test Statistic for Two-Sample Odds Ratio*

Description

Obtains the Miettinen-Nurminen score test statistic for two-sample odds ratio possibly with stratification.

Usage

```
zstatOddsRatio(
  oddsRatioH0 = 1,
  n1 = NA_real_,
  y1 = NA_real_,
  n2 = NA_real_,
  y2 = NA_real_
)
```

Arguments

oddsRatioH0	The odds ratio under the null hypothesis. Defaults to 1.
n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.

Details

The Mantel-Haenszel sample size weights are used for stratified samples.

Value

The value of the score test statistic.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
zstatOddsRatio(oddsRatioH0 = 1, n1 = c(10,10), y1 = c(4,3),
               n2 = c(20,10), y2 = c(2,0))
```

| zstatRateDiff | *Miettinen-Nurminen Score Test Statistic for Two-Sample Rate Difference* |

Description

Obtains the Miettinen-Nurminen score test statistic for two-sample rate difference possibly with stratification.

Usage

```
zstatRateDiff(
  rateDiffH0 = 0,
  t1 = NA_real_,
  y1 = NA_real_,
  t2 = NA_real_,
  y2 = NA_real_
)
```

Arguments

rateDiffH0	The rate difference under the null hypothesis. Defaults to 0.
t1	The exposure for the active treatment group.
y1	The number of events for the active treatment group.
t2	The exposure for the control group.
y2	The number of events for the control group.

Details

The Mantel-Haenszel weights are used for stratified samples.

Value

The value of the score test statistic.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
zstatRateDiff(rateDiffH0 = 0, t1 = c(10,10), y1 = c(4,3),
              t2 = c(20,10), y2 = c(2,0))
```

---

zstatRateRatio	*Miettinen-Nurminen Score Test Statistic for Two-Sample Rate Ratio*

Description

Obtains the Miettinen-Nurminen score test statistic for two-sample rate ratio possibly with stratification.

Usage

```
zstatRateRatio(
  rateRatioH0 = 1,
  t1 = NA_real_,
  y1 = NA_real_,
  t2 = NA_real_,
  y2 = NA_real_
)
```

Arguments

rateRatioH0	The rate ratio under the null hypothesis. Defaults to 1.
t1	The exposure for the active treatment group.
y1	The number of events for the active treatment group.
t2	The exposure for the control group.
y2	The number of events for the control group.

Details

The Mantel-Haenszel weights are used for stratified samples.

Value

The value of the score test statistic.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
zstatRateRatio(rateRatioH0 = 1, t1 = c(10,10), y1 = c(4,3),
               t2 = c(20,10), y2 = c(2,0))
```

---

zstatRiskDiff   *Miettinen-Nurminen Score Test Statistic for Two-Sample Risk differ-
ence*

Description

Obtains the Miettinen-Nurminen score test statistic for two-sample risk difference possibly with
stratification.

Usage

```
zstatRiskDiff(
  riskDiffH0 = 0,
  n1 = NA_real_,
  y1 = NA_real_,
  n2 = NA_real_,
  y2 = NA_real_
)
```

Arguments

riskDiffH0	The risk difference under the null hypothesis. Defaults to 0.
n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.

Details

The Mantel-Haenszel sample size weights are used for stratified samples.

Value

The value of the score test statistic.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
zstatRiskDiff(riskDiffH0 = 0, n1 = c(10,10), y1 = c(4,3),
              n2 = c(20,10), y2 = c(2,0))
```

zstatRiskRatio	*Miettinen-Nurminen Score Test Statistic for Two-Sample Risk Ratio*

Description

Obtains the Miettinen-Nurminen score test statistic for two-sample risk ratio possibly with stratification.

Usage

```
zstatRiskRatio(
  riskRatioH0 = 1,
  n1 = NA_real_,
  y1 = NA_real_,
  n2 = NA_real_,
  y2 = NA_real_
)
```

Arguments

riskRatioH0	The risk ratio under the null hypothesis. Defaults to 1.
n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.

Details

The Mantel-Haenszel sample size weights are used for stratified samples.

Value

The value of the score test statistic.

Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

Examples

```
zstatRiskRatio(riskRatioH0 = 1, n1 = c(10,10), y1 = c(4,3),
               n2 = c(20,10), y2 = c(2,0))
```

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